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ELASTIC MODULI OF BORON NITRIDE NANOTUBES BASED ON FINITE ELEMENT METHOD

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Boron nitride nanotubes (BNNTs) possess superior thermal conductivity and mechanical/electrical properties, and are a suitable and favourable reinforcement for binanocomposites. Experimental studies on nanoscale materials are time-consuming, costly, and require accurate implementation. Therefore, a three-dimensional finite element (FE) model of a space-frame structure is proposed for BNNTs, which is based on molecular structural mechanics. The effects of length, chirality, diameter, and defect on the elastic moduli of BNNTs are investigated. The results show that defects in the nanotubes decrease the mechanical properties. The values of the Young's modulus and shear modulus of BNNTs without defects change from 1.022 TPa to 1.042 TPa and from 0.33 TPa to 0.536 TPa, respectively. It is found that, with increasing chirality and radius of BNNTs, the Young's modulus and shear modulus increase. As the length of zigzag and armchair BNNTs increases, the Young's modulus increases and the shear modulus decreases. Also, it was observed that by using the finite element method (FEM) based on molecular dynamics, one can accurately determine the mechanical properties of BNNTs. The results demonstrate that the proposed FE model is a valuable tool for studying the mechanical behaviour of BNNTs.

1. Introduction

Rubio et al. [1994] theoretically predicted boron nitride nanotube (BNNT). Then, Chopra et al. [1995] synthesized double-walled boron nitride nanotube (DWBNNT), and afterwards single-walled boron nitride nanotube (SWBNNT) was produced by arc discharge [Loiseau et al. 1996] and chemical substitution reactions [Golberg et al. 1999]. Over the past two decades, BNNTs have attracted researchers attention in different fields due to their novelty and superlative mechanical [Chen et al. 2004b; Griebel and Hamaekers 2007; Vaccarini et al. 2000], electrical [Khoo et al. 2004; Chen et al. 2004a; Ishigami et al. 2005; Terrones et al. 1996], and chemical properties [Golberg et al. 2001].

Similar to carbon nanotubes (CNTs), a BNNT can be imagined as rolled up hexagonal BN layers and have different types chirality, as well as zigzag and armchair configurations [Chopra et al. 1995]. BNNTs, like CNTs, have extraordinary mechanical properties [Hernández et al. 1998; Chopra and Zettl 1998], high thermal conductivity along the nanotube length [Chang et al. 2005], and good resistance to oxidation at high temperature [Chen et al. 2004b]. Despite their similar structures, BNNTs have different properties because of their different atoms [Fereidoon et al. 2015]. CNTs show a metallic, semiconductor, or insulator characteristic depending on chirality and diameter, while BNNTs, independent of their chirality, diameter, and number of walls, behave as an insulator for low electric fields [Khaleghian and Azarakhshi 2016; Molani 2017].

Keywords: elastic moduli, boron nitride nanotube, chirality, length, finite element method.

In addition, BNNTs are better able to store hydrogen compared to CNTs and have found many applications in hydrogen storage [Wu et al. 2004]. BNNTs are also nontoxic to health and environment due to their chemical inertness and structural stability. Therefore, BNNTs are particularly suitable for biological employment [Zhi et al. 2005].

The elastic properties of BNNTs have theoretically and experimentally been investigated. Slightly different results were presented, but all calculated values indicate a very high Young's modulus (note that it is slightly smaller than for CNTs), which has led to their use as a structural reinforcement of matrix materials [Zhi et al. 2010]. Polymer nanocomposites combining polymers and nanofiller components have attracted research attention from the academic and industrial communities due to their diverse functional applications, good processing, and relatively low cost [Mehar et al. 2017b; 2018].

First-principles [Bahrami Panah and Vaziri 2015], tight-binding [Hernández et al. 1998], density functional [Mirzaei and Salamat Ahangari 2016], and classical molecular mechanics [Li and Chou 2006] approaches have been performed to characterize the properties of BNNTs. By using thermal vibration amplitude analysis, Chopra and Zettl [1998] estimated $1.22\,\mathrm{TPa}\pm0.24\,\mathrm{TPa}$ for the Young's modulus of multiwalled boron nitride nanotubes (MWBNNTs). Hernández et al. [1999] employed the tight-binding method to obtain 862 GPa–940 GPa for the axial Young's modulus of BNNTs. Verma et al. [2007] obtained the axial Young's modulus of the zigzag and armchair BNNTs using the tight-binding method. They also observed that the Young's modulus of zigzag tubes is higher than for armchair ones.

Akdim et al. [2003] indicated that the Young's modulus of BNNTs is in range of 0.71 TPa–0.83 TPa and is slightly dependent on the tube diameter. Also, theoretically, Young's modulus has been predicted to be 1.2 TPa [Hernández et al. 1998; 1999].

The Young's modulus of DWBNNT was calculated by Fakhrabad and Shahtahmassebi [2013] using the ab initio calculations based on density functional theory (DFT), and their estimated value is 821 GPa and 764 GPa for (2, 2) @ (7, 7) and (2, 2) @ (9, 9), respectively. The Young's modulus of SWBNNTs with vacancy and functionalization defects was calculated by Gerieble and Hamaekers [Griebel et al. 2009] using a molecular dynamics (MD) simulation. They found that Young's modulus decreases with increasing defect concentration. Furthermore, for functionalized BNNTs, they reported no significant decrease with increasing functionalization [Santosh et al. 2009].

The experimental value of Young's modulus of BNNTs is reported to be 1.1 TPa–1.3 TPa [Bettinger et al. 2002]. In another experimental effort, Wei et al. [2010] obtained the value of 895 GPa for the Young's modulus of MWBNNT. Survavanshi et al. [2004] applied the electric-field-induced resonance method and specified the Young's modulus as 0.8 TPa. Golberg et al. [2007] used an integrated TEM-atomic force microscope (AFM) piezodriven holder to directly test the elastic modulus. The values of 0.5 TPa–0.6 TPa were found for MWBNNTs grown by the BOCVD method.

Experimental studies on nanoscale materials are time-consuming, costly, and require accurate implementation. Therefore, analytical, computational, and theoretical approaches are applied to predict the mechanical properties of nanoscale materials [Mehar et al. 2017a; 2017c; 2017d; Mehar and Panda 2017]. Two main classes of theoretical methods are the atomistic-based methods [Yakobson et al. 1996; Lu 1997; Sánchez-Portal et al. 1999] and the continuum mechanics-based ones [Li and Chou 2003; Chang and Gao 2003; Odegard et al. 2002]. A three-dimensional finite element (FE) model, named as the space-frame model, is used to study the mechanical behaviour of BNNTs. Ansari et al. [2015] used DFT calculations to obtain accurate force constants which are employed when determining element properties.

Fundamental to these approaches, BNNTs are considered as geometrical space-frame structures. Therefore, BNNTs can be analysed by classical structural mechanics. In this paper, the effects of length, chirality, diameter, and defect on the elastic moduli of BNNTs are studied. While this method is conceptually simple and computationally efficient, our results indicate that its computational accuracy is comparable to that of more refined methods such as first-principle and tight-binding methods. Our study has clearly demonstrated the dependency of Young's modulus and shear modulus of BNNTs on tube length, chirality, and radius.

2. FE modelling

2.1. Atomic structure of BNNTs. The atomic structure of BNNTs depends on chirality, which is defined by the chiral vector \vec{C}_h and the chiral angle θ . The chiral vector \vec{C}_h can be defined in terms of the lattice translation indices (n, m) and the basic vectors \vec{a}_1 and \vec{a}_2 of the hexagonal lattice as [Hemmatian et al. 2014]

$$\vec{C}_h = n\vec{a}_1 + m\vec{a}_2. \tag{1}$$

The chiral angle θ is the angle between the chiral vector \vec{C}_h with respect to the zigzag direction (n,0) where $\theta=0^\circ$. For the chiral angles of 0° and 30° , the armchair and zigzag nanotubes are formed, respectively. In terms of the roll-up vector, the armchair nanotubes are defined by (n,n) and the zigzag nanotubes by (n,0). For chiral angles different from 0° and 30° , the chiral nanotubes, which are defined by a pair of indices (n,m), where $n\neq m$, are formed. Schematic representations of the three types of nanotubes are shown in Figure 1.

2.2. *Modelling.* BNNTs atoms are bonded together with covalent bonds forming a hexagonal lattice. These bonds have a characteristic bond length and bond angle in the 3D space. The displacement of individual atoms under an external force is constrained by the bonds. Therefore, the total deformation of the nanotube is the result of the interactions between the bonds. By considering the bonds as connecting load-carrying elements, and the atoms as joints of the connecting elements, BNNTs may be simulated as space-frame structures and their mechanical behaviour can be analysed using classical structural mechanics. The 3D FE model is developed using the ANSYS commercial code to assess the mechanical properties of BNNTs.

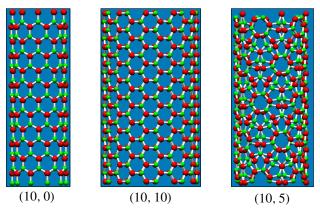


Figure 1. Schematic diagram of zigzag (10, 0), armchair (10, 10), and chiral (10, 5) nanotubes.

nanotube diameter, d	1.648 Å
cross-sectional area, A	2.132Å^2
length of boron-nitrogen bond, l	1.45 Å
polar inertia momentum, I_{xx}	0.7250Å^4
inertia momentum, $I_{zz} = I_{yy} = I$	$0.3625{\rm \AA}^4$
Young's modulus, E	$4.2155 \cdot 10^{-8} \mathrm{N/\AA^2}$
shear modulus, G	$4.9437 \cdot 10^{-9} \mathrm{N/\mathring{A}^2}$

Table 1. The properties of beam elements for a real BNNT [Ansari et al. 2015].

To model a BNNT, it is necessary to create atomic coordinates in the form of a keypoint or node and connecting atoms by a line or element. One of the possible outputs of the Nanotube Modeller software is the PDB, which specifies the coordinates of each atom as x, y, and z, and also identifies the connected atoms. But this output is not understandable for ANSYS, which is an APDL programming language. To convert the output file of the PDB format into an APDL language, Python interface programming software is used. A brief program in Python is written for each atom of carbon, a point with coordinates x, y, and z, and for each atomic connection, which creates a line between the two points. The 3D elastic BEAM4 element is used for meshing linens and modelling bonds. This element is a uniaxial element with tension, compression, torsion, and bending capabilities. It has six degrees of freedom at each node: translations in the nodal x-, y-, and z-directions and rotations about the nodal x-, y-, and z-axes. The element is defined by two or three nodes as well as its cross-sectional area, two moments of inertia, two dimensions, and the material properties. For the automatic generation of the BN bonds elements, a routine was created using the ANSYS macrolanguage.

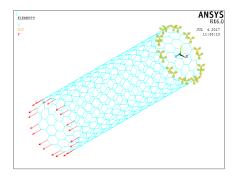
2.3. Atomic properties of beam elements. Molecular structural mechanics (MSM) along with FEM is used for modelling. MSM is a moderately new technique for the mechanical modelling of nanostructures [Li and Chou 2003]. Covalent bonds are modelled with beam elements as they form only at certain intervals among atoms and act linearly. The properties of these elements are obtained by linking the potential energy of bonds (from a chemical point of view) and the strain energy of mechanical elements (from a mechanical point of view). To represent the covalent bond between boron and nitrogen atoms, a circular beam of length l, diameter d, Young's modulus E, and shear modulus G was considered. To obtain the properties of this model, a linkage between the molecular mechanics and the density functional theory is constructed [Ansari et al. 2015]. The required properties of the beam element are given in Table 1.

3. Calculation of elastic moduli

3.1. Young's modulus. The Young's modulus of a material is the ratio of normal stress to normal strain as obtained from a uniaxial tension test $(E = \sigma/\varepsilon)$. Therefore, the Young's modulus of BNNT is calculated using the following equation:

$$E = \frac{FL}{\delta L A_0},\tag{2}$$

where F is applied force to nanotube, A_0 is the cross-sectional area, and L is the initial length. The longitudinal displacement of the nanotube δL is determined from FE analysis. A_0 is equal to πDt ,



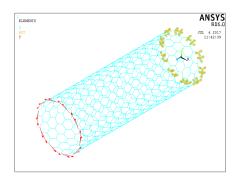


Figure 2. FE meshes of the (10, 10) nanotube with length 40 Å along with the applied loading and boundary conditions: (left) tension, (right) torsion.

where D is the mean diameter of the tube and t is the nanotube thickness. The wall thickness of BNNTs has not yet been clearly specified. The wall thickness is selected as $0.34 \, \text{nm}$ [Zhi et al. 2005] and the centre of the BNNT wall is placed at the midsection of the tube thickness.

In order to apply the conditions of tension, the nodes of the upper end of the BNNT have been fully built-in (zero displacement and rotation conditions), while the nodes of the bottom end, are subjected to tensile forces [Fereidoon et al. 2014]; see Figure 2 (left).

3.2. Shear modulus. The following relation is used for calculating the shear modulus of BNNTs:

$$G = \frac{TL}{J\theta},\tag{3}$$

where T stands for the torque acting at the one end of the nanotube and applied by tangential forces. Here, θ and J are torsional angle and polar moment of inertia of the cross-sectional area of the BNNT, respectively. The torsional angle θ is calculated by FE analysis. J is computed by (4), considering the BNNT as a hollow tube with middiameter D and thickness t:

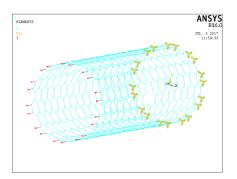
$$J = \frac{1}{32}\pi[(D+t)^4 - (D-t)^4]. \tag{4}$$

In order to apply the conditions of torsion, the nodes of the upper end of the BNNT are fully built-in (zero displacement and rotation conditions), while the nodes of the bottom end are subjected to tangential forces; see Figure 2 (right).

4. Results and discussions

The mechanical properties of BNNTs depend on their length, chirality, diameter, and defect. Several works investigated the dependence of the elastic moduli of BNNTs on their diameter and chirality. Armchair and zig-zag nanotubes are included in the investigation.

4.1. Elastic moduli of BNNT and defected BNNT. The elastic properties of BNNTs depend on their size and chirality. In this section, the FE model is applied to investigate the effect of chirality on the elastic moduli of regular BNNTs and defected ones. For modelling defective nanotubes, three bonds of each nanotube are omitted. Loading and boundary conditions of defected (10, 10) BNNTs with length of 40 Å in tension and torsion states are shown in Figure 3 (left) and Figure 3 (right), respectively.



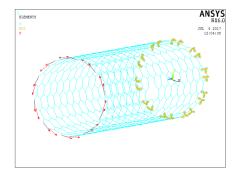


Figure 3. FE meshes of the (10, 10) defected nanotube with length 40 Å along with the applied loading and boundary conditions: (left) tension, (right) torsion.

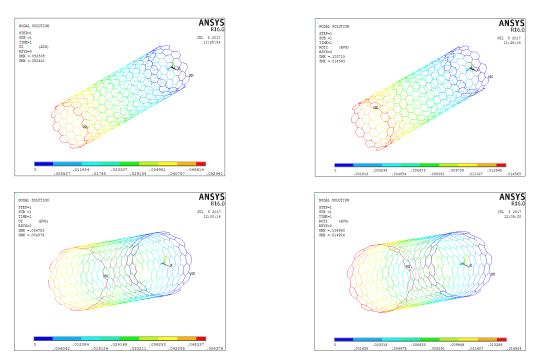


Figure 4. Deformations of a regular nanotube (top) and a defected one (bottom) under tension (left column) and torsion (right column) loading.

Deformations of nanotubes and defected nanotubes under tension and torsion loading are represented in Figure 4. As shown in Figure 4, the longitudinal and angular deformations of defected nanotubes were more pronounced than in regular nanotubes. Figure 5 shows the comparisons of the Young's and shear moduli of regular BNNTs and defected ones with length 40 Å in terms of chirality. Results show that as the chirality increases, the Young's modulus and shear modulus of the BNNT increases but the increase in Young's modulus is not considerable. The mechanical properties of the defected nanotube were lower than the nanotube with the same chirality. Also, as the chirality increases, the elastic moduli of defected BNNT increases.

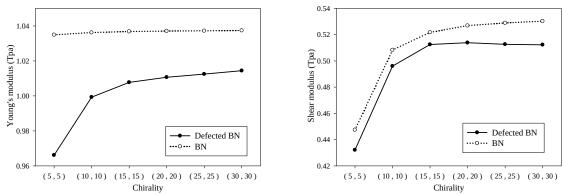


Figure 5. The elastic moduli of a regular nanotube and a defected one plotted against the chirality for $L = 40 \,\text{Å}$.

elastic moduli	(TPa)	reference	
Young's modulus	1.22 ± 0.24	[Chopra and Zettl 1998]	
	1.022-1.112	[Fereidoon et al. 2015]	
	0.71 - 0.83	[Zhi et al. 2010]	
	0.862 - 0.94	[Verma et al. 2007]	
	0.982 - 1.11	[Hernández et al. 1999]	
	0.895	[Fakhrabad and Shahtahmassebi 2013	
	0.7-1.2	[Santosh et al. 2009]	
	0.7-1.2	[Bettinger et al. 2002]	
	1.1–1.3	[Wei et al. 2010]	
	0.764-0.821	[Suryavanshi et al. 2004]	
	0.7 – 0.9	[Zhong et al. 2001]	
	1	[Chowdhury et al. 2010]	
	1.034-1.037	current work	
shear modulus	0.42	[Chowdhury et al. 2010]	
shear modulus	0.44-0.53	current work	

Table 2. Elastic moduli of BNNTs from simulation and experimental works.

The Young's and shear moduli of BNNTs are archived by tension and torsion loading in the range of 1.039 TPa–1.041 TPa and 0.44 TPa–0.52 TPa, respectively. Elastic moduli of BNNT from simulation and experimental works are given in Table 2. The current results are in good agreement with simulated and experimental values.

4.2. Young's modulus. Zigzag nanotubes with chirality (5,0), (10,0), (15,0), (20,0), (25,0), and (30,0) and armchair nanotubes with chirality (5,5), (10,10), (15,15), (20,20), (25,25), and (30,30) were analysed under tension forces. The BNNTs have lengths of $40\,\text{Å}$, $60\,\text{Å}$, $80\,\text{Å}$, and $100\,\text{Å}$. The effects of chirality, length, and radius on the Young's moduli of BNNTs are investigated in the following:

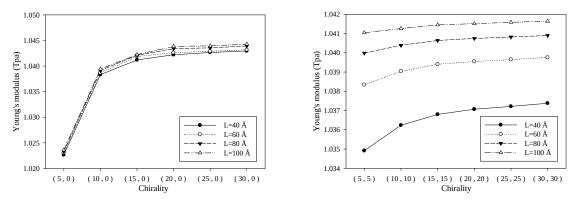


Figure 6. Young's modulus of BNNTs as a function of chirality: (left) zigzag, (right) armchair.

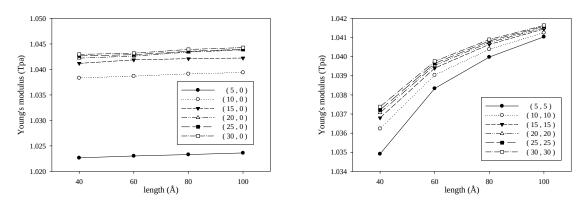


Figure 7. Young's modulus of BNNTs as a function of length: (left) zigzag, (right) armchair.

Chirality. Figures 6 (left) and 6 (right) indicate the variation of Young's modulus of zigzag and armchair nanotubes (respectively) with lengths of 40 Å, 60 Å, 80 Å, and 100 Å as a function of chirality. For armchair and zigzag nanotubes, with increasing chirality and consequently radius, the Young's modulus increases. The gradients of variations are greater in small radii, and with increasing radius, the Young's modulus tends to constant values. Moreover, the Young's moduli of zigzag nanotubes with different lengths are very close, but in armchair nanotubes, the differences are significant.

Length. Variations of Young's modulus of zigzag and armchair nanotubes with respect to length are plotted in Figures 7 (left) and 7 (right), respectively. For armchair and zigzag nanotubes, with increasing length, the Young's modulus increases. The gradients of variations become smaller as the length increases, and tend to constant values. Furthermore, the changes of Young's moduli of zigzag BNNTs with respect to lengths aren't considerable when compared to armchair ones.

Radius. Armchair and zigzag nanotubes are arranged in terms of increasing nanotube radius and are represented in Table 3. Young's moduli of armchair and zigzag nanotubes in terms of radius for different lengths is shown in Figure 8. Generally, with an increase in radius, the Young's modulus of BNNTs increases. But for roughly similar radii, the Young's moduli of zigzag nanotubes are larger than for armchair nanotubes. For example, the radius of the nanotube (10, 10) lies between the radii of the nanotubes (15, 0) and (20, 0), but its Young's modulus is less than the two other BNNTs.

chirality	radius	chirality	radius
(5, 0)	1.999	(25, 0)	9.993
(5, 5)	3.462	(15, 15)	10.385
(10, 0)	3.997	(30, 0)	11.991
(15, 0)	5.996	(20, 20)	13.846
(10, 10)	6.923	(25, 25)	17.308
(20, 0)	7.994	(30, 30)	20.77

Table 3. Arranging armchair and zigzag nanotubes in terms of increasing radius.

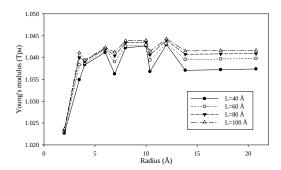


Figure 8. Young's modulus of zigzag and armchair BNNTs as a function of radius.

4.3. Shear modulus. Zigzag nanotubes with chirality (5, 0), (10, 0), (15, 0), (20, 0), (25, 0), and (30, 0) and armchair nanotubes with chirality (5, 5), (10, 10), (15, 15), (20, 20), (25, 25), and (30, 30) were analysed under torsion forces (torque). BNNTs with different lengths of 40 Å, 60 Å, 80 Å, and 100 Å were studied. The influences of chirality, length, and radius on the shear modulus of BNNTs were studied and results are given in the following:

Chirality. Figures 9 (left) and 9 (right) illustrate the variations of shear moduli of zigzag and armchair nanotubes with lengths of 40 Å, 60 Å, 80 Å, and 100 Å in terms of chirality. As the chirality increases, and subsequently as the radii of the zigzag and armchair nanotubes increase, their shear moduli increase. The slope of the changes in the smaller radii is greater and reaches a constant value as the radius increases. Furthermore, the shear moduli of armchair-type nanotubes are larger than the zigzag and increase as the chirality increases. As chirality increases, the shear moduli of armchair and zigzag nanotubes approximately reach equal constant value.

Length. Shear moduli of zigzag and armchair nanotubes with respect to length are plotted in Figure 10, left and right, respectively. Figure 10 indicates that as the length of zigzag and armchair BNNTs increases, the shear modulus decreases. The gradients of variations reduce with increasing length and tend to constant values. The results show that the mechanical properties of BNNTs depend on chirality and the length of the nanotubes.

Radius. Shear moduli of armchair and zigzag nanotubes in terms of radius for different lengths is plotted in Figure 11. In general, with increasing radius, the BNNT shear modulus increases. But for roughly similar radii, the moduli of zigzag nanotubes is larger than the armchair ones.

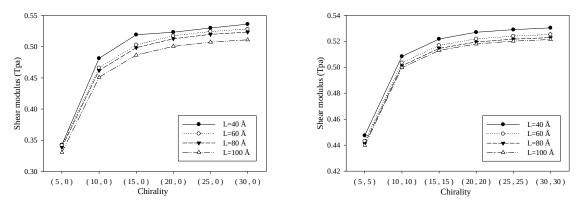


Figure 9. Shear modulus of BNNTs as a function of chirality: (left) zigzag, (right) armchair.

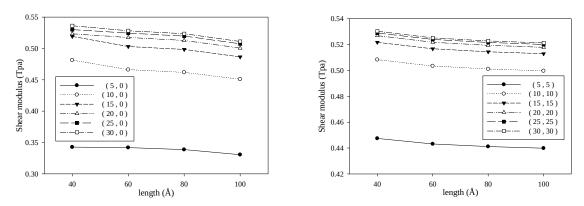


Figure 10. Shear modulus of BNNTs as a function of length: (left) zigzag, (right) armchair.

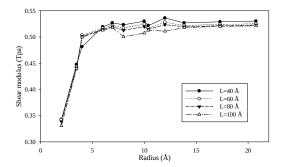


Figure 11. Shear modulus of zigzag and armchair BNNTs as a function of radius.

5. Conclusions

Three-dimensional finite element (FE) models for BNNTs have been proposed. To create the FE models, nodes are placed at the locations of atoms and the bonds between them are modelled using three-dimensional elastic beam elements via considering a linkage between molecular and continuum mechanics. The FE model comprises a small number of elements and performs with minimal computational time

and minimal computational power. This advantage, in combination with the modelling abilities of the FE method, extends the model applicability to all kinds of nanotubes with very large numbers of atoms.

The results showed that defection of nanotube decreases the mechanical properties. The effects of chirality, length, and radius on Young's modulus and shear modulus of armchair and zigzag BNNTs were investigated based on the FE model. The values of the Young's modulus and shear modulus of BNNTs without defects have changed from 1.022 TPa to 1.042 TPa and from 0.33 TPa to 0.536 TPa, respectively.

Results show that with increasing chirality, and consequently radius, the Young's modulus and shear modulus increase. As the length of zigzag and armchair BNNTs increases, the Young's modulus increases and the shear modulus decreases. Generally, as the radius increases, the Young's modulus and shear modulus increase. Furthermore, in a roughly similar radius, generally, the elastic moduli of zigzag nanotubes are larger than the armchair ones. Hence, the elastic moduli of BNNTs, especially at low radii and lengths, depend on the chirality (atomic arrangement) and the length of the nanotubes.

Also, it was observed that by using the FEM based on molecular dynamics, one can accurately determine the mechanical properties of the BNNTs. Due to the mechanical properties, BNNTs can be applied as a suitable substitute for CNTs in combination with polymers to produce specific nanocomposites.

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