Appendix: Laurent polynomial mirrors for 3–dimensional Fano manifolds

This table exhibits Laurent polynomial mirrors for each of the 105 deformation families of 3–dimensional Fano manifolds. The "Method" column summarizes the method by which we computed the quantum period in each case: "quantum Lefschetz" means "quantum Lefschetz with Fano ambient space and no mirror map"; "quantum Lefschetz with weak Fano ambient" means "quantum Lefschetz with non-Fano but weak Fano ambient space"; "quantum Lefschetz with mirror map" means "quantum Lefschetz with non-trivial mirror map"; the other entries should be self-explanatory. The "Minkowski ID" column records the ID in the Graded Ring and → the Database [CGK] of the corresponding Minkowski period sequence of manifold type; there are only 98 non-trivial entries in this column as only the 98 deformation families of 3–dimensional Fano manifolds with very ample anticanonical bundle give rise to Minkowski polynomial mirrors. There are in general many Minkowski polynomials (and infinitely many other Laurent polynomials) mirror to a given 3–dimensional Fano manifold, but we have listed only one such Laurent polynomial in each case.

Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds.

Name	Degree	Laurent polynomial	Method	Minkowski ID
V_2	2	$xy^6+6xy^5z+6xy^5+15xy^4z^2+30xy^4z+15xy^4+20xy^3z^3+60xy^3z^2+60xy^3z+20xy^3+15xy^2z^4+60xy^2z^3+90xy^2z^2+60xy^2z+15xy^2+6xyz^5+30xyz^4+60xyz^3+60xyz^2+30xyz+6xy+xz^6+6xz^5+15xz^4+20xz^3+15xz^2+6xz+x+\frac{6y^2}{z}+30y+\frac{30y}{z}+60z+\frac{60}{z}+\frac{60z^2}{y}+\frac{180z}{y}+\frac{180}{y}+\frac{60}{yz}+\frac{30z^3}{y^2}+\frac{120z^2}{y^2}+\frac{180z}{y^2}+\frac{120}{y^2}+\frac{30}{y^2z}+\frac{6z^4}{y^3}+\frac{30z^3}{y^3}+\frac{60z^2}{y^3}+\frac{60z}{y^3}+\frac{30}{y^3}+\frac{6}{y^3z}+\frac{15}{xy^2z^2}+\frac{60}{xy^3z}+\frac{60}{xy^3z^2}+\frac{90}{xy^4}+\frac{180}{xy^4z}+\frac{90}{xy^4z^2}+\frac{60z}{xy^5}+\frac{180}{xy^5}+\frac{180}{xy^5z}+\frac{60}{xy^5z^2}+\frac{15z^2}{xy^6}+\frac{60z}{xy^6}+\frac{90}{xy^6}+\frac{60}{xy^6z}+\frac{15}{xy^6z^2}+\frac{20}{x^2y^6z^3}+\frac{60}{x^2y^7z^2}+\frac{60}{x^2y^7z^3}+\frac{60}{x^2y^8z}+\frac{120}{x^2y^8z^2}+\frac{60}{x^2y^8z^3}+\frac{20}{x^2y^9}+\frac{60}{x^2y^9z}+\frac{60}{x^2y^9z^2}+\frac{20}{x^2y^9z^3}+\frac{15}{x^3y^{10}z^4}+\frac{30}{x^3y^{11}z^3}+\frac{30}{x^3y^{11}z^4}+\frac{15}{x^3y^{12}z^2}+\frac{30}{x^3y^{12}z^3}+\frac{15}{x^3y^{12}z^4}+\frac{6}{x^4y^{14}z^5}+\frac{6}{x^4y^{15}z^4}+\frac{6}{x^4y^{15}z^5}+\frac{1}{x^5y^{18}z^6}$	Weighted projective complete intersection	n/a
V_4	4	$xy^4+4xy^3z+4xy^3+6xy^2z^2+12xy^2z+6xy^2+4xyz^3+12xyz^2+12xyz+4xy+xz^4+4xz^3+6xz^2+4xz+x+\frac{4y^2}{z}+12y+\frac{12y}{z}+12z+\frac{12}{z}+\frac{4z^2}{y}+\frac{12z}{y}+\frac{12}{y}+\frac{4}{yz}+\frac{6}{xz^2}+\frac{12}{xyz}+\frac{12}{xyz^2}+\frac{6}{xy^2}+\frac{12}{xy^2z}+\frac{6}{xy^2z^2}+\frac{4}{x^2y^2z^3}+\frac{4}{x^2y^3z^2}+\frac{4}{x^2y^3z^3}+\frac{1}{x^3y^4z^4}$	Quantum Lefschetz	165

Continued on next page

Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
V_6	6	$xy^2z^3+3xy^2z^2+3xy^2z+xy^2+2xyz^3+6xyz^2+6xyz+2xy+xz^3+3xz^2+3xz+x+3yz+6y+\frac{3y}{z}+6z+\frac{6}{z}+\frac{3z}{y}+\frac{6}{y}+\frac{3}{yz}+\frac{3}{xz}+\frac{3}{xz^2}+\frac{6}{xyz}+\frac{6}{xyz^2}+\frac{3}{xy^2z}+\frac{3}{xy^2z^2}+\frac{1}{x^2yz^3}+\frac{2}{x^2y^2z^3}+\frac{1}{x^2y^3z^3}$	Quantum Lefschetz	164
V_8	8	$xy^2+2xyz^2+4xyz+2xy+xz^4+4xz^3+6xz^2+4xz+x+\frac{4y}{z}+4z+\frac{4}{z}+\frac{6}{xz^2}+\frac{2}{xy}+\frac{4}{xyz}+\frac{2}{xyz^2}+\frac{4}{x^2yz^3}+\frac{1}{x^3y^2z^4}$	Quantum Lefschetz	163
B_1	8	$xz^4+4xz^3+6xz^2+4xz+x+yz^4+4yz^3+6yz^2+4yz+y+\frac{2}{yz^2}+\frac{4}{yz^3}+\frac{2}{yz^4}+\frac{2}{xz^2}+\frac{4}{xz^3}+\frac{2}{xz^4}+\frac{1}{xy^2z^8}+\frac{1}{x^2yz^8}$	Weighted projective complete intersection	n/a
V_{10}	10	$xyz^3+3xyz^2+3xyz+xy+xz^2+2xz+x+yz^2+2yz+y+3z+\frac{3}{z}+\frac{2}{y}+\frac{2}{yz}+\frac{2}{x}+\frac{2}{xz}+\frac{3}{xyz}+\frac{3}{xyz^2}+\frac{1}{xy^2z^2}+\frac{1}{x^2yz^2}+\frac{1}{x^2y^2z^3}$	Abelian/non-Abelian correspondence	160
V_{12}	12	$x^2y^3z+x^2y^2z+2xy^2z+xy^2+2xyz+2xy+x+yz+3y+z+\frac{2}{y}+\frac{1}{x}+\frac{1}{xz}+\frac{2}{xy}+\frac{3}{xyz}+\frac{1}{xy^2}+\frac{3}{xy^2z}+\frac{1}{xy^3z}$	Abelian/non-Abelian correspondence	150
V_{14}	14	$xz+x+\frac{x}{yz}+yz^3+3yz^2+3yz+y+z+\frac{3}{z}+\frac{1}{yz}+\frac{3}{yz^2}+\frac{1}{y^2z^3}+\frac{z}{x}+\frac{1}{x}+\frac{1}{xyz}$	Abelian/non-Abelian correspondence	147
V_{16}	16	$x+\frac{2x}{yz}+\frac{x}{y^2z^2}+yz^2+2yz+y+2z+\frac{2}{z}+\frac{1}{y}+\frac{2}{yz}+\frac{1}{yz^2}+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Abelian/non-Abelian correspondence	143
B_2	16	$xy^2+2xyz+2xy+xz^2+2xz+x+\frac{2}{xz}+\frac{2}{xy}+\frac{2}{xyz}+\frac{1}{x^3y^2z^2}$	Weighted projective complete intersection	140
V_{18}	18	$xy^2+2xy+x+2y+z+\frac{1}{z}+\frac{2}{y}+\frac{1}{yz}+\frac{1}{x}+\frac{2z}{xy}+\frac{1}{xy}+\frac{1}{xy^2}+\frac{z}{x^2y^2}$	Abelian/non-Abelian correspondence	124
V_{22}	22	$xy+\frac{xy}{z}+x+y+\frac{2y}{z}+z+\frac{2z}{y}+\frac{1}{y}+\frac{z}{y^2}+\frac{y}{xz}+\frac{1}{x}$	Abelian/non-Abelian correspondence	113
B_3	24	$x+\frac{x}{yz}+y+z+\frac{2}{z}+\frac{2}{y}+\frac{y}{xz}+\frac{2}{x}+\frac{z}{xy}$	Quantum Lefschetz	106
B_4	32	$x+yz^2+2yz+y+\frac{2}{yz}+\frac{1}{xy^2z^2}$	Quantum Lefschetz	75
B_5	40	$x+y+z+\frac{1}{z}+\frac{1}{y}+\frac{1}{x}+\frac{1}{xyz}$	Abelian/non-Abelian correspondence	46
Q^3	54	$x+y+z+\frac{1}{xz}+\frac{1}{xy}$	Quantum Lefschetz	3
$\mathbb{P}^3$	64	$x+y+z+\frac{1}{xyz}$	Toric variety	1

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Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
$\mathrm{MM}_{2\text{–}1}$	4	$x^7y^7z^{18}+6x^6y^6z^{15}+6x^5y^5z^{13}+15x^5y^5z^{12}+30x^4y^4z^{10}+20x^4y^4z^9+x^4y^3z^9+x^3y^4z^9+15x^3y^3z^8+60x^3y^3z^7+15x^3y^3z^6+3x^3y^2z^6+3x^2y^3z^6+60x^2y^2z^5+60x^2y^2z^4+6x^2y^2z^3+3x^2yz^4+3x^2yz^3+3xy^2z^4+3xy^2z^3+20xyz^3+90xyz^2+30xyz+xy+6xz+x+6yz+y+\frac{60}{z}+\frac{6}{z^2}+\frac{3}{yz}+\frac{3}{yz^2}+\frac{3}{xz}+\frac{3}{xz^2}+\frac{15}{xyz^2}+\frac{60}{xyz^3}+\frac{15}{xyz^4}+\frac{3}{xy^2z^4}+\frac{3}{x^2yz^4}+\frac{30}{x^2y^2z^5}+\frac{20}{x^2y^2z^6}+\frac{1}{x^2y^3z^6}+\frac{1}{x^3y^2z^6}+\frac{6}{x^3y^3z^7}+\frac{15}{x^3y^3z^8}+\frac{6}{x^4y^4z^{10}}+\frac{1}{x^5y^5z^{12}}$	Hypersurface in product	n/a
$\mathrm{MM}_{2\text{–}2}$	6	$xy^2+2xyz+2xy+xz^2+2xz+x+\frac{y^2}{z}+4y+\frac{4y}{z}+6z+\frac{6}{z}+\frac{4z^2}{y}+\frac{14z}{y}+\frac{14}{y}+\frac{4}{yz}+\frac{z^3}{y^2}+\frac{4z^2}{y^2}+\frac{6z}{y^2}+\frac{4}{y^2}+\frac{1}{y^2z}+\frac{4}{xz}+\frac{12}{xy}+\frac{12}{xyz}+\frac{12z}{xy^2}+\frac{25}{xy^2}+\frac{12}{xy^2z}+\frac{4z^2}{xy^3}+\frac{12z}{xy^3}+\frac{12}{xy^3}+\frac{4}{xy^3z}+\frac{6}{x^2y^2z}+\frac{12}{x^2y^3}+\frac{12}{x^2y^3z}+\frac{6z}{x^2y^4}+\frac{12}{x^2y^4}+\frac{6}{x^2y^4z}+\frac{4}{x^3y^4z}+\frac{4}{x^3y^5}+\frac{4}{x^3y^5z}+\frac{1}{x^4y^6z}$	Quantum Lefschetz with mirror map	n/a
$\mathrm{MM}_{2\text{–}3}$	8	$x^2y^5z^2+4x^2y^4z^2+6x^2y^3z^2+4x^2y^2z^2+x^2yz^2+xy^3z^2+4xy^3z+2xy^2z^2+12xy^2z+xy^2+xyz^2+12xyz+2xy+4xz+x+2yz+6y+2z+\frac{2}{z}+\frac{6}{y}+\frac{2}{yz}+\frac{1}{xy}+\frac{4}{xyz}+\frac{4}{xy^2z}+\frac{1}{xy^2z^2}+\frac{1}{x^2y^3z^2}$	Hypersurface in product	n/a
$\mathrm{MM}_{2\text{–}4}$	10	$xyz^3+3xyz^2+3xyz+xy+xz^2+2xz+x+yz^2+2yz+y+4z+\frac{3}{z}+\frac{2}{y}+\frac{2}{yz}+\frac{2}{x}+\frac{2}{xz}+\frac{4}{xyz}+\frac{3}{xyz^2}+\frac{1}{xy^2z^2}+\frac{1}{x^2yz^2}+\frac{1}{x^2y^2z^3}$	Quantum Lefschetz	161
$\mathrm{MM}_{2\text{–}5}$	12	$\frac{x^2}{yz}+x+\frac{3x}{z}+\frac{3x}{y}+\frac{x}{yz}+y+\frac{3y}{z}+z+\frac{2}{z}+\frac{3z}{y}+\frac{2}{y}+\frac{y^2}{xz}+\frac{3y}{x}+\frac{y}{xz}+\frac{3z}{x}+\frac{2}{x}+\frac{z^2}{xy}+\frac{z}{xy}$	Quantum Lefschetz	158
$\mathrm{MM}_{2\text{–}6}$	12	$x^2yz^2+2xyz^2+2xyz+2xz+x+yz^2+2yz+y+2z+\frac{2}{z}+\frac{1}{y}+\frac{2}{yz}+\frac{1}{x}+\frac{2}{xz}+\frac{1}{xz^2}+\frac{2}{xyz}+\frac{2}{xyz^2}+\frac{1}{xy^2z^2}$	Quantum Lefschetz	149
$\mathrm{MM}_{2\text{–}7}$	14	$xy^3z^3+xy^2z^3+3xy^2z^2+xyz^2+3xyz+x+y^2z+yz+y+z+\frac{3}{yz}+\frac{1}{xz}+\frac{2}{xyz}+\frac{3}{xy^2z^2}+\frac{1}{x^2y^3z^3}$	Quantum Lefschetz	148
$\mathrm{MM}_{2\text{–}8}$	14	$\frac{x^2}{y^2z}+x+\frac{x}{y}+\frac{2x}{yz}+\frac{x}{y^2}+yz+y+z+\frac{1}{z}+\frac{3}{y}+\frac{y^2z}{x}+\frac{2yz}{x}+\frac{y}{x}+\frac{3}{x}+\frac{y^2z}{x^2}+\frac{y}{x^2}$	Quantum Lefschetz with weak Fano ambient	144
$\mathrm{MM}_{2\text{–}9}$	16	$x+\frac{x}{z}+\frac{x}{yz}+\frac{x}{yz^2}+yz^2+2yz+y+2z+\frac{2}{z}+\frac{1}{y}+\frac{1}{yz}+\frac{1}{yz^2}+\frac{yz}{x}+\frac{2}{x}+\frac{1}{xyz}$	Quantum Lefschetz	139

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Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
$\mathrm{MM}_{2\text{–}10}$	16	$xy^2+2xy+x+\frac{x}{z}+y^2z+2yz+2y+z+\frac{2}{y}+\frac{2}{yz}+\frac{1}{x}+\frac{2}{xy}+\frac{1}{xy^2}+\frac{1}{xy^2z}$	Quantum Lefschetz	145
$\mathrm{MM}_{2\text{–}11}$	18	$x+\frac{x}{z}+\frac{x}{y}+yz+y+z+\frac{2}{z}+\frac{2}{y}+\frac{yz}{x}+\frac{y}{x}+\frac{z}{x}+\frac{1}{x}+\frac{1}{xz}+\frac{1}{xy}$	Quantum Lefschetz	120
$\mathrm{MM}_{2\text{–}12}$	20	$\frac{x^2}{yz}+x+\frac{x}{y}+\frac{2x}{yz}+y+z+\frac{1}{y}+\frac{1}{yz}+\frac{2yz}{x}+\frac{y}{x}+\frac{1}{x}+\frac{y^2z}{x^2}$	Quantum Lefschetz	118
$\mathrm{MM}_{2\text{–}13}$	20	$xy+x+\frac{x}{z}+y+z+\frac{2}{z}+\frac{z}{y}+\frac{2}{y}+\frac{1}{yz}+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Quantum Lefschetz	119
$\mathrm{MM}_{2\text{–}14}$	20	$xy^2+2xy+x+2y+z+\frac{2}{y}+\frac{1}{x}+\frac{z}{xy}+\frac{1}{xy}+\frac{1}{xyz}+\frac{1}{xy^2}+\frac{1}{xy^2z}$	Hypersurface in product	122
$\mathrm{MM}_{2\text{–}15}$	22	$x+\frac{x}{z}+\frac{x}{yz}+y+\frac{y}{z}+z+\frac{2}{z}+\frac{2}{y}+\frac{y}{xz}+\frac{2}{x}+\frac{z}{xy}$	Quantum Lefschetz	109
$\mathrm{MM}_{2\text{–}16}$	22	$xy+x+y+z+\frac{1}{z}+\frac{z}{y}+\frac{2}{y}+\frac{1}{yz}+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Quantum Lefschetz	104
$\mathrm{MM}_{2\text{–}17}$	24	$\frac{x^2}{yz}+\frac{x^2}{yz^2}+x+\frac{2x}{z}+\frac{x}{yz}+y+z+\frac{2z}{x}+\frac{1}{x}+\frac{z}{x^2}$	Abelian/non-Abelian correspondence	101
$\mathrm{MM}_{2\text{–}18}$	24	$x+\frac{x}{z}+\frac{x}{yz}+yz+y+z+\frac{1}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	74
$\mathrm{MM}_{2\text{–}19}$	26	$\frac{x^2}{yz}+x+\frac{2x}{yz}+y+z+\frac{1}{yz}+\frac{2yz}{x}+\frac{y}{x}+\frac{y^2z}{x^2}$	Quantum Lefschetz	86
$\mathrm{MM}_{2\text{–}20}$	26	$x+\frac{x}{y}+y+\frac{y}{z}+z+\frac{1}{z}+\frac{1}{y}+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Abelian/non-Abelian correspondence	87
$\mathrm{MM}_{2\text{–}21}$	28	$x+\frac{x}{yz}+y^2z+2yz+y+z+\frac{2}{yz}+\frac{1}{xyz}$	Abelian/non-Abelian correspondence	84
$\mathrm{MM}_{2\text{–}22}$	30	$xy+x+\frac{x}{z}+y+z+\frac{1}{z}+\frac{1}{y}+\frac{1}{x}+\frac{z}{xy}$	Abelian/non-Abelian correspondence	69
$\mathrm{MM}_{2\text{–}23}$	30	$x^2y+2xy+x+y+z+\frac{2}{xy}+\frac{1}{x^2y^2z}$	Quantum Lefschetz	78
$\mathrm{MM}_{2\text{–}24}$	30	$\frac{xy}{z}+x+\frac{x}{z}+y+z+\frac{z}{y}+\frac{1}{y}+\frac{y}{x}+\frac{1}{x}$	Quantum Lefschetz	44
$\mathrm{MM}_{2\text{–}25}$	32	$x+\frac{x}{z}+y+z+\frac{1}{y}+\frac{1}{yz}+\frac{yz}{x}+\frac{1}{x}$	Quantum Lefschetz	43
$\mathrm{MM}_{2\text{–}26}$	34	$xy+x+y+z+\frac{1}{z}+\frac{1}{y}+\frac{1}{x}+\frac{1}{xyz}$	Abelian/non-Abelian correspondence	58
$\mathrm{MM}_{2\text{–}27}$	38	$x+\frac{x}{z}+y+z+\frac{1}{yz}+\frac{1}{x}+\frac{1}{xy}$	Quantum Lefschetz	19
$\mathrm{MM}_{2\text{–}28}$	40	$xyz^2+xyz+x+y+z+\frac{1}{yz}+\frac{1}{xz}$	Quantum Lefschetz	5

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Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
$\mathrm{MM}_{2\text{–}29}$	40	$x+\frac{x}{y}+y+z+\frac{2}{x}+\frac{1}{x^2z}$	Quantum Lefschetz	35
$\mathrm{MM}_{2\text{–}30}$	46	$xyz+x+y+z+\frac{1}{xz}+\frac{1}{xy}$	Quantum Lefschetz	4
$\mathrm{MM}_{2\text{–}31}$	46	$x+\frac{x}{y}+y+z+\frac{1}{yz}+\frac{1}{x}$	Quantum Lefschetz	15
$\mathrm{MM}_{2\text{–}32}$	48	$x+y+z+\frac{1}{y}+\frac{1}{x}+\frac{1}{xyz}$	Quantum Lefschetz	24
$\mathrm{MM}_{2\text{–}33}$	54	$x+\frac{x}{z}+y+z+\frac{1}{xy}$	Toric variety	2
$\mathrm{MM}_{2\text{–}34}$	54	$x+y+z+\frac{1}{yz}+\frac{1}{x}$	Toric variety	10
$\mathrm{MM}_{2\text{–}35}$	56	$x+\frac{x}{yz}+y+z+\frac{1}{x}$	Toric variety	7
$\mathrm{MM}_{2\text{–}36}$	62	$\frac{x^2}{yz}+x+y+z+\frac{1}{x}$	Toric variety	6
$\mathrm{MM}_{3\text{–}1}$	12	$xy^2+2xyz+2xy+xz^2+2xz+x+2y+\frac{2y}{z}+2z+\frac{2}{z}+\frac{2z}{y}+\frac{2}{y}+\frac{1}{x}+\frac{2}{xz}+\frac{1}{xz^2}+\frac{2}{xy}+\frac{2}{xyz}+\frac{1}{xy^2}$	Quantum Lefschetz with weak Fano ambient	154
$\mathrm{MM}_{3\text{–}2}$	14	$xyz^2+xyz+3xz+x+\frac{3x}{y}+\frac{x}{y^2z}+3yz+y+z+\frac{1}{y}+\frac{3}{yz}+\frac{3y}{x}+\frac{1}{x}+\frac{3}{xz}+\frac{y}{x^2z}$	Quantum Lefschetz with mirror map	157
$\mathrm{MM}_{3\text{–}3}$	18	$x+\frac{2x}{y}+\frac{x}{yz}+\frac{x}{y^2}+yz+y+z+\frac{2}{z}+\frac{2}{y}+\frac{yz}{x}+\frac{2y}{x}+\frac{y}{xz}+\frac{1}{x}$	Quantum Lefschetz	135
$\mathrm{MM}_{3\text{–}4}$	18	$xyz+x+yz^2+2yz+y+2z+\frac{2}{z}+\frac{1}{y}+\frac{2}{yz}+\frac{1}{yz^2}+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Quantum Lefschetz with weak Fano ambient	142
$\mathrm{MM}_{3\text{–}5}$	20	$xyz+xz^2+2xz+x+y+2z+\frac{2}{z}+\frac{1}{y}+\frac{1}{yz}+\frac{1}{x}+\frac{2}{xz}+\frac{1}{xz^2}$	Quantum Lefschetz with mirror map	138
$\mathrm{MM}_{3\text{–}6}$	22	$\frac{x^2}{yz}+\frac{x^2}{y^2z}+x+\frac{2x}{y}+\frac{x}{yz}+y+z+\frac{1}{y}+\frac{2y}{x}+\frac{2}{x}+\frac{y}{x^2}$	Quantum Lefschetz	117
$\mathrm{MM}_{3\text{–}7}$	24	$\frac{xy}{z}+x+\frac{x}{z}+\frac{x}{y}+y+z+\frac{2}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	103
$\mathrm{MM}_{3\text{–}8}$	24	$x+\frac{x}{z}+\frac{x}{y}+y+\frac{y}{z}+z+\frac{1}{z}+\frac{2}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	112
$\mathrm{MM}_{3\text{–}9}$	26	$\frac{x^2}{yz}+x+\frac{2x}{yz}+y+z+\frac{1}{yz}+\frac{y}{x}+\frac{z}{x}+\frac{1}{x}$	Quantum Lefschetz	22
$\mathrm{MM}_{3\text{–}10}$	26	$\frac{xy}{z}+x+\frac{x}{y}+y+z+\frac{2}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	99

Continued on next page

Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
$\mathrm{MM}_{3\text{–}11}$	28	$x+\frac{x}{z}+\frac{x}{yz}+y+z+\frac{1}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	72
$\mathrm{MM}_{3\text{–}12}$	28	$xz+x+y+\frac{y}{z}+z+\frac{1}{z}+\frac{z}{y}+\frac{1}{y}+\frac{y}{xz}+\frac{1}{x}$	Quantum Lefschetz	85
$\mathrm{MM}_{3\text{–}13}$	30	$xy+x+y+z+\frac{1}{z}+\frac{1}{y}+\frac{1}{yz}+\frac{z}{x}+\frac{1}{x}$	Quantum Lefschetz	70
$\mathrm{MM}_{3\text{–}14}$	32	$\frac{x^2}{yz}+x+\frac{x}{yz}+y+z+\frac{y}{x}+\frac{z}{x}+\frac{1}{x}$	Quantum Lefschetz with weak Fano ambient	21
$\mathrm{MM}_{3\text{–}15}$	32	$x+\frac{x}{yz}+y+z+\frac{1}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	67
$\mathrm{MM}_{3\text{–}16}$	34	$x+\frac{x}{y}+y+\frac{y}{z}+z+\frac{1}{y}+\frac{y}{xz}+\frac{1}{x}$	Quantum Lefschetz with weak Fano ambient	42
$\mathrm{MM}_{3\text{–}17}$	36	$x+y+\frac{y}{z}+z+\frac{1}{y}+\frac{y}{xz}+\frac{1}{x}+\frac{1}{xy}$	Quantum Lefschetz	39
$\mathrm{MM}_{3\text{–}18}$	36	$x+\frac{x}{y}+y+z+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Quantum Lefschetz	41
$\mathrm{MM}_{3\text{–}19}$	38	$xz+x+y+z+\frac{1}{yz}+\frac{1}{x}+\frac{1}{xyz}$	Quantum Lefschetz	18
$\mathrm{MM}_{3\text{–}20}$	38	$xy+x+y+z+\frac{1}{y}+\frac{1}{x}+\frac{1}{xyz}$	Quantum Lefschetz	38
$\mathrm{MM}_{3\text{–}21}$	38	$x+yz+y+z+\frac{1}{z}+\frac{1}{y}+\frac{yz}{x}+\frac{1}{x}$	Quantum Lefschetz	49
$\mathrm{MM}_{3\text{–}22}$	40	$xz+x+\frac{x}{yz}+y+z+\frac{1}{yz}+\frac{1}{x}$	Quantum Lefschetz	13
$\mathrm{MM}_{3\text{–}23}$	42	$xz+x+\frac{x}{y}+y+z+\frac{1}{yz}+\frac{1}{x}$	Quantum Lefschetz	17
$\mathrm{MM}_{3\text{–}24}$	42	$x+y+z+\frac{1}{y}+\frac{y}{x}+\frac{1}{x}+\frac{1}{xyz}$	Quantum Lefschetz	31
$\mathrm{MM}_{3\text{–}25}$	44	$x+\frac{x}{z}+y+z+\frac{1}{x}+\frac{1}{xy}$	Toric variety	16
$\mathrm{MM}_{3\text{–}26}$	46	$xy+x+y+z+\frac{1}{yz}+\frac{1}{x}$	Toric variety	12
$\mathrm{MM}_{3\text{–}27}$	48	$x+y+z+\frac{1}{z}+\frac{1}{y}+\frac{1}{x}$	Toric variety	45
$\mathrm{MM}_{3\text{–}28}$	48	$x+\frac{x}{z}+y+z+\frac{1}{y}+\frac{1}{x}$	Toric variety	28
$\mathrm{MM}_{3\text{–}29}$	50	$xy+x+\frac{x}{yz}+y+z+\frac{1}{x}$	Toric variety	8

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Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
$\mathrm{MM}_{3\text{–}30}$	50	$x+\frac{x}{y}+y+\frac{y}{z}+z+\frac{1}{x}$	Toric variety	11
$\mathrm{MM}_{3\text{–}31}$	52	$x+\frac{x}{z}+\frac{x}{y}+y+z+\frac{1}{x}$	Toric variety	14
$\mathrm{MM}_{4\text{–}1}$	24	$x^2z+2xz+x+y+z+\frac{1}{y}+\frac{y}{xz}+\frac{1}{x}+\frac{2}{xz}+\frac{1}{xyz}$	Quantum Lefschetz	111
$\mathrm{MM}_{4\text{–}2}$	26	$x+\frac{x}{z}+\frac{x}{y}+y+z+\frac{1}{z}+\frac{2}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz with mirror map	110
$\mathrm{MM}_{4\text{–}3}$	28	$\frac{x^2}{y^2z}+x+\frac{2x}{y}+y+z+\frac{2y}{x}+\frac{1}{x}+\frac{y}{x^2}$	Quantum Lefschetz	88
$\mathrm{MM}_{4\text{–}4}$	30	$x+y+z+\frac{1}{z}+\frac{z}{y}+\frac{2}{y}+\frac{1}{yz}+\frac{y}{x}+\frac{1}{x}$	Quantum Lefschetz	83
$\mathrm{MM}_{4\text{–}5}$	32	$x+\frac{x}{z}+y+z+\frac{1}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz	68
$\mathrm{MM}_{4\text{–}6}$	32	$x+y+\frac{y}{z}+z+\frac{1}{z}+\frac{z}{y}+\frac{1}{y}+\frac{y}{x}+\frac{1}{x}$	Quantum Lefschetz with weak Fano ambient	81
$\mathrm{MM}_{4\text{–}7}$	34	$x+\frac{x}{y}+y+z+\frac{1}{y}+\frac{z}{x}+\frac{2}{x}+\frac{1}{xz}$	Quantum Lefschetz	65
$\mathrm{MM}_{4\text{–}8}$	36	$x+y+z+\frac{1}{z}+\frac{z}{y}+\frac{1}{y}+\frac{1}{x}+\frac{1}{xz}$	Quantum Lefschetz	57
$\mathrm{MM}_{4\text{–}9}$	38	$xy+x+y+z+\frac{1}{y}+\frac{2}{x}+\frac{1}{x^2z}$	Quantum Lefschetz	54
$\mathrm{MM}_{4\text{–}10}$	40	$xy+x+y+z+\frac{1}{y}+\frac{1}{yz}+\frac{1}{x}$	Toric variety	37
$\mathrm{MM}_{4\text{–}11}$	42	$xy+x+y+z+\frac{1}{z}+\frac{1}{y}+\frac{1}{x}$	Product	48
$\mathrm{MM}_{4\text{–}12}$	44	$xy+x+\frac{x}{z}+y+z+\frac{1}{y}+\frac{1}{x}$	Toric variety	34
$\mathrm{MM}_{4\text{–}13}$	46	$xy+\frac{xy}{z}+x+y+z+\frac{1}{y}+\frac{1}{x}$	Toric variety	29
$\mathrm{MM}_{5\text{–}1}$	28	$x+\frac{x}{z}+\frac{x}{y}+y+z+\frac{2}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Quantum Lefschetz with weak Fano ambient	100
$\mathrm{MM}_{5\text{–}2}$	36	$x+\frac{x}{z}+\frac{x}{y}+y+z+\frac{1}{y}+\frac{y}{x}+\frac{1}{x}$	Toric variety	64
$\mathrm{MM}_{5\text{–}3}$	36	$x+y+\frac{y}{z}+z+\frac{1}{z}+\frac{z}{y}+\frac{1}{y}+\frac{1}{x}$	Product	76

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Table 1: Mirror Laurent polynomials for 3-dimensional Fano manifolds – continued from previous page

Name	Degree	Laurent polynomial	Method	Minkowski ID
MM_{6-1}	30	$x+\frac{x}{y}+y+z+\frac{1}{z}+\frac{2}{y}+\frac{y}{x}+\frac{2}{x}+\frac{1}{xy}$	Product	107
MM_{7-1}	24	$x+yz^2+2yz+y+2z+\frac{2}{z}+\frac{1}{y}+\frac{2}{yz}+\frac{1}{yz^2}+\frac{1}{x}$	Product	136
MM_{8-1}	18	$x+yz^3+3yz^2+3yz+y+3z+\frac{3}{z}+\frac{3}{yz}+\frac{3}{yz^2}+\frac{1}{y^2z^3}+\frac{1}{x}$	Product	155
MM_{9-1}	12	$xz^4+4xz^3+6xz^2+4xz+x+y+4z^2+12z+\frac{4}{z}+\frac{1}{y}+\frac{6}{x}+\frac{12}{xz}+\frac{6}{xz^2}+\frac{4}{x^2z^2}+\frac{4}{x^2z^3}+\frac{1}{x^3z^4}$	Product	n/a
MM_{10-1}	6	$xz^6+6xz^5+15xz^4+20xz^3+15xz^2+6xz+x+y+6z^3+30z^2+60z+\frac{30}{z}+\frac{6}{z^2}+\frac{1}{y}+\frac{15}{x}+\frac{60}{xz}+\frac{90}{xz^2}+\frac{60}{xz^3}+\frac{15}{xz^4}+\frac{20}{x^2z^3}+\frac{60}{x^2z^4}+\frac{60}{x^2z^5}+\frac{20}{x^2z^6}+\frac{15}{x^3z^6}+\frac{30}{x^3z^7}+\frac{15}{x^3z^8}+\frac{6}{x^4z^9}+\frac{6}{x^4z^{10}}+\frac{1}{x^5z^{12}}$	Product	n/a

References

[CGK] Tom Coates, Sergey Galkin, and Alexander Kasprzyk. $3d$ minkowski period sequences. online resource. `http://www.grdb.co.uk/forms/period3`.