Pacific Journal of Mathematics

CORRECTION TO THE ARTICLE COVERING OF A HOLOMORPHICALLY CONVEX MANIFOLD CARRYING A POSITIVE LINE BUNDLE

SAID ASSERDA

Volume 236 No. 2

June 2008

CORRECTION TO THE ARTICLE COVERING OF A HOLOMORPHICALLY CONVEX MANIFOLD CARRYING A POSITIVE LINE BUNDLE

SAID ASSERDA

Volume 185:2 (1998), 201–208

Let \widetilde{M} be a connected holomorphic covering of a holomorphically convex manifold M. If M carries a positive holomorphic line bundle L such that the pullback of L is holomorphically trivial on \widetilde{M} , then \widetilde{M} is a Stein manifold.

In the paper being corrected, the argument given on page 203, six lines from the bottom, is erroneous. It is asserted that, after passing to a subsequence of $(z_k) := (x_{\nu_k})$ of (x_{ν}) , we may assume that

$$r(z_k) = \operatorname{dist}_{\tilde{g}}(z_k, x_0) \ge k + \rho_k,$$

where $\rho_k := \sup_{1 \le l \le k} \sup_{x \in X_l} \|s\|_{\pi^*L}$, since this would imply

$$r(z_k) = \operatorname{dist}_{\tilde{g}}(z_k, x_0) \ge k + c |f(z_k)|$$

for k large enough, where f_0 is a nowhere vanishing holomorphic function on $\pi^{-1}(U)$. But a priori $(|f(z_k)|)$ might tend to infinity. We overcome this difficulty as follows.

If the sequence (ρ_k) is bounded then we follow fully Case 1 on page 203.

If the sequence (ρ_k) is unbounded, assume that dim $M = n \ge 2$. Following the notations of Case 1, let k be large enough such that $9/R \le \rho_k^{1/(n-1)} \le \rho_k^{m/(n-1)}$ for all $m \ge 1$. Set

$$Y_k^m := \phi_k^{-1}(B(\phi_k(z_k), \rho_k^{-m/(n-1)})) \subset X_k := \phi_k(B(\phi_k(z_k), R/(4))).$$

 $(X_k \text{ is defined on page 203, line } -4.)$ Let $\theta \in C^{\infty}(\mathbb{R})$ such that $\theta = 1$ if $0 \le t \le 1/2$ and $\theta = 0$ if $t \ge 1$ and $0 \le \theta \le 1$. Let t_m the C^{∞} section of $\pi^*(L^m)$ over \widetilde{M} defined by 0 on $\widetilde{M} \setminus \bigcup_k Y_k^m$ and

$$t_m(x) := \theta(\rho_k^{m/(n-1)} \| \phi_k(x) - \phi_k(z_k) \|) e^{r(z_k)} \otimes_{i=1}^m s \quad \text{if } x \in Y_k^m.$$

MSC2000: 32E40, 32E10.

Keywords: holomorphic convexity, coverings, line bundle, Cauchy-Riemann operator.

Following page 204, line -2, we have on Y_k^m

$$\|\bar{\partial}t_m\|_{\pi^*(L^m)}^2 \leq C\rho^{2m/(n-1)}e^{2r(z_k)}\rho_k^{2m}.$$

Hence

$$\begin{split} \int_{\widetilde{M}} \|\bar{\partial}t_m\|^2 e^{-(\Psi+3c_1\tau)} dV_{\widetilde{g}} &\leq C \sum_{k=1}^{+\infty} \rho^{2m/(n-1)} e^{-r(z_k)} \rho_k^{2m} \operatorname{Vol}_{\widetilde{g}}(Y_k^m) \\ &\leq C \sum_{k=1}^{+\infty} \rho^{2m/(n-1)} e^{-r(z_k)} \rho_k^{2m} \operatorname{Vol}(B_e(\phi_k(z_k), \rho_k^{-m/(n-1)})) \\ &\leq C \sum_{k=1}^{+\infty} e^{-r(z_k)} < \infty, \end{split}$$

since we may suppose that $r(z_k) \ge k$ for k large enough. After this, we follow page 205, line -3.

If dim M = 1, then \widetilde{M} is a noncompact Riemann surface and hence a Stein manifold, by the Behnke–Stein theorem.

Acknowledgment

I think A. D. R. Choudary and V. Vâjâitu for bringing the error to my attention.

Received March 7, 2008.

SAID ASSERDA Université Ibn Tofaïl Département de Mathématiques BP 242 Kénitra 14 000 Morocco

said.asserda@laposte.net