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Junhua Xiao, Chuanfu Shi, Yaoling Xu and Fucheng Zhang

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INTERFACE STRESS OF ORTHOTROPIC MATERIALS WITH A NANODEFECT UNDER ANTIPLANE SHEAR LOADING

JUNHUA XIAO, CHUANFU SHI, YAOLING XU AND FUCHENG ZHANG

A theoretical study is conducted on an orthotropic solid with a nanodefect (e.g., inclusion, hole, or crack) under far-field antiplane shear loading. A rigorous analytical solution of the stress fields is presented using the Gurtin–Murdoch surface/interface model and a conformal mapping technique. Several new and existing solutions are considered for the special and degenerated cases. The major results of the study are as follows:

- (1) Interface stresses are greatly dependent on size when the size of a defect is at the nanometer scale, and the interface stresses approach the classical elasticity results when a defect has large characteristic dimensions.
- (2) The interface effect of a nanodefect decreases with an increase in defect section aspect ratio.
- (3) When the modulus of the defect (inclusion) increases, the interface effect decreases, i.e., the interface effect can be neglected when the inclusion is sufficiently hard.

1. Introduction

Several composite materials can be regarded as orthotropic solids in engineering applications. The general properties, as well as the fracture and damage properties, of orthotropic solids have received considerable attention with respect to elastic-plastic and fracture damage theories. When the size of defects (e.g., inclusion, hole, or crack) in an orthotropic solid is at the nanometer scale, the interface effect of nanodefects plays an important role in micromechanical properties because of the high surface-to-volume ratios of this solid material [Nan and Wang 2013; Grekov and Yazovskaya 2014].

In recent years, significant progress has been made in addressing the fracture characteristics of orthotropic solids with holes or cracks from a fundamental perspective by applying classical elastoplastic theory. Tang and Hwang [1991] discussed the near-tip field solution for a plane stress mode I stationary crack in an elastic-perfectly orthotropic plastic material based on phenomenological plasticity theory. Gao and Tong [1995] used the Cauchy integral method to study the fundamental solutions for the complex stress functions and the stress intensity factors of an equal-parameter orthotropic plate with an elliptical hole or crack. Ozturk and Erdogan [1997] formulated the mode I crack problem for an inhomogeneous orthotropic plane and obtained a solution for various loading conditions and material parameters. Kim, Lee, and Joo [1999] presented a numerical solution by applying the Fourier integral transform method on the problem of a three-layered orthotropic material with a center crack that was subjected to an arbitrary antiplane shear loading. Berbinau and Soutis [2001] presented a new analytical method for solving mixed boundary value problems along holes in orthotropic plates. Kwon and Meguid [2002] proposed a general solution for the field intensity factors and the energy release rate of a Griffith crack normal to

Keywords: orthotropic materials, nanodefects, interface stresses, antiplane shear, Gurtin–Murdoch surface/interface model.

the interface between a rectangular piezoelectric ceramic and two of the same rectangular orthotropic materials with finite lengths under combined in-plane electrical and antiplane mechanical loadings. Lee, Kwon, Lee, and Kwon [2002] provided the dynamic field intensity factors for the problem of an interfacial crack moving along the interface between a piezoelectric material and two orthotropic materials under electromechanical longitudinal shear loading. Li [2003] analytically determined the stress intensity factors for the problem of an orthotropic strip with two collinear cracks normal to the strip boundaries under remote uniform antiplane shear loading. Faal and Fariborz [2007] derived the stress fields in an orthotropic infinite plane with Volterra-type climb and glide edge dislocations. Chalivendra [2008] developed quasistatic stress fields for a crack oriented along one of the principal axes of an inhomogeneous orthotropic medium by conducting asymptotic analysis coupled with the Westergaard stress function approach. Zhang and Deng [2008] derived elastic stress fields near the cohesive zone of a crack aligned with the principal axes of a degenerated orthotropic material using complex variable and eigenfunction expansion methods. Xiao and Jiang [2009] obtained a closed-form solution for orthotropic materials weakened by a doubly periodic array of cracks under far-field antiplane shear loading by applying elliptical function and analytical function theories on the boundary value problems. Moharrami and Ayatollahi [2011] conducted stress analysis on an orthotropic plane with a Volterra-type dislocation. The distributed dislocation technique was adopted to obtain the integral equations for an orthotropic plane weakened by cracks under time-harmonic antiplane traction. Goldstein and Shifrin [2012] investigated a crack that was initially located on a symmetry axis of an orthotropic plane and subjected to biaxial loading. Liu and Zhou [2014] presented a solution for a plane rectangular crack in a 3D infinite orthotropic elastic material by applying a generalization of Almansi's theorem and the Schmidt method. Liu, Zhou, Wu, and Wu [2015] investigated a nonlocal theory solution for a rectangular crack in a 3D infinite orthotropic elastic medium using a generalization of Almansi's theorem and the Schmidt method. Peng, Li, and Feng [2015] investigated the interaction between a mode I crack and a symmetrical shape inclusion in an orthotropic medium subjected to remote stress by using transformation toughening theory and the Eshelby inclusion method.

Extensive investigations have also been conducted on the effective properties of orthotropic composite solids. Zhao and Yu [2000] presented a model for orthotropic damage on materials by combining the macroscopic mechanical properties with the microstructure parameters of a material based on Eshelby's equivalence principle. Bouyge, Jasiuk, Boccara, and Ostoja-Starzewski [2002] determined the couple-stress moduli and characteristic lengths of a 2D matrix-inclusion composite with the inclusions arranged in a periodic square array and both linear elastic constituents being of Cauchy type. Yang and Becker [2004] studied the effective properties and microscopic deformation of anisotropic plates with periodic holes via direct mathematical homogenization. Ieşan and Scalia [2007] investigated linear theory of inhomogeneous and orthotropic elastic materials with voids. Nie, Chan, Shin, and Roy [2008] presented analytic solutions for elastic fields induced by normal and shear eigenstrains in an elliptical region embedded into orthotropic composite materials by applying conformal transformation and the complex function method. Monchiet, Gruescu, Cazacu, and Kondo [2012] achieved effective compliance of an orthotropic medium with arbitrarily oriented cracks by using newly derived expressions of the Eshelby tensor.

The present work constitutes research on the interface stresses of an orthotropic solid with a nanodefect. A closed-form solution for the problem of orthotropic materials with a nanosized elliptical defect is presented under antiplane shear loading by applying the Gurtin–Murdoch surface/interface model and a

conformal mapping technique. The influences of defect size, matrix material moduli ratio, defect shape ratio, and defect elastic property on stress fields are discussed.

2. Computational model and basic equations

A schematic diagram of an orthotropic solid with an isotropic nanodefect (i.e., nanoelliptical inclusion) that considers the interface effect is presented in Figure 1. Regions $\Omega_{\rm I}$ and $\Omega_{\rm M}$ denote the elliptical defect and the matrix, respectively. The Gurtin–Murdoch surface/interface model [Gurtin and Murdoch 1975; 1978; Gurtin et al. 1998] indicates that interface L can be regarded as a layer without thickness and with different material properties from the defect and the matrix. The semimajor and semiminor axes of the elliptical defect are denoted as a and b, respectively. I, 0, and M denote the defect, interface, and matrix, respectively. $G_{\rm I}$ denotes the antiplane shear modulus of the defect (inclusion). C_{44} and C_{55} are the principal shear moduli of the orthotropic solid, which are located along the y- and x-axes in Figure 1, respectively. The Oz-axis is perpendicular to the section in the Cartesian coordinate system. The matrix is subjected to far-field antiplane shear stress τ_{vz}^{∞} .

The governing equation and the constitutive equation of the matrix can be given as [Li 2003]

$$\frac{\partial \tau_{xz}}{\partial x} + \frac{\partial \tau_{yz}}{\partial y} = 0,\tag{1}$$

where w is the antiplane displacement.

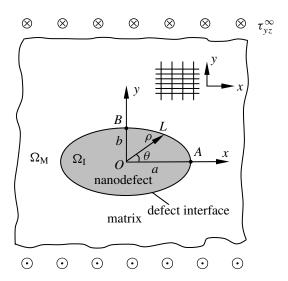


Figure 1. Schematic diagram of an orthotropic solid with an nanodefect (nanoelliptic inclusion) considering interface effect (z-plane, z = x + iy).

Nonclassical boundary conditions on nanodefect interface L can be written as [Luo and Wang 2009; Sharma et al. 2003]

$$w_{\rm P}(t) = w_{\rm M}(t) \qquad t = \rho e^{\mathrm{i}\theta}, \tag{3}$$

$$\tau_{rz}^{P}(t) - \tau_{rz}^{M}(t) = \frac{2\mu^{S}}{\rho} \frac{\partial \epsilon_{\theta z}^{0}}{\partial \theta} \quad t = \rho e^{i\theta}, \tag{4}$$

where (ρ,θ) denotes the polar coordinates on the interface L; $\tau^0_{\theta z}$ and $\epsilon^0_{\theta z}$ denote the stress and strain components on the interface, respectively; $\mu^S = C^S_{44} |\sin\theta| + C^S_{55} |\cos\theta|$; and C^S_{44} and C^S_{55} denote the interface elastic constants along the y- and x-axes in Figure 1, respectively. The unit for interface elastic constants C^S_{44} and C^S_{55} is N/m. The expression of μ^S in terms of θ is merely an assumption made by the authors

The interfacial strain for a coherent interface is equal to the associated tangential strain in the abutting materials, i.e.,

$$\epsilon_{\theta z}^{0} = \epsilon_{\theta z}^{P} = \epsilon_{\theta z}^{M}. \tag{5}$$

3. Analysis and solution

By substituting (2) into (1), a second-order linear homogeneous partial differential equation with constant coefficients on w is obtained as

$$C_{55}\frac{\partial^2 w}{\partial x^2} + C_{44}\frac{\partial^2 w}{\partial y^2} = 0. ag{6}$$

The solution for (6) can be expressed as

$$w = \operatorname{Re}F(z_m),\tag{7}$$

where $f(z_m)$ is an analytical function with respect to z_m , $z_m = x + \mathrm{i} m y$, and $m = \sqrt{C_{55}/C_{44}}$. By substituting (7) into (2), the expressions obtained are

$$\tau_{xz} = C_{55} \frac{\partial \operatorname{Re} f(z_m)}{\partial x} = C_{55} \operatorname{Re} f'(z_m),$$

$$\tau_{yz} = mC_{44} \frac{\partial \operatorname{Re} f(z_m)}{\partial (my)} = -mC_{44} \operatorname{Im} f'(z_m),$$
(8)

where $f'(z_m)$ denotes the derivative with respect to z_m . Then, (8) can be rewritten as

$$\frac{\tau_{xz}}{C_{55}} - i \frac{\tau_{yz}}{\sqrt{C_{44}C_{55}}} = \text{Re}\,f'(z_m) + i\text{Im}\,f'(z_m) = f'(z_m). \tag{9}$$

The z_m -plane (Figure 2) is generated by the map of $z_m = x + imy$ from the z-plane (Figure 1), where O_1 and O_2 denote the foci of the elliptical inclusion.

To solve the problem in Figure 2, a new variable ζ is introduced as

$$\zeta = \xi + i\eta = le^{i\phi},\tag{10}$$

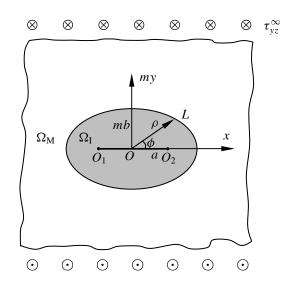


Figure 2. z_m -plane corresponding to the plane z ($z_m = x + imy$).

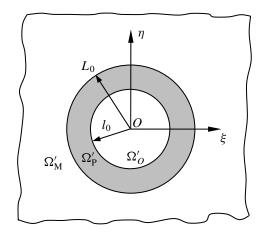


Figure 3. Conformal mapping in the ζ -plane ($\zeta = \xi + i\eta$).

where (l, ϕ) denotes the polar coordinates in the ζ -plane. The z_m -plane is mapped onto the ζ -plane via conformal transformation,

$$z_m = \Omega(\zeta) = \zeta + \frac{n}{\zeta},\tag{11}$$

where $n = (a^2 - m^2b^2)/4$. Region $\Omega_{\rm I}$ in the z_m -plane is mapped onto circular region $\Omega'_{\rm O}$, with radius l_0 , and circular region $\Omega'_{\rm P}$, with radius L_0 , shown in Figure 3, respectively.

From the transformation relationship between Figures 2 and 3, the equations obtained are

$$x = \xi + \frac{n\xi}{\xi^2 + \eta^2}, \quad my = \eta - \frac{n\eta}{\xi^2 + \eta^2}.$$
 (12)

From (12), the following expressions are derived:

$$l_0 = \sqrt{n},\tag{13}$$

$$L_0 = \frac{a + mb}{2}.\tag{14}$$

In an annular region, an analytical function $F(\zeta)$ can be expanded into a Laurent series [Muskhelishvili 1953]:

$$F(\zeta) = a^* \ln \zeta + \sum_{k=-\infty}^{\infty} a_k \zeta^k, \tag{15}$$

where a^* and a_k are complex constants to be determined. The exact solution can be obtained by taking the following finite terms of the series:

$$F_{\rm I}(\zeta) = A_1 \left(\zeta + n/\zeta \right) = A_1 \left(l e^{i\phi} + \frac{n e^{-i\phi}}{l} \right) \quad \text{in } \Omega_{\rm I}', \tag{16}$$

$$F_{\rm M}(\zeta) = B_1 \zeta + B_{-1} \frac{1}{\zeta} = B_1 l e^{i\phi} + \frac{B_{-1}}{l} e^{-i\phi} \quad \text{in } \Omega_{\rm M}',$$
 (17)

where A_1 , B_1 , and B_{-1} are complex constants.

By applying far-field conditions, coefficient B_1 can be obtained from (9) and (17) as

$$B_1 = -i \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}}. (18)$$

The boundary conditions on L_0 in Figure 3 can be summarized as

$$w_{\mathbf{I}}(z) = w_{\mathbf{M}}(z),\tag{19}$$

$$\tau_{rz}^{\rm I}(z) - \tau_{rz}^{\rm M}(z) = \frac{2\mu^{\rm S}}{L_0} \frac{\partial \epsilon_{\theta z}^{L_0}}{\partial \theta},\tag{20}$$

where $\mu^S = C_{44}^S |\sin \theta| + C_{55}^S |\cos \theta|$, and C_{44}^S and C_{55}^S denote the interface elastic constants along the y-and x-axes in Figure 1, respectively.

From boundary conditions (19) and (20), the expressions obtained are

$$\left(1 + \frac{n}{L_0^2}\right) A_1 = B_1 - \frac{B_{-1}}{L_0^2},$$
(21)

$$\[G_{\rm I}\left(1 - \frac{n}{L_0^2}\right) + \frac{\mu^S}{L_0}\left(1 + \frac{n}{L_0^2}\right)\] A_1 = C_{44}\left(B_1 + \frac{B_{-1}}{L_0^2}\right). \tag{22}$$

By integrating (21) and (22) into (18), the expressions

$$A_1 = S_1 B_1, \quad B_{-1} = S_{-1} B_1,$$
 (23)

are derived, where

$$S_{1} = \frac{2C_{44}}{G_{I}(1 - n/L_{0}^{2}) + (\mu^{S}/L_{0})(1 + n/L_{0}^{2}) + C_{44}(1 + n/L_{0}^{2})},$$

$$S_{-1} = \frac{G_{I}(1 - n/L_{0}^{2}) + (\mu^{S}/L_{0})(1 + n/L_{0}^{2}) - C_{44}(1 + n/L_{0}^{2})}{G_{I}(1 - n/L_{0}^{2}) + (\mu^{S}/L_{0})(1 + n/L_{0}^{2}) + C_{44}(1 + n/L_{0}^{2})}L_{0}^{2}.$$
(24)

From (9), (16), (17), (18), and (23), the overall stress fields in the composites can be expressed as

$$\tau_{yz} + i\tau_{xz} = G_1 S_1 \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}} \qquad \text{in the inclusion,}$$
 (25)

$$\frac{\tau_{yz}}{\sqrt{C_{44}C_{55}}} + i\frac{\tau_{xz}}{C_{55}} = \frac{\zeta^2 - S_{-1}}{\zeta^2 - n} \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}} \quad \text{in the matrix}, \tag{26}$$

where $\zeta = \xi + i\eta = (z_m + \sqrt{z_m^2 - 4n})/2$, $z_m = x + imy$.

4. Special cases

(1) Orthotropic solid with a rigid nanoelliptical inclusion:

Let $G_{\rm I} \to \infty$ in (25) and (26). The stress fields degenerate into

$$\tau_{yz} + i\tau_{xz} = \frac{2C_{44}}{1 - n/L_0^2} \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}} \quad \text{in the inclusion,}$$
 (27)

$$\frac{\tau_{yz}}{\sqrt{C_{44}C_{55}}} + i\frac{\tau_{xz}}{C_{55}} = \frac{\zeta^2 - L_0^2}{\zeta^2 - n} \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}} \quad \text{in the matrix.}$$
 (28)

(2) Orthotropic solid with a nanoelliptical hole:

Let $G_{\rm I} = 0$. Equation (26) degenerates into

$$\frac{\tau_{yz}}{\sqrt{C_{44}C_{55}}} + i\frac{\tau_{xz}}{C_{55}} = \frac{\zeta^2 - (\mu^S/L_0 - C_{44})/(\mu^S/L_0 + C_{44})L_0^2}{\zeta^2 - n} \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}}.$$
 (29)

Equation (29) agrees with the existing results [Xiao et al. 2014, Equation (23)].

(3) Nanocrack in an orthotropic solid:

Take b = 0 in (29). The crack tip stress field can be obtained as

$$\frac{\tau_{yz}}{\sqrt{C_{44}C_{55}}} + i\frac{\tau_{xz}}{C_{55}} = \frac{4\zeta^2 - (2\mu^S/a - C_{44})/(2\mu^S/a + C_{44})a^2}{4\zeta^2 - a^2} \frac{\tau_{yz}^{\infty}}{\sqrt{C_{44}C_{55}}}.$$
 (30)

The III-type stress intensity factor at tip A in Figure 1 can be defined as

$$K_{\text{III}}^{A} = \lim_{\substack{y=0\\z \to a}} \tau_{yz} \sqrt{2\pi(z-a)} = \tau_{yz}^{\infty} \sqrt{\pi a} \frac{C_{44}}{C_{44} + 2\mu^{s}/a} = K_{A}^{*} \tau_{yz}^{\infty} \sqrt{\pi a}, \tag{31}$$

where $K_A^* = K_{\text{III}}^A/(\tau_{yz}^\infty \sqrt{\pi a})$ denotes the dimensionless stress intensity factor at tip A. When ignoring the interface effect of inclusion, i.e., $\mu^s = 0$, (31) degenerates into the existing solution presented by Hwu [1991], i.e.,

$$K_{\text{III}}^A = \tau_{yz}^\infty \sqrt{\pi a}.\tag{32}$$

5. Results and discussion

The interface elastic constant can be obtained through atomistic simulations. Studies on orthotropic solids remain lacking; thus, we consider $C_{44}^S/C_{55}^S=C_{44}/C_{55}$ in this work. We assume that the ratio of the elastic constant C_{44}^S of the interface to that of the matrix along the y-axis is a real constant α , i.e., $\alpha=C_{44}^S/C_{44}$, where α varies from $-2\cdot 10^{-10}$ m to $2\cdot 10^{-10}$ m [Luo and Wang 2009]. Then, $\mu^S=C_{44}^S|\sin\theta|+C_{55}^S|\cos\theta|=C_{44}^S(|\sin\theta|+C_{55}/C_{44}|\cos\theta|)$. We then define the section aspect ratio of the elliptical inclusion as $\gamma=b/a$, $\beta=G_1/C_{44}$.

Example 1. A comparison of the present solution for $\alpha = 0$ (classical elasticity theory) with the finite element results is plotted in Figure 4, where a = 5 nm, $\gamma = b/a = 0.5$, $\beta = G_{\rm I}/C_{44} = 0$, $C_{55} = 12$ GPa, and $C_{44} = 5.7$ GPa. The finite element results agree with the present solution when $\alpha = 0$. With the increase in angle θ from 0° to 90° , the interface stress concentration factors decrease monotonously when $\alpha = 2 \cdot 10^{-10}$ m and $\alpha = 0$, whereas the interface stress concentration factors initially decrease and then increase when $\alpha = -2 \cdot 10^{-10}$ m.

Example 2. The variation in the stress concentration factors at points A and B (Figure 1) with the semimajor axis of the inclusion is plotted in Figure 5, where $\gamma = b/a = 0.2$, $\beta = G_{\rm I}/C_{44} = 2$, and $C_{55}/C_{44} = 2$. Stress τ_{yz}^A is calculated using (26) when $\rho = a$ and $\theta = 0^\circ$ (Figure 1). Then, stress τ_{yz}^A is the bulk stress, and stress concentration factor $\tau_{yz}^A/\tau_{yz}^\infty$ is dimensionless.

Figure 5 shows that stress concentration factors are dramatically dependent on size when the size of an elliptical inclusion is at the nanometer scale. The present solution approaches classical elasticity theory when the inclusion has large characteristic dimensions.

Example 3. The material moduli ratio C_{55}/C_{44} can be regarded as a parameter in studying the influence of material orthotropy on stress concentration factors. The variation in the stress concentration factors

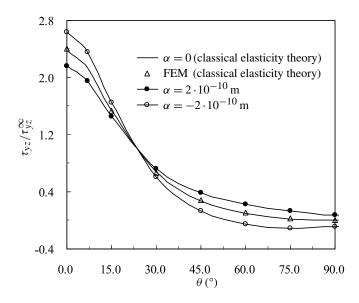


Figure 4. Distribution of the interface stress concentration factors on the interface of the elliptic hole.

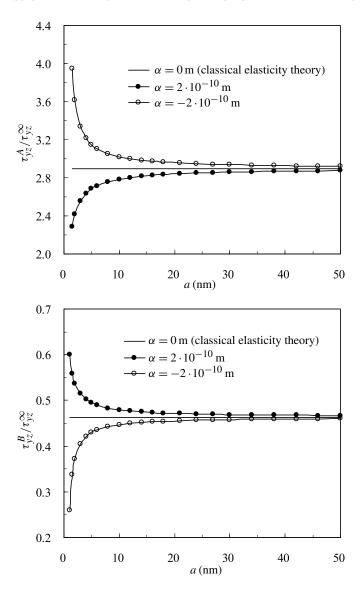


Figure 5. Variation of the stress concentration factors at points A (top) and B (bottom) with the size of the elliptic inclusion.

at points A and B with $\lg(C_{55}/C_{44})$ is plotted in Figure 6, where a=5 nm, $\gamma=b/a=0.2$, and $\beta=G_1/C_{44}=2$.

When the ratio of the elastic main direction $\lg(C_{55}/C_{44})$ increases, the increase in C_{55}/C_{44} shields the stress concentration factor at point A but amplifies said factor at point B.

Example 4. Figure 7 shows the variation in the stress concentration factors at points A and B with the inclusion section aspect ratio $\gamma = b/a$, where a = 5 nm, $\beta = G_1/C_{44} = 2$, and $C_{55}/C_{44} = 2$.

When the inclusion section aspect ratio γ increases gradually from 0 to 1, the stress concentration factor at point A decreases monotonically, whereas at point B it increases monotonically. The interface

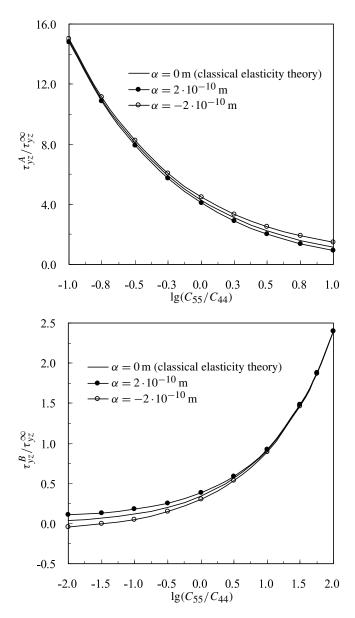


Figure 6. Variation of the stress concentration factors at points A (top) and B (bottom) with the ratio of the elastic main direction C_{55}/C_{44} .

effect of the nanoinclusion decreases with the increase in the inclusion section aspect ratio γ .

Example 5. The variation in the stress concentration factors at points A and B with the dimensionless logarithmic inclusion shear modulus $\lg(G_{\rm I}/G_{44})$ is plotted in Figure 8, where a=5 nm, $\gamma=b/a=0.2$, and $C_{55}/C_{44}=2$.

Figure 8 illustrates an interesting phenomenon in which the interface effect can be neglected when

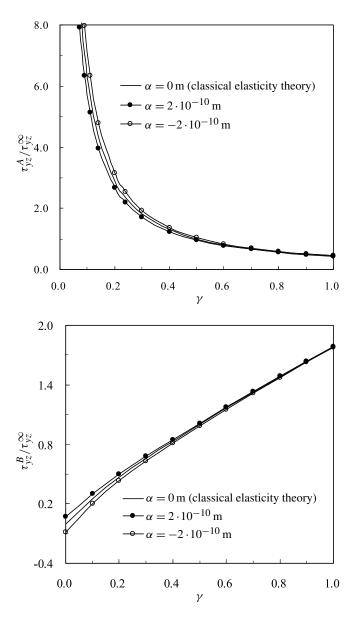
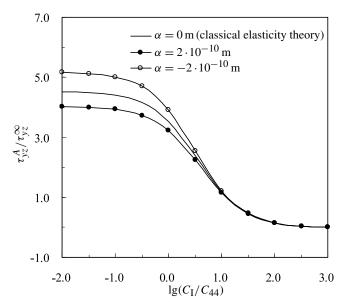


Figure 7. Variation of the stress concentration factors at points A (top) and B (bottom) with the elliptic inclusion shape ratio $\gamma = b/a$.

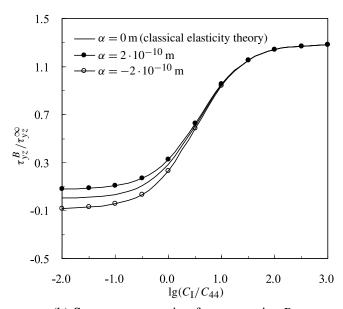
the inclusion is sufficiently hard. The influence of the interface effect depends on the modulus of the inclusion, i.e., the interface effect decreases with the increase in the modulus of the inclusion.

6. Conclusions

The problem of an orthotropic solid with a nanodefect under far-field antiplane shear loading was investigated using the Gurtin–Murdoch surface/interface model and a conformal mapping technique. An



(a) Stress concentration factor at point A.



(b) Stress concentration factor at point B.

Figure 8. Variation of the stress concentration factors at points A and B with the elliptic cavity shape ratio $\gamma = b/a$.

analytical solution for the overall stress field in the nanoinhomogeneous material was obtained. The proposed solution is generalized, such that several new and existing solutions can be regarded as special or degenerate cases. The effects of defect size, matrix material moduli ratio, defect shape ratio, and inclusion elastic property on the interface stresses were discussed.

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JUNHUA XIAO: xiaojunhua@ysu.edu.cn

Key Laboratory of Mechanical Reliability for Heavy Equipments and Large Structures of Hebei Province, Yanshan University, Qinhuangdao, 066004, China

CHUANFU SHI: 794509661@qq.com

Key Laboratory of Mechanical Reliability for Heavy Equipments and Large Structures of Hebei Province, Yanshan University, Qinhuangdao, 066004, China

YAOLING XU: xylysu@163.com

Key Laboratory of Mechanical Reliability for Heavy Equipments and Large Structures of Hebei Province, Yanshan University, Qinhuangdao, 066004, China

FUCHENG ZHANG: zfc@ysu.edu.cn

State Key Laboratory of Metastable Materials Science and Technology, Yanshan University, Qinhuangdao, 066004, China



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