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THE SPLITTING OF OPERATOR ALGEBRAS. II

STEVE WRIGHT

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Let $\{A_{\alpha}: \alpha \in A\}$ be a family of C^* -algebras (resp., W^* algebras). For $\alpha_0 \in A$, we let $P_{\alpha_0}: \bigoplus_{\alpha} A_{\alpha} \to A_{\alpha_0}$ denote the canonical coordinate projection of $\bigoplus_{\alpha} A_{\alpha}$ onto A_{α_0} . If *B* is a C^* -(resp., W^* -) subalgebra of $\bigoplus_{\alpha} A_{\alpha}$, we say that *B* splits if $B = \bigoplus_{\alpha} P_{\alpha}(B)$. In this note, we give conditions both necessary and sufficient for *B* to split. In the *C**-category, these conditions are given in terms of separation properties of the spectrum and primitive ideal space of *B*, and in the W^* -category, the conditions are expressed in terms of disjointness of certain subsets of the center of *B*. We also give examples to show that these conditions cannot be weakened, and are hence the best possible of their kind.

In [4], Sze-kai Tsui and the author obtained several results on the splitting of singly-generated operator algebras. Theorems 2.1 and 3.4 of [4] are the principle results of that paper, and it is the purpose of this paper to present results which both improve and generalize the main results of [4].

If A is a C^{*}-algebra (resp., W^{*}-algebra) and $a \in A$, then C^{*}(a) (resp., W^{*}(a)) denotes the C^{*}-subalgebra (resp., W^{*}-subalgebra) of A generated by a. Let π be a representation of A_{α_0} , for some fixed $\alpha_0 \in A$. We define a representation $\tilde{\pi}$ of $\bigoplus_{\alpha} A_{\alpha}$ by

$$\widetilde{\pi} \colon \bigoplus_{\alpha} a_{\alpha} \longrightarrow \pi(a_{\alpha_0}) , \qquad \bigoplus_{\alpha} a_{\alpha} \in \bigoplus_{\alpha} A_{\alpha} .$$

The sets

 $\sum_{a_0} = \{ \ker (\tilde{\rho}|_{\mathcal{C}^{\star}(\bigoplus_{\alpha} a_{\alpha})}): \rho \text{ an irreducible representation of } C^{*}(a_{\alpha_0}) \}$

are subsets of the primitive ideal space of $C^*(\bigoplus_{\alpha} a_{\alpha})$. The first main result of [4] asserted that $C^*(a_1 \bigoplus a_2)$ splits if and only if \sum_i and \sum_i disconnect the pimitive ideal space of $C^*(a_1 \bigoplus a_2)$ equipped with the hull-kernel topology. In Theorem 2.2 of this paper, we improve and generalize this to arbitrary C^* -subalgebras of arbitrary direct sums of C^* -algebras.

Let N be W^* -algebra with predual N_* and let τ be a $\sigma(N, N_*)$ continuous representation of N. We set $\operatorname{supp} \tau = \operatorname{complement}$ of the central support projection of ker τ in N. We denote the class of all nonzero $\sigma(N, N_*)$ -continuous representations of N by $\operatorname{Rep}_{\sigma}(N)$. If S and T are subsets of N, we say that S and T are orthogonal if st = ts = 0, for $s \in S$ and $t \in T$.

Let $N_{\alpha}: \alpha \in \mathscr{A}$ be a family of W^* -algebras, with $\bigoplus_{\alpha} n_{\alpha}$ a fixed

element of $\bigoplus_{\alpha} N_{\alpha}$. We set

$$\mathbf{S}_{\alpha_0} = \{ \mathrm{supp} \ (\widetilde{\tau} \mid_{W^*(\boldsymbol{\oplus}_{\alpha^n \alpha^{\prime}})}) \colon \tau \in \mathrm{Rep}_{\sigma} \ (W^*(n_{\alpha_0})) \} \ .$$

The second main theorem of [4] asserted that $W^*(n_1 \bigoplus n_2)$ splits if and only if S_1 and S_2 are orthogonal and $\sup(S_1 \cup S_2) = \text{identity in}$ $W^*(n_1) \bigoplus W^*(n_2)$. In Theorem 2.4 of this paper we improve and generalize this to arbitrary W^* -subalgebras of arbitrary direct sums of W^* -algebras.

2. Solution of the splitting problem. Let $\{A_{\alpha}: \alpha \in \mathfrak{A}\}$ be a family of C*-algebras, and let $P_{\alpha}: \bigoplus_{\alpha} A_{\alpha} \to A_{\alpha}$ denote the canonical coordinate projection of $\bigoplus_{\alpha} A_{\alpha}$ onto A_{α} . A C*-subalgebra B of $\bigoplus_{\alpha} A_{\alpha}$ is said to be substantial in $\bigoplus_{\alpha} A_{\alpha}$ if $P_{\alpha}(B) = A_{\alpha}$, for each $\alpha \in \mathfrak{A}$. A C*-subalgebra B of $\bigoplus_{\alpha} A_{\alpha}$ is said to split if $B = \bigoplus_{\alpha} P_{\alpha}(B)$. The question that concerns us asks: when does a C*-subalgebra of $\bigoplus_{\alpha} A_{\alpha}$ split?

The following lemma, the key to our answer to this question, is a trivial modification of a result kindly suggested to us by Don Hadwin, who in turn heard it from T. B. Hoover:

LEMMA 2.1. Let $\{A_1, \dots, A_n\}$ be C*-algebras, with B a substantial C*-subalgebra of $A_1 \oplus \dots \oplus A_n$. Then $B = A_1 \oplus \dots \oplus A_n$ if and only if the following condition holds: there exist no distinct indices i and j and irreducible representations ρ_{α} of A_{α} , $\alpha = i$, j, for which $\tilde{\rho}_i|_B = \tilde{\rho}_j|_B$.

Proof. (\Rightarrow) . This is clear.

(\Leftarrow). Fix $i \neq j$. It sufficies to show that $(P_i \bigoplus P_i)(B) =$ $A_i \oplus A_i$, and hence we may assume with no loss of generality that n=2. Set $J_i=B\cap \ker (P_i)$, i=1, 2. Then J_1+J_2 is a closed, two-sided ideal in B. Let $a_1 \in A_1$. Since $P_1(B) = A_1$, there exists $a' \in A_2$ such that $a_1 \oplus a' \in B$. Define the *-homomorphism $\sigma_1: A_1 \rightarrow$ $B/(J_1+J_2)$ by $\sigma_1\colon a_1 o a_1\oplus a'+(J_1+J_2).$ Let $a_2\in A_2.$ Since $P_2(B) = A_2$, there exists $a'' \in A_1$ such that $a'' \bigoplus a_2 \in B$. Define the *-homomorphism $\sigma_2: A_2 \to B/(J_1 + J_2)$ by $\sigma_2: a_2 \to a'' \bigoplus a_2 + (J_1 + J_2)$. One easily checks that $\tilde{\sigma}_1|_B = \tilde{\sigma}_2|_B$. Suppose $\tilde{\sigma}_1(B) \neq (0)$. Let ρ be an irreducible representation of $\tilde{\sigma}_1(B)$. Since $\sigma_1(A_1) = \tilde{\sigma}_1(B) = \tilde{\sigma}_2(B) =$ $\sigma_2(A_2), \rho_i = \rho \circ \sigma_i$ is an irreducible representation of $A_i, i = 1, 2,$ and we thus have $\widetilde{
ho}_{_1}|_{_B} = \widetilde{
ho}_{_2}|_{_B}$, contrary to assumption. Thus $\widetilde{\sigma}_{_1}(B) =$ $\widetilde{\sigma}_{_2}(B)=(0),$ whence $\sigma_{_1}=\sigma_{_2}=0.$ It follows that $J_{_1}=(0)\oplus A_{_2},$ $J_2 = A_1 \bigoplus (0)$, whence $B = A_1 \bigoplus A_2$.

We now introduce some notation and terminology for the state-

ment and proof of our principle result.

Let A be a C^{*}-algebra. We let A^{**} denote the enveloping W^{*}algebra of A, realized as the ultraweak closure of the image of A under its universal representation. If S is a subset of A^{**} , we will denote the ultraweak closure of S by S⁻. If I is a closed, twosided ideal in A then I^- is an ultraweakly closed, two-sided ideal in A^{**} , so there is a central projection p of A^{**} such that $I^- = A^{**}p$. We set s(I) = p.

If p is a central projection of A^{**} , the representation of A defined by $a \to ap$, $a \in A$, will be denoted by π_p .

If B is a C^{*}-subalgebra of A, we will write $B/B \cap I = A/I$ to indicate that the canonical injection of $B/B \cap I$ into A/I is surjective.

The class of all irreducible representations of A will be denoted by Irr (A), and we identify Irr (A/I) with $\{\rho \in \text{Irr } (A): I \subseteq \text{ker } (\rho)\}$.

We recall that two representations of A are *disjoint* if they have no nonzero, unitarily equivalent subrepresentations.

Finally, we need to consider the *restricted* direct sum $\widehat{\bigoplus}_{\alpha} A_{\alpha}$ of a family $A_{\alpha}: \alpha \in \mathfrak{A}$ of C^* -algebras. By definition, $\widehat{\bigoplus}_{\alpha} A_{\alpha}$ is the closed, two-sided ideal of $\bigoplus_{\alpha} A_{\alpha}$ consisting of all elements $\bigoplus_{\alpha} a_{\alpha}$ for which the sets $\{\alpha \in \mathfrak{A}: || a_{\alpha} || \geq \varepsilon\}$ are finite for each $\varepsilon > 0$.

We can now present our solution of the splitting problem for arbitrary families of C^* -algebras:

THEOREM 2.2. Let A_{α} : $\alpha \in \mathfrak{A}$ be a family of C^* -algebras, B a C^* -subalgebra of $\bigoplus_{\alpha} A_{\alpha}$. Let $A = \bigoplus_{\alpha} P_{\alpha}(B)$, $I = \bigoplus_{\alpha} P_{\alpha}(B)$. The following are equivalent:

- (i) B splits;
- (ii) $B/B \cap I = A/I$, and the sets

 $\{\ker\,(\rho|_{\scriptscriptstyle B})\colon\rho\in\operatorname{Irr}\,(A/I)\}\;,\qquad \{\ker\,(\widetilde{\rho}|_{\scriptscriptstyle B})\colon\rho\in\operatorname{Irr}\,(P_{\scriptscriptstyle \alpha}(B))\}\;,\qquad \alpha\in\mathfrak{A}\;,$

are pairwise disjoint subsets of the primitive ideal space of B;

(iii) $B/B \cap I = A/I$, and the following condition holds: for each fixed $\alpha \in \mathfrak{A}$ and $(\alpha_1, \alpha_2) \in \mathfrak{A} \times \mathfrak{A}$ with $\alpha_1 \neq \alpha_2$, and for each ordered pair (ρ_1, ρ_2) in Irr $(P_{\alpha_1}(B)) \times \operatorname{Irr} (P_{\alpha_2}(B))$ (resp., Irr $(A/I) \times \operatorname{Irr} (P_{\alpha}(B))$), we have $\tilde{\rho}_1|_B \neq \tilde{\rho}_2|_B$ (resp., $\rho_1|_B \neq \tilde{\rho}_2|_B$).

Proof. The implications $(i) \Rightarrow (ii)$ and $(ii) \Rightarrow (iii)$ are clear.

(iii) \Rightarrow (i). We may assume with no loss of generality that B is substantial in $A = \bigoplus_{\alpha} A_{\alpha}$. Let p = s(I), so that $I^- = A^{**}p$. The map $a + I \rightarrow a(1 - p)$ of A/I into $A^{**}(1 - p)$ extends to an isomorphism of $(A/I)^{**}$ onto $A^{**}(1 - p)$. Since $B/B \cap I = A/I$, we conclude that $B^-(1 - p) = A^{**}(1 - p)$.

Let Σ denote the set of all finite subsets of the indexing set

 $\mathfrak{A}_{\sigma} = \bigoplus \{A_{\alpha} : \alpha \in \sigma\}, P_{\sigma} = \bigoplus \{P_{\alpha} : \alpha \in \sigma\}, and B_{\sigma} = \bigoplus \{A_{\alpha} : \alpha \in \sigma\}, P_{\sigma} = \bigoplus \{P_{\alpha} : \alpha \in \sigma\}, and B_{\sigma} = P_{\sigma}(B).$ It follows from the hypothesis that B_{σ} is a substantial C*-subalgebra of A_{σ} which satisfies the conditions of Lemma 2.1, so by that lemma, $B_{\sigma} = A_{\sigma}$. Thus $P_{\sigma}|_{B}$ implements a *-isomorphism of $B/\ker(P_{\sigma}|_{B})$ onto A_{σ} , and since this isomorphism is an isometry, it follows that B has the following property:

$$(*) \qquad \text{for each } a = \bigoplus_{\alpha} a_{\alpha} \in \bigoplus_{\alpha} A_{\alpha} \text{ and } \sigma \in \Sigma, \text{ there exists} \\ b_{\sigma} = \bigoplus_{\alpha} b_{\alpha}^{\sigma} \in B \text{ such that } \|b_{\sigma}\| \leq 1 + \|a\| \text{ and} \\ b_{\alpha}^{\sigma} = a_{\alpha}, \text{ for each } \alpha \in \sigma.$$

Set P_{α} = support projection of A_{α}^{**} in A^{**} . Then $\{p_{\alpha}: \alpha \in \mathfrak{A}\}$ is a family of pairwise orthogonal projections of I^{-} such that $\bigoplus_{\alpha} p_{\alpha} = p$. Letting $p_{\sigma} = \bigoplus\{p_{\alpha}: \alpha \in \sigma\}$ for each $\sigma \in \Sigma$, and considering Σ as a net, ordered by inclusion, we have $\lim_{\alpha} ||x - xp_{\alpha}|| = 0$, for each $x \in I$.

Fix $x \in I$. By (*), for each $\sigma \in \Sigma$ there exists $b_{\sigma} \in B$ such that $xp_{\sigma} = b_{\sigma}p_{\sigma}$ and $||b_{\sigma}|| \leq 1 + ||x||$. Since $\{b \in B^{-}: ||b|| \leq 1 + ||x||\}$ is ultraweakly compact, $\{b_{\sigma}\}$ has an ultraweak accumulation point $b \in B^{-}$. Passing if necessary to a cofinal subnet, we may assume that ultraweak-lim_{σ} $b_{\sigma} = b$, and we hence have

$$x = \lim_{\sigma} x p_{\sigma} = \lim_{\sigma} b_{\sigma} p_{\sigma} = ext{ultraweak-lim}_{\sigma} b_{\sigma} p_{\sigma} = b p \; .$$

Thus $I \subseteq B^-p$, whence $A^{**}p = I^- = B^-p$.

We assert that $\pi_p|_B$ and $\pi_{1-p}|_B$ are disjoint. If they are not, we can find irreducible representations ρ_1 and ρ_2 of A with $I \not\subseteq \ker(\rho_1)$, $I \subseteq \ker(\rho_2)$, such that $\rho_1|_B = \rho_2|_B$. Since $\rho_1 = \tilde{\rho}$ for $\rho \in \operatorname{Irr}(A_{\alpha})$ for some $\alpha \in \mathfrak{A}$, this contradicts (iii).

Let q = support projection of B^- in A^{**} . Since $A^{**} = B^- p \bigoplus B^-(1-p)$, q = 1, and so $1 \in B^-$. Thus by the disjointness of $\pi_p|_B$ and $\pi_{1-p}|_B$ and Proposition 5.2.1 of [1], we have (with ' denoting the commutant):

$$\begin{split} B^- &= (\pi_p \oplus \pi_{1-p})(B)'' = (Bp)'' \oplus (B(1-p))'' \\ &= B^- p \oplus B^-(1-p) \\ &= A^{**} \ . \end{split}$$

If $\iota: B \to A$ denotes the inclusion map, then B^- can be identified with $\iota^{**}(B^{**})$ in A^{**} . We have hence shown that ι^{**} is a surjection of B^{**} onto A^{**} . By duality and the Hahn-Banach theorem, we therefore conclude that B = A.

If instead of the full direct sum $\bigoplus_{\alpha} A_{\alpha}$, we consider C^* -subalgebras of restricted direct sums $\widehat{\bigoplus}_{\alpha} A_{\alpha}$, then $I^{**} = A^{**}$ in the above proof, and so we immediately deduce: COROLLARY 2.3. Let A_{α} : $\alpha \in \mathfrak{A}$ be a family of C^{*}-algebras, B a C^{*}-subalgebra of $\widehat{\bigoplus}_{\alpha} A_{\alpha}$. The following are equivalent:

(i) B splits;

(ii) The sets {ker $(\tilde{\rho}|_B)$: $\rho \in Irr(P_{\alpha}(B))$ }, $\alpha \in \mathfrak{A}$, are pairwise disjoint subsets of the primitive ideal space of B;

(iii) For each $(\alpha_1, \alpha_2) \in \mathfrak{A} \times \mathfrak{A}$ with $\alpha_1 \neq \alpha_2$ and for each $(\rho_1, \rho_2) \in \operatorname{Irr}(P_{\alpha_1}(B)) \times \operatorname{Irr}(P_{\alpha_2}(B))$, we have $\tilde{\rho}_1|_B \neq \tilde{\rho}_2|_B$.

The reasoning of Theorem 2.2 can be applied to easily obtain a solution to the splitting problem for an arbitrary direct sum of W^* -algebras. Indeed, recalling the notation of the introduction, we have:

THEOREM 2.4. Let $N_{\alpha}: \alpha \in \mathfrak{A}$ be a family of W^* -algebras, M a W^* -subalgebra of $\bigoplus_{\alpha} N_{\alpha}$. The following are equivalent:

(i) M splits;

(ii) The subsets {supp $(\tilde{\tau}|_{M})$: $\tau \in \operatorname{Rep}_{\sigma}(P_{\alpha}(M))$ }, $\alpha \in \mathfrak{A}$, of the center of M are pairwise disjoint;

(iii) For each $(\alpha_1, \alpha_2) \in \mathfrak{A} \times \mathfrak{A}$ with $\alpha_1 \neq \alpha_2$ and for each $(\tau_1, \tau_2) \in \operatorname{Rep}_{\sigma}(P_{\alpha_1}(M)) \times \operatorname{Rep}_{\sigma}(P_{\alpha_2}(M))$, we have $\tilde{\tau}_1|_M \neq \tilde{\tau}_2|_M$.

Proof. The implications $(i) \Rightarrow (ii)$ and $(ii) \Rightarrow (iii)$ are clear.

(iii) \Rightarrow (i). Lemma 2.1 holds with C^* -(sub)algebra (resp., irreducible representation) replaced by W^* -(sub)algebra (resp., nonzero, $\sigma(A_{\alpha}, (A_{\alpha})_*)$ -continuous representation). Thus the argument of the first part of the implication (iii) \Rightarrow (i) of Theorem 2.2, appropriately modified, together with the fact that the net $\{p_{\sigma}: \sigma \in \Sigma\}$ (where $p_{\alpha} =$ identity of N_{α}) converges in the *-strong topology to the identity of $\bigoplus_{\alpha} N_{\alpha}$ now finishes the proof.

REMARKS. (1) The splitting phenomenon is much more likely to occur in the W*-category than in the C*-category, to which Theorems 2.2 and 2.4 attest. In fact, an example of two diagonal operators T_1 and T_2 acting on a separable Hilbert space is given in [4] for which $W^*(T_1 \oplus T_2)$ splits, while neither $W^*(\operatorname{Re} T_1 \oplus \operatorname{Re} T_2)$, $W^*(\operatorname{Im} T_1 \oplus \operatorname{Im} T_2)$, nor $C^*(T_1 \oplus T_2)$ splits.

(2) Theorems 1.4 and 2.2 of [3] can be combined with Lemma 2.1 to give an alternate proof of Theorem 2.2. The proof given here seems more natural in the present context, quickly gives a solution to the splitting problem for W^* -algebras, and avoids the fairly complicated machinery of algebras of operator fields and regularized dual spaces used in [3].

(3) In closing, we present some simple examples which show

that the conditions of Theorem 2.2 cannot be weakened. More specifically, we give examples of a proper, substantial C^* -subalgebra B of l_{∞} for which $B/B \cap c_0 = l_{\infty}/c_0$ and for which

$$(^{**})$$
 $(P_1 \oplus \cdots \oplus P_n)$ $(B) = C^n$, for each positive integer n ,

and a proper, substantial C^* -subalgebra C of l_{∞} which satisfies the second part of condition (ii) of Theorem 2.2 and for which $C/C \cap c_0$ has codimension 1 in l_{∞}/c_0 .

We identify l_{∞} with the C*-algebra C(X) of continuous, complexvalued functions on the Stone-Čech compactification X of the positive integers Z_+ with discrete topology. Z_+ is a discrete, dense, open subset of X. Set $E = X \setminus Z_+$. Then c_0 can be identified with the ideal of functions in C(X) which vanish on E.

Choose $x \in Z_+$, $y \in E$, and set $B = \{f \in C(X): f(x) = f(y)\}$. B is a proper C*-subalgebra of C(X). Let $\{x_1, \dots, x_n\}$ be a fixed finite subset of Z_+ , (a_1, \dots, a_n) a fixed n-tuple of complex numbers. Then by the Tietze extension theorem ([2], Theorem 5.1, p. 149), we can find an $f \in C(X)$ such that $f(x_i) = a_i$, $i = 1, \dots, n$, and f(x) = f(y). Thus B is substantial in C(X) and satisfies (**). Let g be a fixed element of C(X). Again by the Tietze extension theorem, there exists $f \in C(X)$ such that f = g on E and f(x) = g(y). Thus $f \in B$, and since f - g = 0 on E, $f - g \in c_0$. Hence $B/B \cap c_0 = l_{\infty}/c_0$.

To obtain C, simply choose distinct elements x and y of E and set $C = \{f \in C(X): f(x) = f(y)\}$. Since elements of $\operatorname{Irr}(l_{\infty})$ of the form $\tilde{\rho}, \rho$ an irreducible representation of some coordinate algebra, correspond to evaluation at points of Z_+ and elements of $\operatorname{Irr}(l_{\infty}/c_0)$ correspond to evaluation at points of E, the previous reasoning shows that C satisfies the second part of condition (ii) of Theorem 2.2. Now l_{∞}/c_0 can be identified with the C^* -algebra C(E) of continuous, complex-valued functions on E, and $C/C \cap c_0$ can be identified with the subalgebra D of all $f \in C(E)$ for which f(x) = f(y). Since D is the kernel of the linear functional $f \to f(x) - f(y)$ on C(E), it follows that $C/C \cap c_0$ has codimension 1 in l_{∞}/c_0 .

These arguments can clearly be used to construct similar examples for an arbitrary infinite direct sum of commutative C^* -algebras.

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