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ON THE ORDERS OF AUTOMORPHISMS OF A CLOSED RIEMANN SURFACE

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Let S be a closed Riemann surface of genus $g (\ge 2)$. It is known that the maximum value of the orders of automorphisms of S is 4g + 2. In this paper we determine the orders of automorphisms of S which are greater than or equal to 3g, and characterize those Riemann surfaces having the corresponding automorphisms. Except for several cases, such Riemann surfaces are determined uniquely up to conformal equivalence.

THEOREM 1. Let N(S, h) be the order of an automorphism h of S. Then, max_{S,h} N(S, h) = 4g + 2. The Riemann surface having the automorphism of maximum order 4g + 2 is conformally equivalent to the Riemann surface defined by

$$y^2 = x(x^{2g+1} - 1).$$

The automorphism h of order 4g + 2 is given by

 $h(x, y) = \left(e^{2\pi i/(2g+1)}x, e^{2\pi i/(4g+2)}y\right).$

Although the existence of the Riemann surface with the automorphism of order 4g + 2 is well known, in the above theorem the uniqueness (up to conformal equivalence) is shown.

To simplify, we write Theorem 1 in the following form:

$$\max N = 4g + 2, \qquad S: y^2 = x(x^{2g+1} - 1),$$
$$h(x, y) = (e^{2\pi i/(2g+1)}x, e^{2\pi i/(4g+2)}y).$$

Under similar notation,

THEOREM 2.

 $\max_{N < 4g+2} N = 4g, \quad S: y^2 = x(x^{2g} - 1), \quad h(x, y) = (e^{2\pi i/2g}x, e^{2\pi i/4g}y).$

THEOREM 3. If
$$g \equiv 0 \pmod{3}$$
, for $g \neq 3$,

$$\max_{N < 4g} N = 3g + 3, \qquad S: y^3 = x^2 (x^{g+1} - 1),$$

$$h(x, y) = (e^{2\pi i / (g+1)}x, e^{4\pi i / (3g+3)}y).$$

For g = 3, we have 4g = 3g + 3. Then there exist two Riemann surfaces defined by

$$y^2 = x(x^6 - 1)$$
 and $y^3 = x^2(x^4 - 1)$

which have an automorphism of order 12. Furthermore,

 $\max_{N < 3g+3} N = 3g, \quad S: y^3 = x(x^g - 1), \quad h(x, y) = (e^{2\pi i/g}x, e^{2\pi i/3g}y),$

except for

$$S: y^{20} = x^5(x-1)^4 \quad (g = 6, N = 20 = 3g + 2),$$

$$: y^{28} = x^7(x-1)^4 \quad (g = 9, N = 28 = 3g + 1),$$

$$: y^{36} = x^9(x-1)^4 \quad (g = 12, N = 36 = 3g).$$

THEOREM 4. If $g \equiv 1 \pmod{3}$,

$$\max_{N < 4g} N = 3g + 3, \qquad S: y^3 = x(x^{g+1} - 1),$$
$$h(x, y) = (e^{2\pi i/(g+1)}x, e^{2\pi i/(3g+3)}y).$$

 $\max_{N<3g+3} N = 3g, \quad S: y^3 = x(x^g - 1), \quad h(x, y) = (e^{2\pi i/g}x, e^{2\pi i/3g}y),$

except for

S:
$$y^{12} = x^3(x-1)^2$$
 (g = 4, N = 12 = 3g),
: $y^{30} = x^5(x-1)^6$ (g = 10, N = 30 = 3g).

THEOREM 5. If $g \equiv 2 \pmod{3}$,

 $\max_{N < 4g} N = 3g, \quad S: y^3 = x^2(x^g - 1), \quad h(x, y) = (e^{2\pi i/g}x, e^{4\pi i/3g}y),$

except for

S:
$$y^6 = x^3(x-1)^3(x-\zeta)^2$$
 $(g=2, N=6=3g, \zeta \in \mathbb{C}, \zeta \neq 0, 1).$

We introduce the following notation; $\langle h \rangle$ denotes the cyclic group generated by *h* of order *N*. $\tilde{S} = S / \langle h \rangle$ denotes the closed Riemann surface of genus \tilde{g} obtained by identifying those points on *S* which are equivalent under the action of $\langle h \rangle$ on *S*. $\tilde{p}_1, \ldots, \tilde{p}_t \in \tilde{S}$ denote the projections of branch points of the covering map $\varphi: S \to \tilde{S}$. v_1, \ldots, v_t denote the multiplicities of φ at the branch points over $\tilde{p}_1, \ldots, \tilde{p}_t$, respectively. A Fuchsian group is said to be a $(\gamma; m_1, \ldots, m_n)$ group if its signature is $(\gamma; m_1, \ldots, m_n)$. If n = 0, it is said to be a surface group. A homomorphism from a Fuchsian group onto a finite group is said to be a surface kernel homomorphism if its kernel is a surface group.

LEMMA 1. (Harvey [2].) Let Γ be a $(\gamma; m_1, \ldots, m_n)$ group, Z_N the cyclic group of order N, and $M = \text{lcm}(m_1, \ldots, m_n)$. Then there exists a surface kernel homomorphism from Γ onto Z_N if and only if the signature $(\gamma; m_1, \ldots, m_n)$ satisfies the following l.c.m. condition;

(1) $M = \text{lcm}(m_1, \dots, \check{m}_i, \dots, m_n)$ $(i = 1, \dots, n)$. Here, \check{m}_i denotes the omission of m_i .

(2) M|N, if $\gamma = 0$ then M = N.

(3) $n \neq 1$, if $\gamma = 0$ then $n \geq 3$.

(4) If 2|M, the number of m_i 's which are divisible by the maximum power of 2 which divides M is even.

LEMMA 2. (Riemann-Hurwitz relation.)

$$2g - 2 = N(2\tilde{g} - 2) + N\sum_{i=1}^{t} \left(1 - \frac{1}{\nu_i}\right).$$

LEMMA 3. If $\tilde{t} = 0$, then S is conformally equivalent to the Riemann surface defined by

 $y^N = f(x)$ (f(x) is a polynomial of x).

LEMMA 4. $(\tilde{g}; v_1, \ldots, v_t)$ satisfies the l.c.m. condition.

Proof. Let D be the unit disk, K a Fuchsian surface group which uniformize S, and ψ the natural projection from D onto S = D/K. Let $D^* = D - (\varphi \circ \psi)^{-1} \{ \tilde{p}_1, \dots, \tilde{p}_t \}, \tilde{S}^* = \tilde{S} - \{ \tilde{p}_1, \dots, \tilde{p}_t \}$, and let Γ be the covering transformation group of the covering $\varphi \circ \psi$: $D^* \to S^*$. Then Γ is a $(\tilde{g}; \nu_1, \dots, \nu_t)$ group and $\Gamma/K \approx Z_N$. So from Lemma 1, we find that $(\tilde{g}; \nu_1, \dots, \nu_t)$ satisfies the l.c.m. condition.

LEMMA 5. If N > 2g - 2, then $\tilde{g} = 0$, t = 3, 4.

Proof. From the Riemann-Hurwitz relation, if $\tilde{g} \ge 2$,

 $2g-2 \ge N(2\tilde{g}-2) \ge 2N.$

This contradicts the hypothesis. If $\tilde{g} = 1$, from the l.c.m. condition, $t \ge 2$.

Then,

$$2g-2 = N \sum_{i=1}^{t} \left(1 - \frac{1}{\nu_i}\right) \ge tN/2 \ge N.$$

This also contradicts the hypothesis. So $\tilde{g} = 0$, and

$$2g - 2 = -2N + N \sum_{i=1}^{t} \left(1 - \frac{1}{\nu_i} \right) \ge \frac{(t-4)N}{2}$$

Thus t = 3, 4 or 5. But if t = 5,

$$2g-2 = N\left(3 - \sum_{i=1}^{5} \frac{1}{\nu_i}\right),$$

and from N > 2g - 2, we find that

$$2 < \sum_{i=1}^{5} \frac{1}{\nu_i} < 3.$$

The signatures which satisfy these inequalities are the following:

(0; 2, 2, 2, 2, *), (0; 2, 2, 2, 3, 3), (0; 2, 2, 2, 3, 4), (0; 2, 2, 2, 3, 5).None of these satisfies the l.c.m. condition.

LEMMA 6. If
$$N > 2g + 2$$
, then $t = 3$.

Proof. From Lemma 5, $\tilde{g} = 0$, t = 3, 4. If t = 4, from the Riemann-Hurwitz relation, we find that

$$1 < \sum_{i=1}^{4} \frac{1}{\nu_i} < 2.$$

The signatures which satisfy these inequalities and the l.c.m. condition are the following (N on the right side is given by $N = M = \text{lcm}(\nu_1, \nu_2, \nu_3, \nu_4)$, g is calculated from \tilde{g} , ν_1 , ν_2 , ν_3 , ν_4 , N by the Riemann-Hurwitz relation):

$(0; 2, 2, m, m) (m \neq 2)$	if $2 m$,	g=m/2, N=m=2g,
	if 2 + m,	g = m - 1, N = 2m = 2g + 2,
(0; 2, 3, 3, 6)		g=3, N=6=2g,
(0; 2, 3, 4, 12)		g=6, N=12=2g,
(0; 2, 3, 5, 30)		g = 15, N = 30 = 2g,
(0; 3, 3, 3, 3)		g = 2, N = 3 = 2g - 1,
(0; 3, 3, 4, 4)		g=6, N=12=2g,
(0; 3, 3, 5, 5)		g = 8, N = 15 = 2g - 1.

None of these satisfies N > 2g + 2.

Proof of theorems. If we assume $N \ge 3g (\ge 2g + 2)$, from Lemma 3, $\tilde{g} = 0$, t = 3 or exceptionally (I) $\tilde{g} = 0$, t = 4, $(\tilde{g}; \nu_1, \nu_2, \nu_3, \nu_4) = (0; 2, 2, 3, 3)$, g = 2, N = 6. When $\tilde{g} = 0$, t = 3, from the Riemann-Hurwitz relation, we find that

$$\frac{1}{3} < \frac{1}{\nu_1} + \frac{1}{\nu_2} + \frac{1}{\nu_3} < 1.$$

The signatures which satisfy these inequalities and the l.c.m. condition are the following;

	(0; 2, m, m)	$(2 m \text{ then } 4 m (m \neq 4))$	g=m/4,	N=m=4g,
	(0; 2, m, 2m)	$(2 + m (m \neq 3))$	g=(m-1)/2,	N=2m=4g+2,
	(0; 3, m, m)	$(3 m(m \neq 3))$	g=m/3,	N=m=3g,
	(0; 3, m, 3m)	(3 + m)	g=m-1,	N=3m=3g+3,
(II)	(0; 4, 5, 20)		g = 6,	N=20=3g+2,
	(0; 4, 6, 12)		g=4,	N=12=3g,
	(0; 4, 7, 28)		g=9,	N=28=3g+1,
	(0; 4, 9, 36)		g = 12,	N=36=3g,
	(0; 5, 6, 30)		g = 10,	N=30=3g.

So if we exclude the exceptional cases (I) and (II), the signatures $(\tilde{g}; \nu_1, \nu_2, \nu_3)$ are listed as following;

If
$$N = 4g + 2$$
, $(0; 2, 2g + 1, 4g + 2)$.
If $N = 4g$, $(0; 2, 4g, 4g)$.
If $N = 3g + 3$, $(0; 3, g + 1, 3g + 3)$.
(In this case, $3 + m$ and $g = m - 1$ imply $g \equiv 0, 1 \pmod{3}$.)
If $N = 3g$, $(0; 3, 3g, 3g)$.

Now S branches over three points of the Riemann sphere \overline{C} , and the branching orders are given as above, so if we assume that the projections of branch points are 0, 1 and ∞ , from Lemma 3, S is conformally equivalent to the Riemann surface defined by

$$y^N = x^a (x-1)^b,$$

where a, b are given by the following conditions;

$$1 \le a, b < N, N/(N, a) = \nu_1, N/(N, b) = \nu_2, N/(N, a + b) = \nu_3.$$

((N, a) denotes the g.c.m. of N and a.)

Then if N = 4g + 2, S is defined by

(1)
$$y^{4g+2} = x^{2g+1}(x-1)^{2k}$$
 $((2g+1,k) = 1, 1 \le k < 2g+1).$

This surface is conformally equivalent to the Riemann surface defined by

$$Y^2 = X(X^{2g+1} - 1)$$

under the birational transformation

$$\begin{cases} y = \frac{Y}{X^{g+1+k}}, \\ x = -\frac{1}{X^{2g+1}} + 1, \end{cases} \begin{cases} Y = e^{(g+1)\pi i/(2g+1)} \frac{x^a(x-1)^b y^{(2g+1)c}}{(x^p(x-1)^q y^{2r})^{g+1}}, \\ X = e^{\pi i/(2g+1)} \frac{1}{x^p(x-1)^q y^{2r}}, \end{cases}$$

where (a, b, c), (p, q, r) are the solutions of the indeterminate equations

$$\begin{cases} 2a + (2g + 1)c = 1, \\ b + kc = 0, \end{cases} \qquad \begin{cases} p + r = 0, \\ (2g + 1)q + 2kr = 1. \end{cases}$$

If N = 4g, S is defined by

(2)
$$y^{4g} = x^{2g}(x-1)^k$$
 $((4g,k) = (4g,2g-k) = 1, 1 \le k < 4g).$

This surface is conformally equivalent to the Riemann surface defined by

$$Y^2 = X(X^{2g} - 1),$$

under the birational transformation

$$\begin{cases} y = e^{\pi i/4g} X^{(k-1)/2} Y, \\ x = -X^{2g} + 1, \end{cases} \qquad \begin{cases} Y = e^{\pi i/4g} x^a (x-1)^b y^c, \\ X = e^{\pi i/2g} x^p (x-1)^q y^r, \end{cases}$$

where (a, b, c), (p, q, r) are the solutions of the indeterminate equations

$$\begin{cases} 2a + c = 1, \\ 4gb + kc = 1, \end{cases}$$
 $\begin{pmatrix} p + r = 0, \\ 2gq + kr = 1. \end{cases}$

If N = 3g + 3, S is defined by

(3)
$$y^{3g+3} = x^{j(g+1)}(x-1)^{3k}$$

((g+1,k) = (3g+3, (3-j)(g+1)-3k) =

 $j = 1, 2, 1 \le k < g + 1$).

1,

When $g \equiv 0 \pmod{3}$, (3) is conformally equivalent to the Riemann surface defined by

$$Y^3 = X^2 (X^{g+1} - 1),$$

under the birational transformation

$$\begin{cases} y = e^{k\pi i/(g+1)} \frac{Y^j}{X^{k+j(g/3+1)}}, \\ x = -\frac{1}{X^{g+1}} + 1, \end{cases}$$
$$\begin{cases} Y = e^{(g+3)\pi i/(3g+3)} \frac{x^a(x-1)^b y^{(g+1)c}}{(x^p(x-1)^q y^{3r})^{g/3+1}}, \\ X = e^{\pi i/(g+1)} \frac{1}{x^p(x-1)^q y^{3r}}, \end{cases}$$

where (a, b, c), (p, q, r) are the solutions of the indeterminate equations

$$\begin{cases} 3a + j(g+1)c = 1, \\ b + kc = 0, \end{cases} \qquad \begin{cases} p + jr = 0, \\ (g+1)q + 3kr = 1. \end{cases}$$

When $g \equiv 1 \pmod{3}$, (3) is conformally equivalent to the Riemann surface defined by

$$Y^3 = X(X^{g+1} - 1),$$

under the birational transformation

$$\begin{cases} y = e^{k\pi i/(g+1)} \frac{Y^j}{X^{k+j(g+2)/3}}, \\ x = -\frac{1}{X^{g+1}} + 1, \end{cases}$$
$$\begin{cases} Y = e^{(g+2)\pi i/(3g+3)} \frac{x^a(x-1)^b y^{(g+1)c}}{(x^p(x-1)^q y^{3r})^{(g+2)/3}}, \\ X = e^{\pi i/(g+1)} \frac{1}{x^p(x-1)^q y^{3r}}, \end{cases}$$

where (a, b, c), (p, q, r) are the solutions of the indeterminate equations

$$\begin{cases} 3a + j(g+1)c = 1, \\ b + kc = 0, \end{cases} \qquad \begin{pmatrix} p + jr = 0, \\ gp + kr = 1. \end{cases}$$

If N = 3g, S is defined by

(4)
$$y^{3g} = x^{jg}(x-1)^k$$

 $((3g,k) = (3g, (3-j)g - k) = 1, j = 1, 2, 1 \le k < g).$

Then we notice that $k \equiv j \pmod{3}$ or $k \equiv 2j \pmod{3}$. In the case $k \equiv j \pmod{3}$, (4) is comformally equivalent to the Riemann surface defined by

$$Y^3 = X(X^g - 1),$$

under the birational transformation

$$\begin{cases} y = e^{((k+jg)\pi i/3g)} X^{(k-j)/3} Y^{j}, \\ x = -X^{g} + 1, \end{cases} \qquad \begin{cases} Y = e^{((g+1)\pi i/3g)} x^{a} (x-1)^{b} y^{c}, \\ X = e^{\pi i/g} x^{p} (x-1)^{q} y^{3r}, \end{cases}$$

where (a, b, c), (p, q, r) are the solutions of the indeterminate equations

$$\begin{cases} 3a + jc = 1, \\ 3gb + kc = 1, \end{cases} \qquad \begin{cases} p + jr = 0, \\ gq + kr = 1 \end{cases}$$

In the case $k \equiv 2j \pmod{3}$, (4) is conformally equivalent to the Riemann surface defined by

$$Y^3 = X^2(X^g - 1),$$

under the birational transformation

$$\begin{cases} y = e^{((k+jg)\pi i/3g)} X^{(k-2j)/3} Y^j, \\ x = -X^g + 1, \end{cases} \qquad \begin{cases} Y = e^{\pi i/3} x^a (x-1)^b y^c, \\ X = e^{\pi i/3} x^p (x-1)^q y^{3r}, \end{cases}$$

where (a, b, c), (p, q, r) are the solutions of the indeterminate equations

$$\begin{cases} 3a + jc = 1, \\ 3gb + kc = 2, \end{cases} \quad \begin{cases} p + jr = 0, \\ gq + kr = 1. \end{cases}$$

Finally, if $g \equiv 0 \pmod{3}$, two Riemann surfaces

$$y^3 = x(x^g - 1)$$
 and $Y^3 = X^2(X^g - 1)$

are conformally equivalent under the birational transformation

$$\begin{cases} y = -X^{g/3+1}Y, \\ x = X^{-1}, \end{cases} \qquad \begin{cases} Y = -x^{g/3+1}y, \\ X = x^{-1}. \end{cases}$$

For a surface in (4), if $g \equiv 1 \pmod{3}$, we obtain $k \equiv j \pmod{3}$, while if $g \equiv 2 \pmod{3}$, $k \equiv 2j \pmod{3}$.

In the exceptional case (I), the surfaces are conformally equivalent to the Riemann surface defined by

$$y^6 = x^3(x-1)^3(x-\zeta)^2$$
 ($\zeta \in \mathbf{C}, \zeta \neq 0, 1$).

In the case (II), the surfaces which have the same signature are conformally equivalent to each other. Thus we have the following forms

$$y^{20} = x^{5}(x-1)^{4}, \quad (0; 4, 5, 20),$$

$$y^{28} = x^{7}(x-1)^{4}, \quad (0; 4, 7, 28),$$

$$y^{12} = x^{3}(x-1)^{2}, \quad (0; 4, 6, 12),$$

$$y^{36} = x^{9}(x-1)^{4}, \quad (0; 4, 9, 36),$$

$$y^{30} = x^{6}(x-1)^{5}, \quad (0; 5, 6, 30).$$

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