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1. Introduction. We shall use notions given in [1]. Let G be a compact Lie group acting on a locally compact Hausdorff space X. We denote by F(G, X) the set of stationary points of G in X, that is, $F(G, X) = \{x \in X | Gx = x\}$. If G is a cyclic group generated by $g \in G$, F(G, X) is also written F(g, X).

Whenever $x \in X$, we call $Gx = \{gx | g \in G\}$ the orbit of x and $G_x = \{g \in G | gx = x\}$ the isotropy group at x. By a principal orbit we mean an orbit Gx such that G_x is minimal. By an exceptional orbit we mean an orbit of maximal dimension which is not a principal orbit. By a singular orbit we mean an orbit not of maximal dimension. Denote by U the union of all the principal orbits, by D the union of all the exceptional orbits and by B the union of all the singular orbits. Then U, D and B are all G-invariant and they are mutually disjoint. Moreover, $X = U \cup D \cup B$ and both B and $D \cup B$ are closed in X.

Denote by X^* the orbit space X/G and by π the natural projection of X onto X^* . Whenever $A \subset X, A^*$ denotes the image πA . If X is a connected cohomology *n*-manifold over Z [1; p. 9], where Z denotes the ring of integers, then the following results are known.

(1.1) U^* is connected [1; p. 122] so that whenever $x, y \in U, G_x$ and G_y are conjugate.

(1.2) $\dim_z B^* \leq \dim_z U^* - 1$ so that if r is the dimension of principal orbits and B_k is the union of all the k-dimensional singular orbits (k < r), then $\dim_z B_k \leq n - r + k - 1$ [1; p. 118]. Hence $\dim_z B \leq n - 2$.

Denote by E^{n+1} the euclidean (n + 1)-space, by S^n the unit *n*-sphere in E^{n+1} and by SO(3) the rotation group of E^3 . In this note G is to be SO(3) and X is to be a compact cohomology *n*-manifold over Z with $H^*(X; Z) = H^*(S^n; Z)$.

Let us first observe the following examples.

1. Let G = SO(3) act trivially on $X = S^1$. (Here we have n = 1.)

2. Let G = SO(3) act on $E^{n+1} = E^5 \times E^{n-4}$ $(n \ge 4)$ by the definition

$$g(x, y) = (gx, y)$$
,

where the action of G on E^5 is an irreducible orthogonal action. Then G acts on $X = S^n$ and in this action, the 2-dimensional orbits are all

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projective planes, F(G, X) is an (n-5)-sphere and for every $x \in U, G_x$ is a dihedral group of order 4.

3. Let $G = \mathrm{SO}(3)$ act on $E^{n+1} = E^3 \times E^3 \times E^{n-5}$ ($n \ge 5$) by the definition

$$g(x, y, z) = (gx, gy, z) ,$$

where the action on E^3 is the familiar one. Then G acts on $X = S^n$ and in this action, the 2-dimensional orbits are all 2-spheres, F(G, X) is an (n-6)-sphere and for every $x \in U$, G_x is the identity group.

In all three examples, $D = \phi$ and dim B = n - 2. The orbit space X^* is X itself in the first example and it is a closed (n-3)-cell with boundary B^* in the other two examples.

The purpose of this note is to prove that if X is a compact cohomology *n*-manifold over Z with $H^*(X; Z) = H^*(S^n; Z)$, then every action of G = SO(3) on X with $\dim_z B = n - 2$ strongly resembles one of these examples. In fact, we shall prove the following:

THEOREM. Let X be a compact cohomology n-manifold over Z with $H^*(X; Z) = H^*(S^n; Z)$ and let G = SO(3) act on X with $\dim_z B = n - 2$. Then $D = \phi$ and one of the following occurs.

1. n = 1 and G acts trivially on X.

2. $n \ge 4$ and for every $x \in U$, G_x is a dihedral group of order 4. Moreover, the 2-dimensional ordits are all projective planes and F(G, X)is a compact cohomology (n-5)-manifold over Z_2 with $H^*(F(G, X); Z_2) =$ $H^*(S^{n-5}; Z_2)$, where Z_2 denotes the prime field of characteristic 2.

3. $n \ge 5$ and for every $x \in U$, G_x is the identity group. Moreover, the 2-dimensional orbits are all 2-spheres and F(G, X) is a compact cohomology (n - 6)-manifold over Z_2 with $H^*(F(G, X); Z_2) = H^*(S^{n-6}; Z_2)$.

In the last two cases, B^* is a compact cohomology (n-4)-manifold over Z with $H^*(B^*; Z) = H^*(S^{n-4}; Z)$ and X^* is a compact Hausdorff space which is cohomologically trivial over Z and such that $X^* - B^*$ is a cohomology (n-3)-manifold over Z.

The proof of this theorem is given in the next three sections.

2. The set D. Let X be a connected cohomology n-manifold over Z and let G = SO(3) act on X with $\dim_z B = n - 2$. If G acts trivially on X, it is clear that n = 1 and that $D = \phi$. Hence we shall assume that the action of G on X is nontrivial.

Since G is a 3-dimensional simple group which has no 2-dimensional

subgroup, it follows that

(2.1) G acts effectively on X and no orbit is 1-dimensional.

(2.2) Principal orbits are 3-dimensional so that for every $x \in U \cup D$, G_x is finite.

By (2.1), principal orbits are either 2-dimensional or 3-dimensional. If principal orbits are 2-dimensional, then B = F(G, X) so that, by (1.2), $\dim_z B < n-2$, contrary to our assumption.

(2.3) Denote by B_2 the union of all the 2-dimensional orbits. Then $\dim_z B_2 = n - 2$ so that $B_2 \neq \phi$ and $n \ge 4$. Moreover, whenever Gz is a 2-dimensional orbit, G_z is either a circle group or the normalizer of a circle group and accordingly Gz is either a 2-sphere or a projective plane.

By (2.2), $n = \dim_z X \ge \dim_z U \ge 3$. We infer that $B_2 \ne \phi$ so that $n-2 = \dim_z B_2 \ge 2$. Hence $n \ge 4$.

(2.4) Let $x \in U$. Whenever $y \in D$, there is a $g \in G$ such that G_x is a normal subgroup of G_{gy} .

Let S be a connected slice at y [1; p. 105]. Then S is a connected cohomology (n-3)-manifold over Z and G_y acts on S. As seen in [7], S is also a connected cohomology (n-3)-manifold over Z_p for every prime p, where Z_p denotes the prime field of characteristic p.

Let $x' \in S \cap U$. We claim that $G_{x'}$ is a normal subgroup of G_y . Since G_y is a finite group (see (2.2)) and $G_{x'}$ is a subgroup of G_y , there exists a neighborhood N of the identity in G such that $N^{-1}G_{x'}N \cap G_y = G_{x'}$. Let V be a neighborhood of x' such that whenever $x'' \in V$, $hG_{x''}h^{-1} \subset G_{x'}$ for some $h \in N$. (For the existence of V, see [4; p. 216].) Then for every $x'' \in V \cap S$, $G_{x''} \subset N^{-1}G_{x'}N \cap G_y = G_{x'}$ so that $G_{x''} = G_{x'}$. Therefore $G_{x'}$ leaves every point of $V \cap S$ fixed. Since S is a connected cohomology (n-3)-manifold over Z_p for every prime p, it follows from Newman's theorem [6] that $G_{x'} \in S$, which is clearly a normal subgroup of G_y . By (1.1), G_x and $G_{x'}$ are conjugate so that our assertion follows.

(2.5) Let $x \in U$. Whenever Gz is 2-dimensional, there is a $g \in G$ such that $G_x \subset G_{gz}$. Hence G_x is either cyclic or dihedral and it is cyclic if there is a 2-dimensional orbit which is a 2-sphere.

For the rest of this section, we assume that

$$H_{c}^{*}(X; Z) = H^{*}(S^{n}; Z)$$
.

Under this assumption, $H^0_c(X; Z) = H^0(S^n; Z) = Z$. Hence X is compact.

(2.6) Let T be a circle group in G. Then F(T, X) is a compact cohomology (n - 4)-manifold over Z with $H^*(F(T, X); Z) = H^*(S^{n-4}; Z)$.

Since F(T, X) intersects every singular orbit at one or two points, $\dim_z F(T, X) = \dim_z B^* = n - 4$. Hence our assertion follows [1; Chapters IV and V].

(2.7) Let $g \in G$ be of order p^{α} , where p is a prime and α is a positive integer. If $g \in G_x$ for some $x \in U \cup D$, then F(g, X) is a compact cohomology (n-2)-manifold over Z_p with $H^*(F(g, X); Z_p) = H^*(S^{n-2}; Z_p)$. Hence F(g, X) intersects every principal orbit.

It is known that X is also a compact cohomology *n*-manifold over Z_p with $H^*(X; Z_p) = H^*(S^n; Z_p)$. Since G is connected, g preserves the orientation of X. It follows that for some r < n of the same parity, F(g, X) is a compact cohomology r-manifold over Z_p with $H^*(F(g, X); Z_p) = H^*(S^r; Z_p)$ [1; Chapters IV and V].

Let T be the circle group in G containing g. By (2.6), $F(g, X) \cap B = F(T, X)$ is a compact cohomology (n - 4)-manifold over Z_p . Since, by hypothesis, there exists a point of $U \cup D$ contained in F(g, X), $F(g, X) \cap B$ is properly contained in F(g, X) so that r = n - 2. Hence F(g, X) is a compact cohomology (n - 2)-manifold over Z_p with $H^*(F(g, X); Z_p) = H^*(S^{n-2}; Z_p).$

Since $\dim_z D^* < n-3$ [1; p. 121] and since F(g, X) intersects every exceptional orbit at a set of dimension ≤ 1 , it follows that $\dim_{Z_p}(F(g, X) \cap D) \leq \dim_z(F(g, X) \cap D) < n-2$. But we have $\dim_{Z_p}F(g, X) = n-2$ and $\dim_{Z_p}(F(g, X) \cap B) = n-4$. Therefore $F(g, X) \cap U \neq \phi$. Hence, by (1.1), F(g, X) intersects every principal orbit.

(2.8) Let $x \in U$ and $y \in D$. Let p be a prime and let α be a positive integer. If G_y has an element of order p^{α} , so does G_x .

Let $g \in G_y$ be of order p^{α} . By (2.7), $F(g, X) \cap Gx \neq \phi$ so that for some $h \in G$, $hx \in F(g, X)$. Hence $h^{-1}gh$ is an element of G_x of order p^{α} .

(2.9) $D = \phi$.

Suppose that $D \neq \phi$. Let $x \in U$ and $y \in D$ be such that G_x is a proper normal subgroup of G_y (see (2.4)). We first claim that G_y is dihedral.

It is well known that a finite subgroup of SO(3) is either cyclic or dihedral or tetrahedral or octahedral or icosahedral. If G_y is cyclic, so is G_x . Let the order of G_y be $p_1^{s_1} \cdots p_k^{s_k}$, where $p_1, \cdots p_k$ are distinct primes and s_1, \cdots, s_k are positive integers. Then for every $i = 1, \cdots, k$, G_y contains an element of order $p_i^{s_i}$ so that, by (2.8), G_x also contains an element of order $p_i^{s_i}$. Hence G_x is of order $\geq p_1^{s_1} \cdots p_k^{s_k}$ and consequently $G_x = G_y$, contrary to the fact that G_x is a proper subgroup of G_y . If G_y is either tetrahedral or octahedral or icosahedral, then by (2.8), G_x contains a subgroup of order 2 and a subgroup of order 3. In case G_x is octahedral, it also contains a subgroup of order 4. Hence G_x , as a normal subgroup of G_y , is equal to G_y , contrary to our hypothesis. This proves that G_y is dihedral.

Now the order of G_y is even. It follows from (2.7) that whenever $g \in G$ is of order 2, F(g, X) is a compact cohomology (n-2)-manifold over Z_2 with $H^*(F(g, X); Z_2) = H^*(S^{n-2}; Z_2)$. Let H be a dihedral subgroup of G of order 4. By Borel's theorem [1; p. 175], F(H, X) is a compact cohomology (n-3)-manifold over Z_2 with $H^*(F(H, X); Z_2) = H^*(S^{n-3}; Z_2)$. Since $\dim_{Z_2}(F(H, X) \cap (D \cup B)) \leq \dim_Z(F(H, X) \cap (D \cup B)) < n-3$, it follows that $F(H, X) \cap U$ is not null. Hence we may assume that $H \subset G_x \subset G_y$.

Let T be the circle group in G such that its normalizer contains G_y . Then $H \cap T \subset G_x \cap T \subset G_y \cap T$ so that $G_y \cap T$ is a cyclic group and $G_x \cap T$ is a proper subgroup of $G_y \cap T$ of even order. Let the order of $G_y \cap T$ be $2^{s_0}p_1^{s_1} \cdots p_k^{s_k}$, where p_1, \cdots, p_k are distinct odd primes and s_0, s_1, \cdots, s_k are positive integers. By (2.8), there are k + 1 elements g_0, g_1, \cdots, g_k of G_x of order $2^{s_0}, p_1^{s_1}, \cdots, p_k^{s_k}$ respectively. Since p_1, \cdots, p_k are odd, $g_1 \cdots, g_k$ are in $G_x \cap T$. Therefore no element of $G_x \cap T$ is of order 2^{s_0} . But this implies that $s_0 > 1$ so that $g_0 \in G_x \cap T$. Hence we have arrived at a contradiction.

3. Case that the 2-dimensional orbits are all projective planes.

Let X be a compact cohomology n-manifold over Z with $H^*(X; Z) = H^*(S^n; Z)$ and let G = SO(3) act nontrivially on X with $\dim_z B = n - 2$. Throughout this section, we assume that for some $x \in U, G_x$ is of even order.

(3.1) Let H be a dihedral subgroup of G of order 4 and let M be the normalizer of H that is the octahedral group containing H. Then F(H, X) is a compact cohomology (n - 3)-manifold over Z_2 with $H^*(F(H, X); Z_2) = H^*(S^{n-3}; Z_2)$ and K = M/H is isomorphic to the symmetric group of three elements and acts on F(H, X). Moreover, the natural map of F(H, X)/K into X^* is onto.

By (2.7), for every $g \in G$ of order 2, F(g, X) is a compact cohomology (n-2)-manifold over Z_2 with $H^*(F(g, X); Z_2) = H^*(S^{n-2}; Z_2)$. It follows from Borel's theorem [1; p. 175] that F(H, X) is a compact cohomology (n-3)-manifold over Z_2 with $H^*(F(H, X); Z_2) = H^*(S^{n-3}; Z_2)$.

Clearly K = M/H is isomorphic to the symmetric group of three elements and the action of M on F(H, X) induces an action of K on F(H, X). Moreover, there is a natural map $f: F(H, X)/K \to X^*$.

Let $z \in F(H, X) \cap B$. If Gz = z, then $F(H, X) \cap Gz = z$. If Gz is 2-dimensional, then G_z contains H so that by (2.3) it is the normalizer of a circle group. Therefore any two isomorphic dihedral subgroups of G_z are conjugate in G_z . Let g be an element of G with $gz \in F(H, X)$. It is clear that $g^{-1}Hg \subset g^{-1}G_{gz}g = G_z$ so that for some $h \in G_z$, $h^{-1}g^{-1}Hgh = H$ or $gh \in M$. Hence $gz = ghz \in Mz$. This proves that $F(H, X) \cap Gz \subset Mz$.

From these results it follows that F(H, X) intersects every singular orbit at a finite set. [This and one or two facts mentioned below can be seen by examining the standard action of SO(3) on S^2 or on P^2 (viewed as the acts of lines through the region in E^3).] Therefore, by (1.2), $\dim_z (F(H, X) \cap B) \leq \dim_z B^* < n - 3$. As a consequence of this result and that $D = \phi$ (see (2.9)), we have $F(H, X) \cap U \neq \phi$. Hence F(H, X)intersects every principal orbit and consequently it intersects every orbit. This proves that the natural map $f: F(H, X)/K \to X^*$ is onto.

(3.2) Every 2-dimensional orbit is a projective plane and intersects F(H, X) at exactly three points.

Let Gz be a 2-dimensional orbit. By (3.1), F(H, X) intersects Gz so that we may assume that $z \in F(H, X)$. Since G_z contains H, it follows from (2.3) that G_z is the normalizer of a circle group. Hence Gz is a projective plane.

In the proof of (3.1) we have shown that $F(H, X) \cap Gz \subset Mz$. But it is clear that $Mz \subset F(H, X) \cap Gz$. Hence

$$F(H, X) \cap Gz = Mz = M/(M \cap G_z)$$
.

Since M is of order 24 and $M \cap G_z$ is of order 8, it follows that $F(H, X) \cap Gz$ contains exactly three points.

(3.3) B^* is a compact cohomology (n-4)-manifold over Z with $H^*(B^*; Z) = H^*(S^{n-4}; Z)$.

Let T be a circle group in G. It is clear that $F(T, X) \subset B$. Since, by (2.1) and (3.2), every singular orbit is either a point or a projective plane, it follows that F(T, X) intersects every singular orbit at exactly one point. Therefore the natural projection π maps F(T, X) homeomorphically onto B^* and hence our assertion follows from (2.6).

(3.4) Let Y = F(H, X) - F(G, X). Then $\overline{Y} = F(H, X)$ and every point of Y has a neighborhood V in Y which is a cohomology (n-3)-manifold over Z and such that the isotropy group is constant on V - B.

Let T be a circle group whose normalizer N contains H. Then $F(H, X) \supset F(N, X) = F(T, X) \supset F(G, X)$. Since F(H, X) is a compact (n-3)-manifold over Z_2 (see (3.1)) and since F(T, X) is a compact (n-4)-manifold over Z_2 (see (2.6)), it follows that the closure of F(H, X) - F(T, X) is F(H, X). Hence $\overline{Y} = F(H, X)$.

1390

Let $x \in Y \cap U$ and let S be a slice at x. Then S is a cohomology (n-3)-manifold over Z. Moreover, $G_y = G_x$ for all $y \in S$ so that $S \subset Y$. Since both S and Y are cohomology (n-3)-manifolds over Z_2 , it follows that S is open in Y. Hence our assertion follows by taking S as V.

Let $z \in Y \cap B$ and let S be a slice at z. Then S is a cohomology (n-2)-manifold over Z and G_z is the normalizer of a circle group T acting on S. Whenever $x \in S \cap U$, $G_x \cap T$ is a finite cyclic group in T and the index of $G_x \cap T$ in G_x is 2 because G_x in a dihedral subgroup of G_z . Since the order of G_x is independent of $x \in S \cap U$, so is the order of $G_x \cap T$. Hence $G_x \cap T$ is independent of $x \in S \cap U$ so that for $x \in F(H, S) \cap U$.

$$G_x S = H(G_x \cap T)S = HS = S$$

and

$$F(G_x, S) = F(G_x/(G_x \cap T), S) = F(H/(H \cap T), S) = F(H, S)$$
.

Let Q be a neighborhood of the identity of G such that $Q^{-1}TQ \cap G_z = T$. If $gy \in F(H, X)$ with $g \in Q$ and $y \in S$, then $g^{-1}Hg \subset g^{-1}G_{gy}g = G_y \subset G_z$ so that $g^{-1}(H \cap T)g \subset Q^{-1}TQ \cap G_z = T$. Therefore $g^{-1}Tg = T$ or $g \in G_z$. Hence $gy \in G_z y \subset S$. This proves that $F(H, S) = F(H, X) \cap S = F(H, X) \cap QS$ is open in F(H, X) so that it is a cohomology (n-3)-manifold over Z_2 .

Since S is a cohomology (n-2)-manifold over Z with

$$F(H/(H \cap T), S) = F(H, S)$$
 ,

it follows that F(H, S) is also a cohomology (n-3)-manifold over Z. (If Z_2 acts on a cohomology m manifold over Z with $F(Z_2)$ being a cohomology (m-1)-manifold over Z_2 , then $F(Z_2)$ is also a cohomology (m-1)-manifold over Z.) That G_x is constant on $F(H, S) \cap U$ is a direct consequence of the fact that $F(G_x, S) = F(H, S)$ for all $x \in F(H, S) \cap U$.

(3.5) Y is a connected cohomology (n-3)-manifold over Z and the isotropy group is constant on Y - B.

By (3.4), Y is a cohomology (n-3)-manifold over Z. Let T be a circle group in G whose normalizer N contains H. Then $F(H, X) \supset F(N, X) =$ $F(T, X) \supset F(G, X)$. From (2.6) and (3.1), it is easily seen that F(H, X) -F(T, X) has exactly two components with F(T, X) as their common boundary. By (2.3), there exists a point z of F(T, X) such that Gz is a projective plane so that $z \in F(T, X) - F(G, X)$. Hence Y is connected.

Let $x \in Y \cap U$. Then $F(G_x, X) \cap Y$ is clearly closed in Y. But, by (3.4), it is also open in Y. Hence, by the connectedness of Y, $F(G_x, X) \cap Y = Y$.

(3.6) Whenever $x \in F(H, X) \cap U$, $G_x = H$. Hence for every $x \in U$, G_x is a dihedral group of order 4.

Let x be a point of $F(H, X) \cap U$. Since $H \subset G_x$, $F(H, X) \supset F(G_x, X)$. But, by (3.4) and (3.5), $F(H, X) \subset F(G_x, X)$. Hence $F(H, X) = F(G_x, X)$.

It is clear that $G' = \{g \in G | gF(H, X) = F(H, X)\}$ is a closed subgroup of G containing M. Since $F(H, X) = F(G_x, X)$, G_x is a normal subgroup of G' so that G' is contained in the normalizer of G_x . But, by (2.5), G_x is dihedral and H is the only dihedral group whose normalizer contains M. It follows that $G_x = H$. Hence, by (1.1), the isotropy group at any point of U is a dihedral group of order 4.

(3.7) Whenever $x \in F(H, X)$, $F(H, X) \cap Gx = Kx$ which contains one point or three points or six points according as Gx is 0-dimensional or 2-dimensional or 3-dimensional.

If Gx is 0-dimensional, it is clear that $F(H, X) \cap Gx = x = Kx$. If Gx is 2-dimensional, we have shown in the proof of (3.2) that $F(H, X) \cap Gx = Mx = Kx$ which contains exactly three points.

Now let Gx be 3-dimensional. If g is an element of G with $gx \in F(H, X)$, then, by (3.6), $gHg^{-1} = gG_xg^{-1} = G_{gx} = H$ so that $g \in M$. Therefore $F(H, X) \cap Gx \subset Mx$. But it is obvious that $Mx \subset F(H, X) \cap Gx$. Hence

$$F(H, X) \cap Gx = Mx = Kx$$

which clearly contains six points.

From this result, it is easily seen that the natural map $f: F(H, X)/K \to X^*$ is a homeomorphism onto.

(3.8) Whenever $a \in K$ is of order 2, we abbreviate F(a, F(H, X))by F(a). Then $F(a) \subset B$ and F(a) is a compact cohomology (n - 4)manifold over Z with $H^*(F(a); Z) = H^*(S^{n-4}; Z)$. Moreover, F(H, X) - F(a) contains exactly two components V and V' with aV = V'.

Whenever $x \in F(H, X) \cap U$, $G_x = H$ (see (3.6)) so that $x \notin F(a)$. Hence $F(a) \subset B$. Let a = a'H with a' being of order 4 and let T be the circle group containing a'. Then F(a) = F(T, X) and hence the first part follows from (2.6). Now F(H, X) is a compact cohomology (n - 3)-manifold over Z_2 with $H^*(F(H, X); Z_2) = H^*(S^{n-3}; Z_2)$ and F(a) = F(a, F(H, X)) is a compact cohomology (n - 4)-manifold over Z_2 . The second part follows.

(3.9) F(H, X) - B contains exactly six components and whenever P is a component of F(H, X) - B, KP = F(H, X) - B and the natural

projection π maps P homeomorphically onto U^* .

Let P be a component of F(H, X) - B. Since the isotropy group is constant on P (see (3.5)), the natural projection π defines a local homeomorphism $\pi': P \to U^*$. By (3.7), for every $x^* \in U^*$, $\pi'^{-1}x^*$ contains no more than six points. We infer that π' is closed so that $\pi'P$ is both open and closed in U^* . Hence, by the connectedness of U^* , $\pi'P = U^*$.

Let Q be a second component of F(H, X) - B and let $y \in Q$. Then there is a point $x \in P$ such that $\pi x = \pi y$. Therefore, by (3.7), for some $k \in K$, y = kx so that Q = kP. Hence KP = F(H, X) - B.

Let $x \in P$. By (3.8), x and ax belong to different components of $F(H, X) - F(a) \supset F(H, X) - B$. Therefore aP is a component of F(H, X) - B different from P. Similarly, bP and cP are components of F(H, X) - B different from P.

If aP, bP and cP are not distinct, say bP = cP, then $\{k \in K | kP = P\}$ is of order 3 so that P and aP = bP = cP are the only two components of F(H, X) - B. Now $F(H, Z) - B = F(H, Z) - (F(a) \cup F(b) \cup F(c))$ and F(a), F(b), F(c) are manifold over Z of dimension one less than the dimension of F(H). Hence $F(H, X) \cap B = F(a) \cap F(b) \cap F(c) = F(G, X)$. This is impossible, because the intersection of F(H, X) and a 2-dimensional orbit is contained in B but not contained in F(G, X). From this result it follows that P, aP, bP, cP are distinct components of F(H, X) - B. Hence P, aP, bP, cP, bcP, cbP are all the distinct components of F(H, X) - B.

Now it is clear that for every $x^* \in U^*$, $\pi'^{-1}x^*$ contains exactly one point. Hence π' is a homeomorphism.

(3.10) Let P be a component of F(H, X) - B. Then the map of $G/H \times P$ onto U defined by $(gH, x) \rightarrow gx$ is a homeomorphism onto. Hence U is homeomorphic to the topological product of a principal orbit and U^* .

This is an immediate consequence of (3.5) and (3.9).

(3.11) The closure of F(a) - F(G, X) is equal to F(a). Hence $\dim_{\mathbb{Z}_2} F(G, X) \leq \dim_{\mathbb{Z}} F(G, X) \leq n-5$.

Suppose that the closure of F(a) - F(G, X) is not equal to F(a). Then there is a point z of F(G, X) and a neighborhood A of z such that $A \cap F(a) = A \cap F(G, X)$. Since $A \cap F(G, X) \subset F(b)$ and since, by (3.8), both $A \cap F(G, X)$ and F(b) are cohomology (n - 4)-manifolds over Z, $A \cap F(G, X)$ is open in F(b) so that we may assume that $A \cap F(G, X) =$ $A \cap F(b)$. Similarly, we may assume that $A \cap F(G, X) = A \cap F(c)$. Hence $A \cap F(G, X) = A \cap F(H, X) \cap B$. By (3.1) and (3.8), we may also assume that KA = A and $A \cap (F(H, X) - F(a))$ contains exactly two components Q and Q'. Now both Q and Q' are contained in F(H, X) - B and aQ = bQ = Q' Therefore abQ = Q so that ab maps the component of F(H, X) - B containing Q into itself, contrary to (3.9).

Since, by (3.8), F(a) is a cohomology (n-4)-manifold over Z and since F(G, X) is nowhere dense in F(a), it follows that $\dim_{Z_2} F(G, X) \leq \dim_Z F(G, X) \leq n-5$.

(3.12) If n = 4, then F(G, X) is null.

This is a direct consequence of (3.11).

(3.13) Let T be a circle group in G, let N be the normalizer of T and let A be an orbit. If A is a projective plane, then A/T is an arc and N/T acts trivially on A/T so that F(N/T, A/T) = A/T = A/N. If A is 3-dimensional, then A/T is a 2-sphere and A/N is a closed 2-cell so that F(N/T, A/T) is a circle.

If A is a projective plane, it is clear that A/T is an arc and N/T acts trivially on A/T. Therefore A/N = A/T = F(N/T, A/T).

Now let A be 3-dimensional. By (3.6), we may let $A = G/H = \{gH | g \in G\}$. Therefore A/T is the double coset space (G/H)/T and (G/T)/H are homeomorphic. Since G/T is a 2-sphere and since every element of H preserves the orientation of G/T, it follows that (G/T)/H is a 2-sphere. Hence A/T is a 2-sphere.

As seen in [3], the double coset space (G/N)/H is a closed 2-cell. Since A/N may be regarded as the double coset space (G/H)/N which is homeomorphic to (G/N)/H, we infer that A/N is a closed 2-cell.

From these results, it follows that f(N/T, A/T) is a circle.

(3.14) X^* is cohomological trivial over Z.

Let N be the normalizer of a circle group T in G. Then N/T is a cyclic group of order 2 which acts on X/T with $(X/T)/(N/T) = X^*$. Since, by (2.6), $H^*(F(T, X); Z) = H^*(S^{n-4}; Z)$, it follows that H(X/T; Z) = $H^*(S^{n-1}; Z)$ [1; p. 65].

By (3.13), F(N|T, B|T) = B|T and for every singular orbit A, A|T is either a single point or an arc. It follows from the Vietoris map theorem that $H^*(B|T; Z) = H^*(B^*; Z) = H^*(S^{n-4}; Z)$ (see (3.3)). By (3.10) and (3.13), F(N|T, U|T) is homeomorphic to the topological product of a circle and U^* so that $H^{n-2}(F(N|T, U|T); Z) \neq 0$. Therefore $H^*(F(N|T, X|T); Z) = H^*(S^{n-2}; Z)$. Hence $H^*(X|N; Z) = 0$. By (3.13), for every orbit A, A|N is either a single point or an arc or a closed 2-cell. It follows from the Vietoris map theorem that $H^*(X^*; Z) = H^*(X|N; Z) = 0$.

$$(3.15) \qquad \qquad H^k_c(U^*;Z_2) = \begin{cases} Z_2 & for \ k=n-3 \ ; \\ 0 & otherwise \ . \end{cases}$$

This follows from (3.3), (3.14) and the cohomology sequence of (X^*, B^*) .

Since for a principal orbit A, we have

$$H^k(A;\,Z_2) = egin{cases} Z_2 & ext{for} \ \ k=0,\,3\ ; \ Z_2 \oplus Z_2 & ext{for} \ \ k=1,\,2\ ; \ 0 & ext{otherwise} \ , \end{cases}$$

our assertion follows from (3.10) and (3.15).

As a consequence of (3.16) and the cohomology sequence of (X, B), we have

(3.17)
$$H^{k}(B; Z_{2}) = \begin{cases} Z_{2} & \text{for } k = 0, \ n-4; \\ Z_{2} \bigoplus Z_{2} & \text{for } k = n-3, \ n-2; \\ 0 & \text{otherwise}. \end{cases}$$

$$(3.18) \quad Let \, T \, be \, a \, circle \, group \, in \, G \, and \, let \, n \geq 5. \quad Then \ H^k_c(F(T,\,X) - F(G,\,X); \, Z_2)) = egin{cases} \widetilde{H}^{k-1}(F(G,\,X); \, Z_2) & (the \, reduced \, group) \ for \, k = 1 \ H^{k-1}(F(G,\,X); \, Z_2) \oplus Z_2 & for \, k = n-4 \ H^{k-1}(F(G,\,X); \, Z_2) & otherwise \ . \end{cases}$$

This follows from (2.6) and the cohomology sequence of (F(T, X), F(G, X)).

This follows from the cohomology sequence of (B, F(G, X)).

(3.20) B - F(G, X) is homeomorphic to the topological product of a projective plane and F(T, X) - F(G, X). Hence

$$egin{aligned} &H^k_c(B-F(G,\,X);\,Z_2)\ &=H^k_c(F(T,\,X)-F(G,\,X);\,Z_2)\oplus H^{k-1}_c(F(T,\,X)-F(G,\,X);\,Z_2)\ &\oplus H^{k-2}_c(F(T,\,X)-F(G,\,X);\,Z_2)\ . \end{aligned}$$

The first part follows from the that F(T, X) - F(G, X) is a crosssection of the transformation group (G, B - F(G, X)) on which the isotropy group is constant. The second part follows from the first part and the fact that if A is a projective plane, then

$$H^k(A;Z_2)=egin{cases} Z_2 & ext{for} \ k=0,\ 1,\ 2;\ 0 & ext{otherwise.} \end{cases}$$

(3.21) $\dim_{\mathbb{Z}_2} F(G, X) = n - 5$. If n = 4, then B contains exactly two projective planes. If n = 5, then F(G, X) contains exactly two points. If n > 5, then $H^{n-5}(F(G, X); \mathbb{Z}_2) = \mathbb{Z}_2$ so that F(G, X) is not null.

Setting k = n - 2 in (3.20), we have, by (2.6) and (3.17),

 $Z_2 \oplus Z_2 = H_c^{n-4}(F(T, X) - F(G, X); Z_2)$.

If n = 4, then, by (3.12), $H^{\circ}(F(T, X); Z_{\varepsilon}) = Z_2 \bigoplus Z_2$ so that F(T, X) contains exactly two points. Hence B contains exactly two projective planes.

If n = 5, then $H^1_c(F(T, X) - F(G, X); Z_2) = \widetilde{H}^\circ(F(G, X); Z_2) \oplus$ $H^1(F(T, X); Z_2)$ so that $\widetilde{H}^\circ(F(G, X); Z_2) = Z_2$. Hence F(G, X) contains exactly two points.

If n > 5, it follows from (3.18) that $H^{n-5}(F(G, X); Z_2) = Z_2$. Hence F(G, X) is not null.

 $(3.22) \quad H^*(F(G, X); Z_2) = H^*(S^{n-5}; Z_2).$

For n = 4 and 5, the result has been shown in (3.12) and (3.21). For n > 5, our assertion follows from (3.18), (3.19), (3.20) and (3.21).

(3.23) F(G, X) is a compact cohomology (n-5)-manifold over Z_2 .

To prove (3.23), we have only to localize the preceding computations. Details are omitted.

REMARK. There is no difficulty to use Z in place of Z_2 in these computations. However, the computations over Z will not strengthen our final results (3.22) and (3.23).

4. Case that the 2-dimensional orbits are all 2-spheres.

Let X be a compact cohomology n-manifold over Z with $H^*(X; Z) = H^*(S^n; Z)$ and let G = SO(3) act nontrivially on X with dim_z B = n - 2.

1396

Throughout this section, we assume that for some $x \in U$, G_x is of odd order.

(4.1) Let H be a dihedral subgroup of G of order 4. Then F(H, X) is a compact cohomology (n - 6)-manifold over Z_2 with $H^*(F(H, X); Z_2) = H^*(S^{n-6}; Z_2)$. Hence $n \ge 5$.

Let $g \in G$ be of order 2 and let T be the circle group in G containing g. Since for some $x \in U$, G_x is of odd order, $F(g, X) \subset B$ so that F(g, X) = F(T, X) is a compact cohomology (n - 4)-manifold over Z_2 with $H^*(F(g, X); Z_2) = H^*(S^{n-4}; Z_2)$. By Borel's theorem [1; p. 175], F(H, X) is a compact cohomology (n - 6)-manifold over Z_2 with $H^*(F(H, X); Z_2) = H^*(S^{n-6}; Z_2)$. From this result it follows that $n - 6 \ge -1$. Hence $n \ge 5$.

(4.2) The 2-dimensional orbit are all 2-spheres.

Suppose that this assertion is false. Then there is, by (2.3), a projective plane Gz. Denote by T the identity component of G_z and by Ha dihedral subgroup of G_z of order 4. Let S be a connected slice at z. Then S is a cohomology (n-2)-manifold over Z and G_z acts on S. Moreover, $F(T, S) = F(T, X) \cap S$ is open in F(T, X) so that it is a cohomology (n-4)-manifold over Z. Hence we may let S be so chosen that F(T, S) is connected and that both S and F(T, S) are orientable.

Since T is a circle group and since $\dim_Z S - \dim_Z F(T, S) = 2$, it follows that S/T is a connected cohomology (n-3)-manifold over Z with boundary F(T, S) [1; p. 196]. Hence we have a connected cohomology (n-3)-manifold Y over Z obtained by doubling S/T on F(T, S) [1; p. 196]. Since S is orientable, so is S/T - F(T, S). It follows from the connectedness of F(T, S) that Y is orientable.

It is clear that $K = G_z/T$ is a cyclic group of order 2 which acts on S/T with KF(T, S) = F(T, S). Since F(K, F(T, S)) = F(H, S) is a cohomology (n - 6)-manifold over Z_z , we infer from the dimensional parity that K preserves the orientation of F(T, S) [1; p. 79].

The action of K on S/T defines a natural action of K on Y which also preserves the orientation of Y. Hence $\dim_{Z_2} F(K, Y) > n - 6$ so that for some $y^* = Ty \in S/T - F(T, S)$, $Ky^* = y^*$. But this implies that $G_z y = Ty$ so that y is a point of D, contrary to (2.9). Hence (4.2) is proved.

(4.3) F(G, X) is a compact cohomology (n-6)-manifold over Z_2 with $H^*(F(G, X); Z_2) = H^*(S^{n-6}; Z_2).$

By (4.2), F(G, X) = F(H, X). Hence our assertion follows from (4.1).

(4.4) Whenever $x \in U$, G_x is the identity group.

If X is strongly paracompact, the result can be found in [5]. But an unpublished result of Yang shows that it is true in general.

(4.5) B^* is a compact cohomology (n - 4)-manifold over Z with $H^*(B^*; Z) = H^*(S^{n-4}; Z)$.

Proof. Let T be a circle group in G and N its normalizer. Then F(T, X) is a compact cohomology (n - 4)-manifold over Z with $H^*(F(T, X); Z) = H^*(S^{n-4}; Z)$ and N/T is a cyclic group of order 2 acting on F(T, X) with $F(T, X)/(N/T) = B^*$. Therefore $H^*(B^*; Z)$ is finitely generated [1; p. 44]. If H is a dihedral subgroup of N of order 4, it is easily seen that F(N/T, F(T, X)) = F(H, X) so that F(N/T, F(T, X)) is a compact cohomology (n-6)-manifold over Z_2 with $H^*(F(N/T, F(T, X)); Z_2) = H^*(S^{n-6}; Z_2)$. Hence, by the dimensional parity theorem, N/T preserves the orientation of F(T, X).

By [1; pp. 63–64],

$$H^*(B^*; Z_2) = H^*(F(T, X)/(N/T); Z_2) = H^*(S^{n-4}; Z_2)$$
.

We now use the following diagram from [1; p. 45]

$$\cdots \longrightarrow H^{k}(B^{*}; Z) \xrightarrow{2} H^{k}(B^{*}; Z) \xrightarrow{q} H^{k}(B^{*}; Z_{2}) \longrightarrow \cdots$$

$$\uparrow^{\pi^{*}} \qquad \uparrow^{\mu}$$

$$H^{k}(F(T, X); Z)$$

in which the horizontal sequence is exact and the triangle is commutative. For $k \neq 0$, n - 4, we have $H^k(B^*; Z_2) = 0$ and $H^k(F(T, X); Z) = 0$; hence $H^k(B^*; Z) = 0$. For k = 0, we have $H^0(B^*; Z) = Z$, because B^* is clearly connected. For k = n - 4, $H^{n-4}(B^*; Z)$ is a finitely generated group with $H^{n-4}(B^*; Z) \otimes Z_2 = H^{n-4}(B^*; Z_2) = Z_2$. It follows from the universal coefficient theorem that there is a finite subgroup K of $H^{n-4}(B^*; Z)$ of odd order such that $H^{n-4}(B^*; Z)/K$ is Z or Z_2 . Since $K = 2K = \mu\pi^*K = 0$, $H^{n-4}(B^*; Z) = Z$ or Z_2 . But $H^{n-4}(B^*; Z) \neq Z_2$, because N/T preserves the orientation of F(T, X). Hence $H^{n-4}(B^*; Z) = Z$.

By localizing this result, we can show that B^* is a cohomology (n-4)-manifold over Z near every point of F(G, X). (This result is also shown in [2].) Since the projection of F(T, X) - F(G, X) onto $B^* - F(G, X)$ is a local homeomorphism, B^* is a cohomology (n-4)-manifold over Z near every point of $B^* - F(G, X)$. Hence B^* is a compact cohomology (n-4)-manifold over Z.

(4.6) Let T be a circle group in G and let N be the normalizer of T. Then $H^*(B|N; Z) = H^*(S^{n-4}; Z)$.

Let A be a singular orbit. If A is a single point, so is A/N. If A

is a 2-sphere, we may let A = G/T. Therefore A/N = (G/T)/N is homeomorphic to (G/N)/T which is known to be a closed 2-cell [3]. Hence A/N is a closed 2-cell.

Since, by (2.1) and (4.2), every singular orbit is either a single point or a 2-sphere, it follows from Vietoris map theorem that $H^*(B/N; Z) = H^*(B^*; Z)$. Hence our assertion follows from (4.5).

(4.7)
$$H^{k}(X/N;Z) = \begin{cases} Z & for \ k = 0 ; \\ Z_{2} & for \ k = n-1 ; \\ 0 & otherwise. \end{cases}$$

Since $H^*(F(T, X); Z) = H^*(S^{n-4}; Z)$, it follows that $H^*(X/T; Z) = H^*(S^{n-1}; Z)$. Now N/T is a cyclic group of order 2 acting on X/T with (X/T)/(N/T) = X/N.

Let A be an orbit. If A is 3-dimensional, then, by (4.4), A/T is a 2-sphere and N/T acts freely on A/T. If A is a 2-sphere, then A/Tis an arc and F(N/T, A/T) is a single point. If A is a point, then F(N/T, A/T) = A/T = A. Hence F(N/T, X/T) is homeomorphic to B^* so that, by (4.5), $H^*(F(N/T, X/T); Z_2)$.

As in the proof of (4.5), we can show that

(4.8)
$$H_c^k(U/N;Z) = \begin{cases} Z & for \ k = n - 3 \ Z_2 & for \ k = n - 1 \ 0 & otherwise. \end{cases}$$

(4.9) There is an exact sequence

$$\cdots o H^{k-3}_c(U^*;Z_2) o H^k_c(U^*;Z) o H^k_c(U/N;Z) o H^{k-2}_c(U^*;Z_2) o \cdots$$

By (4.4), G acts freely on U. Hence we have the desired exact sequence as seen in [3].

Since $\dim_z U^* = n - 3$, we have

$$H^k_c(U^*;Z) = 0 \quad {
m for} \ k > n-3$$
 .

It follows from (4.9) and (4.8) that $H_c^{n-3}(U^*; Z_2) = H_c^{n-1}(U/N; Z) = Z_2$. From (4.9), it is easily seen that $H_c^{n-3}(U^*; Z) = Z \bigoplus I$, where $I = im(H_c^{n-6}(U^*; Z_2) \rightarrow H_c^{n-3}(U^*; Z))$ so that every element of I different from 0 is of order 2. By the universal coefficient theorem,

$$egin{aligned} &Z_2 = H_c^{n-3}(U^*;Z_2) = H_c^{n-3}(U^*;Z) \otimes Z_2 \oplus \operatorname{Tor}(H^{n-2}(U^*;Z),Z_2) \ &= Z_2 \oplus I \ . \end{aligned}$$

Hence I = 0, proving that

$$H^{n-3}_c(U^*;Z)=Z.$$

If k < n-3, then by (4.8) and (4.9), $H_{\circ}^{k}(U^{*};Z) = H_{\circ}^{k-3}(U^{*};Z_{2})$. Hence for k < n-3,

$$H^k_c(U^*;Z)=0$$
 .

(4.11) X^* is cohomologically trivial over Z.

This is an easy consequence of (4.5), (4.10) and the cohomology sequence of (X^*, B^*) .

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equation 1193 Andrew Michael Bruckner and E. Ostrow, Some function classes related to the class of convex functions 1203 J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the complex domain 1217 P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility 1235 David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem 1241 Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for $y'' = f(x, y, y')$ 1251 Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K-polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous para	Tsuyoshi Andô, On fundamental properties of a Banach space with a cone	1163
(Sherman) Elwood Bohn, Equicontinuity of solutions of a quasi-linear 1193 Andrew Michael Bruckner and E. Ostrow, Some function classes related to the 1203 J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the 1203 J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the 1217 P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility 1235 David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem and generalizations of the Gerschgorin circle theorem 1241 Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for y" = f(x, y, y') Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K-polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1322 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones <t< td=""><td>Sterling K. Berberian, A note on hyponormal operators</td><td>1171</td></t<>	Sterling K. Berberian, A note on hyponormal operators	1171
equation 1193 Andrew Michael Bruckner and E. Ostrow, Some function classes related to the class of convex functions 1203 J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the complex domain 1217 P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility 1235 David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem 1241 Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for $y'' = f(x, y, y')$ 1251 Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K-polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous para	Errett Albert Bishop, Analytic functions with values in a Frechet space	1177
Andrew Michael Bruckner and E. Ostrow, Some function classes related to the class of convex functions. 1203 J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the complex domain . 1217 P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility 1235 David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem 1241 Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for y" = f(x, y, y') 1251 Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K-polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures	(Sherman) Elwood Bohn, Equicontinuity of solutions of a quasi-linear	
class of convex functions1203J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the complex domain1217P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility1235David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem1241Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for y" = f (x, y, y')1251Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary1273Ruth Goodman, K-polar polynomials1277Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness1289Robert Winship Heath, Arc-wise connectedness in semi-metric spaces1321Isdore Heller and Alan Jerome Hoffman, On unimodular matrices1321Robert G. Heyneman, Duality in general ergodic theory1328Charles Ray Hobby, Abelian subgroups of p-groups1343Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron1347Adam Koranyi, The Bergman kernel function for tubes over convex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators gener	equation	1193
J. H. Curtiss, Limits and bounds for divided differences on a Jordan curve in the complex domain 1217 P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility 1235 David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem 1241 Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for y" = f(x, y, y') 1251 Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K-polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Peai Mundscher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces of rings of solutions of linear differential equatio	Andrew Michael Bruckner and E. Ostrow, Some function classes related to the	
complex domain1217P. H. Doyle, III and John Gilbert Hocking, Dimensional invertibility1235David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem1241Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for y" = f(x, y, y')1251Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary1273Ruth Goodman, K-polar polynomials1277Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness1289Robert Winship Heath, Arc-wise connectedness in semi-metric spaces1301Isidore Heller and Alan Jerome Hoffman, On unimodular matrices1321Robert G. Heyneman, Duality in general ergodic theory1329Charles Ray Hobby, Abelian subgroups of p-groups1343Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron1347Adam Koranyi, The Bergman kernel function for tubes over convex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differ	5 5	1203
David G. Feingold and Richard Steven Varga, Block diagonally dominant matrices and generalizations of the Gerschgorin circle theorem		1217
and generalizations of the Gerschgorin circle theorem 1241 Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for y" = f(x, y, y') 1251 Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K-polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over corvex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W	P. H. Doyle, III and John Gilbert Hocking, <i>Dimensional invertibility</i>	1235
Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the boundary value problem for $y'' = f(x, y, y')$ 1251Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary1273Ruth Goodman, K-polar polynomials1277Israel Halperin and Maria Wonenburger, On the additivity of lattice completeness1289Robert Winship Heath, Arc-wise connectedness in semi-metric spaces1301Isidore Heller and Alan Jerome Hoffman, On unimodular matrices1321Robert G. Heyneman, Duality in general ergodic theory1329Charles Ray Hobby, Abelian subgroups of p-groups1343Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron1347Adam Koranyi, The Bergman kernel function for tubes over corvex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Ledward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov bound	David G. Feingold and Richard Steven Varga, <i>Block diagonally dominant matrices</i>	
boundary value problem for $y'' = f(x, y, y')$ 1251Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary1273Ruth Goodman, K-polar polynomials1277Israel Halperin and Maria Wonenburger, On the additivity of lattice1289completeness1289Robert Winship Heath, Arc-wise connectedness in semi-metric spaces1301Isidore Heller and Alan Jerome Hoffman, On unimodular matrices1321Robert G. Heyneman, Duality in general ergodic theory1329Charles Ray Hobby, Abelian subgroups of p-groups1343Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron1347Adam Koranyi, The Bergman kernel function for tubes over convex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435	and generalizations of the Gerschgorin circle theorem	1241
Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary 1273 Ruth Goodman, K -polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1322 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an appl	Leonard Dubois Fountain and Lloyd Kenneth Jackson, A generalized solution of the	
Ruth Goodman, K -polar polynomials 1277 Israel Halperin and Maria Wonenburger, On the additivity of lattice 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of	boundary value problem for $y'' = f(x, y, y')$	1251
Israel Halperin and Maria Wonenburger, On the additivity of lattice 1289 Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435 <td>Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary</td> <td>1273</td>	Robert William Gilmer, Jr., Rings in which semi-primary ideals are primary	1273
completeness1289Robert Winship Heath, Arc-wise connectedness in semi-metric spaces1301Isidore Heller and Alan Jerome Hoffman, On unimodular matrices1321Robert G. Heyneman, Duality in general ergodic theory1329Charles Ray Hobby, Abelian subgroups of p-groups1343Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron1347Adam Koranyi, The Bergman kernel function for tubes over convex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions of two complex variables in domains with the Bergman-Shilov boundary1435	Ruth Goodman, <i>K</i> -polar polynomials	1277
Robert Winship Heath, Arc-wise connectedness in semi-metric spaces 1301 Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions of two complex variables in domains with the Bergman-Shilov boundary 1423	Israel Halperin and Maria Wonenburger, On the additivity of lattice	
Isidore Heller and Alan Jerome Hoffman, On unimodular matrices 1321 Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		
Robert G. Heyneman, Duality in general ergodic theory 1329 Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435	Robert Winship Heath, Arc-wise connectedness in semi-metric spaces	1301
Charles Ray Hobby, Abelian subgroups of p-groups 1343 Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435	Isidore Heller and Alan Jerome Hoffman, On unimodular matrices	1321
Kenneth Myron Hoffman and Hugo Rossi, The minimum boundary for an analytic polyhedron 1347 Adam Koranyi, The Bergman kernel function for tubes over convex cones 1355 Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435	Robert G. Heyneman, <i>Duality in general ergodic theory</i>	1329
polyhedron1347Adam Koranyi, The Bergman kernel function for tubes over convex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435	Charles Ray Hobby, Abelian subgroups of p-groups	1343
Adam Koranyi, The Bergman kernel function for tubes over convex cones1355Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435	Kenneth Myron Hoffman and Hugo Rossi, <i>The minimum boundary for an analytic polyhedron</i>	1347
Pesi Rustom Masani and Jack Max Robertson, The time-domain analysis of a continuous parameter weakly stationary stochastic process 1361 William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		
continuous parameter weakly stationary stochastic process1361William Schumacher Massey, Non-existence of almost-complex structures on quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435		
William Schumacher Massey, Non-existence of almost-complex structures on 1379 Waternionic projective spaces 1379 Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		1361
quaternionic projective spaces1379Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3)1385Ronald John Nunke, A note on Abelian group extensions1401Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435		
Deane Montgomery and Chung-Tao Yang, A theorem on the action of SO(3) 1385 Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		1379
Ronald John Nunke, A note on Abelian group extensions 1401 Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		1385
Carl Mark Pearcy, A complete set of unitary invariants for operators generating finite W*-algebras of type I 1405 Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		1401
finite W*-algebras of type I1405Edward C. Posner, Integral closure of rings of solutions of linear differential equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435		
Edward C. Posner, Integral closure of rings of solutions of linear differential equations 1417 Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions 1423 J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary 1435		1405
equations1417Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions1423J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary1435		
application to Bessel functions		1417
J. Śladkowska, Bounds of analytic functions of two complex variables in domains with the Bergman-Shilov boundary	Duane Sather, Asymptotics. III. Stationary phase for two parameters with an application to Bessel functions	1423
with the Bergman-Shilov boundary 1435		1120
		1435
	Joseph Gail Stampfli, <i>Hyponormal operators</i>	
	George Gustave Weill, Some extremal properties of linear combinations of kernels	1.55
on Riemann surfaces		1459
Edward Takashi Kobayashi, Errata: "A remark on the Nijenhuis tensor"		1467