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PEAK INTERPOLATION SETS FOR SOME ALGEBRAS OF ANALYTIC FUNCTIONS

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PEAK INTERPOLATION SETS FOR SOME ALGEBRAS OF ANALYTIC FUNCTIONS

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For certain algebras of analytic functions on holomorphically convex sets in C^n metric sufficient conditions are given for a set (not necessarily compact) to be an interpolation set. The results extend the Rudin-Carleson theorem for the disc algebra.

Let K be a compact subset of C^n which is holomorphically convex, i.e. K is the intersection of a decreasing sequence of pseudoconvex domains (see [4], Ch. 2). We denote by H(K) the uniform closure on K of the algebra of all functions analytic in a neighborhood of K. and by A(K) the algebra of all continuous functions on K analytic on K° (the interior of K). If E is any subset of the boundary ∂K of K then we denote by H_{E}^{∞} the algebra of all bounded continuous functions on $K^0 \cup E$ which are analytic on K^0 . We show that if the boundary of K is well behaved at each point of E, and E satisfies a metric condition which says roughly that E has zero 2-dimensional measure in the directions of the complex tangent and zero one dimensional measure in the orthogonal direction, then E is a peak interpolation set (in an appropriate sense) for $H^{\infty}_{E \cup (\partial K \setminus E)}$. If E is compact then it is a peak interpolation set in the usual sense ([2], p. 59) for the uniform algebra H(K). We show also that if E has zero one-dimensional measure then the conditions on ∂K can be relaxed.

We say that ∂K is strictly pseudoconvex in a neighborhood of a point $\zeta \in \partial K$ if there is an open neighborhood V of ζ such that $V \cap$ ∂K is a C²-submanifold of V and the Levi form is positive definite at ζ . Then we can find an open neighborhood V of ζ and a C² strictly plurisubharmonic function ρ in V such that $K \cap V = \{z \in V: \rho(z) \leq 0\}$ and grad $\rho \neq 0$ on $V \cap \partial K$. (See [3] Prop. IX. A4).

LEMMA 1. Let K be a holomorphically convex compact set in C^n and let ζ be a point of ∂K in a neighborhood of which ∂K is strictly pseudoconvex. We can find positive numbers m_{ζ} and M_{ζ} and $G_{\zeta} \in H(K)$, such that

(a) Re $G_{\zeta}(z) \geq m_{\zeta} | \zeta - z |^2, z \in K$

- (b) Re $G_{\zeta}(z) \leq M_{\zeta} | \zeta z |^2, z \in \partial K$
- (c) grad ($\operatorname{Re} G_{\zeta}$)(ζ) = grad $\rho(\zeta)$.

Proof. Put

$$F(z) = \sum_{i=1}^n rac{\partial
ho(\zeta)}{\partial \zeta_i} \left(z_i - \zeta_i
ight) + rac{1}{2} \sum_{i,j=1}^n rac{\partial^2
ho(\zeta)}{\partial \zeta_i \partial \zeta_j} \left(z_i - \zeta_i
ight) \left(z_j - \zeta_j
ight) \, .$$

Then the Taylor expansion of ρ about ζ is

$$ho(z)=2 \operatorname{Re} F(z) + \sum_{i,j=1}^n rac{\partial^2
ho\left(\zeta
ight)}{\partial \zeta_i \, \overline{\partial \zeta_j}} (z_i-\zeta_i) (z_j-\zeta_j) + o(|z-\zeta|^2) \;.$$

Since ρ is strictly plurisubharmonic at ζ it follows that, shrinking V if necessary, we can find m > 0 with Re $F(z) \leq -m|\zeta - z|^2$ for $z \in K \cap V$. Since $\rho = 0$ on $\partial K \cap V$ we also deduce that for some constant M

Re
$$F(z) \ge -M|\zeta - z|^2$$
; $z \in \partial K \cap V$.

Choose a pseudoconvex open neighborhood U of K so that Re F < 0on an open neighborhood W of $\partial V \cap U$ in U. Let $W_1 = W \cup (V \cap U)$ and $W_2 = W \cup (U \setminus \overline{V})$, so that $W_1 \cup W_2 = U$ and $W_1 \cap W_2 = W$. By solving a Cousin problem in U (see [4], Theorem 5.5.1) we can find analytic functions g_1 and g_2 on W_1 and W_2 respectively such that $g_2 - g_1 = F^{-2} \log F$ on W.

$$ext{Put} \ h(z) = egin{cases} F(z) \exp{(F(z)^2 g_1(z))}, \ z \in W_1 \ \exp{(F(z)^2 g_2(z))}, \ z \in W_2 \ . \end{cases}$$

The definitions agree on W so h is an analytic function on U, h(z) = 0only when $z = \zeta$, and in a neighborhood of ζ , $h(z) = F(z) + 0(|z - \zeta|^3)$. Thus Re $h \leq 0$ near ζ , so there exists $\varepsilon > 0$ such that if $z \in K$ and $|h(z) - \varepsilon| \leq \varepsilon$ then $z = \zeta$. Put

$$G(z) = \, - \, rac{h(z)}{arepsilon \, - \, h(z)}$$
 , $z \in K$.

Then $G \in \overline{H}(K)$, Re G(z) > 0 for $z \in K \setminus \{\zeta\}$. Finally, near ζ , Re $G(z) = -\varepsilon^{-1} \operatorname{Re} F(z) + \varepsilon^{-2} (\operatorname{Im} F)^2 + 0(|z - \zeta|^3)$ from which it follows that $G_{\zeta} = 2\varepsilon G$ has the required properties.

If S is a real subspace of C^n and Y is any subset we denote by $d_s(Y)$ the diameter (in the Euclidean metric) of the (real) orthogonal projection of Y on S.

Let K be a compact holomorphically convex subset of C^* and suppose ∂K is strictly pseudoconvex in a neighborhood of a point $\zeta \in \partial D$. Then in a neighborhood of ζ we can write $\partial K = \{z: \rho(z) = 0\}$ where $\rho(z)$ is strictly plurisubharmonic in a neighborhood of ζ and grad $\rho \neq 0$. The vector *i* grad ρ is orthogonal to grad ρ and so lies in the (real) tangent space to ∂K at ζ ; let $T(\zeta)$ be the orthogonal complement to *i* grad ρ in this space. Then $T(\zeta)$ is the unique complex subspace of the real tangent space with complex dimension n - 1. Let $L(\zeta)$ be the real line spanned by the vector i grad ρ .

If E is any subset of ∂K we denote by H^{∞}_{E} the set of all bounded continuous functions on $K^{\circ} \cup E$ which are analytic on K° . We define $A(K) = H^{\infty}_{\partial K}$.

THEOREM 1. Let F be a subset of ∂K such that ∂K is strictly pseudoconvex in a neighborhood of F. Suppose that for every $\varepsilon > 0$ the set F can be covered by a sequence $\{V_i\}$ of open sets with diameter $< \varepsilon$ such that if $\zeta_i \in F \cap V_i$ for each i then $\sum_i d_{L(\zeta_i)}(V_i) < \varepsilon$ and $\sum_i \{d_{T(\zeta_i)}(V_i)\}^2 < \varepsilon$. Let V be a neighborhood of F, let $\eta > 0$, and let g be a bounded continuous function on F with $||g|| \leq 1$.

Then we can find $f \in H^{\infty}_{F \cup (K \setminus \overline{F})}$ with f | F = g, $||f|| \leq 1$, and $|f| < \eta$ on $K \setminus V$.

The proof will be split up into lemmas.

LEMMA 2. Let F, V and η be as in the theorem. Then we can find $f \in H^{\infty}_{F \cup (K \setminus \overline{F})}$ with f = 1 on F, $||f|| \leq 2$ and $|f| < \eta$ on $K \setminus V$.

Proof. For each $\zeta \in F$ we choose m_{ζ} , $M_{\zeta} > 0$, and a function $G_{\zeta} \in H(K)$ as in Lemma 1.

If W_{ζ} is a sufficiently small open neighborhood of ζ , then whenever $\zeta \in U \subseteq W_{\zeta}$ and $z \in U \cap \partial K$ we have

$$egin{aligned} &|\,G_{\zeta}(z)\,| &\leq \operatorname{Re}G_{\zeta}(z)\,+\,|\operatorname{Im}G_{\zeta}(z)\,| \ &\leq A_{\zeta}\,|\,z-\zeta\,|^{\,2}\,+\,|<\operatorname{grad}\,(\operatorname{Im}G_{\zeta})(\zeta),\,z-\zeta\,>\,| \ &\leq 2A_{\zeta}(d_{\scriptscriptstyle 1}^{\scriptscriptstyle 2}\,+\,d_{\scriptscriptstyle 2}^{\scriptscriptstyle 2})\,+\,|\,\operatorname{grad}\,
ho(\zeta)\,|\,d_{\scriptscriptstyle 1}\ &\leq B_{\zeta}(d_{\scriptscriptstyle 1}\,+\,d_{\scriptscriptstyle 2}^{\scriptscriptstyle 2}) \end{aligned}$$

where $d_1 = d_{L(\zeta)}(U)$, $d_2 = d_{T(\zeta)}(U)$, A_{ζ} , B_{ζ} do not depend on z, and \langle , \rangle denotes the real scalar product.

For each positive integer n let

Then $F = \bigcup_n F_n$. For each n we choose a sequence $\{V_i^{(n)}\}$ of open sets with diameter less than 1/n such that each point of F_n is contained in infinitely many $V_i^{(n)}$, and $\sum_i \{d_{L(\zeta_i^n)}(V_i^n) + (d_{T(\zeta_i^n)}(V_i^n))^2\} < \eta n^{-2}2^{-n-2}$ for some choice of $\zeta_i^{(m)} \in V_i^{(m)} \cap F_n$. Renumber the collection of all $V_i^{(n)}$ as V_1, V_2, \cdots . For each j choose n_j so that $V_j = V_i^{(n_j)}$ for some i, and let $\zeta_j = \zeta_i^{(n_j)}$. Let $G_j = G_{\zeta_j}$. Writing $c_j = d_{L(\zeta_j)}(V_j) + \{d_{T(\zeta_j)}(V_j)\}^2$ we define

$$B_r(z) = \prod_{j=1}^r rac{G_j(z)}{2n_j c_j + G_j(z)}$$
, $z \in K, r = 1, 2, \cdots$.

Then $B_r \in H(K)$ and $|B_r| \leq 1$ on K. We claim that $\{B_r\}$ converges pointwise on $F \cup (K \setminus \overline{F})$ to a limit B which is continuous on $F \cup (K \setminus \overline{F})$, analytic on K° , zero at each point of F, with $||B|| \leq 1$ and $|1 - B| < \eta$ on $K \setminus V$.

If $z \in K \setminus V$ then Re $G_j(z) \ge m_{\zeta_j} |z - \zeta_j|^2 > 1/n_j$, so

$$egin{aligned} &\sum_{j=1}^\infty \left| 1 - rac{G_j(z)}{2n_j c_j + G_j(z)}
ight| \, = \, \sum_{j=1}^\infty rac{2n_j c_j}{|\, 2n_j c_j + G_j(z)\,|} \ &\leq \sum_{j=1}^\infty 2n_j^2 c_j < \eta/2 \;, \end{aligned}$$

which proves that $B_r(z)$ converges to a limit B(z) with $|1 - B(z)| < \eta$. If $z \in K \setminus \overline{F}$ then

$$\sum_{j=j_0}^\infty rac{2n_j c_j}{|\,2n_j c_j\,+\,G_j(z)\,|} \leq \, \sum_{j=j_0}^\infty rac{2n_j^2 c_j}{|\,z\,-\,\zeta_j\,|^{\,2}} \leq d(z,\,F)^{-2} \sum_{j=j_0}^\infty \,2n_j^2 c_j \;.$$

The series on the right converges, so B_r converges uniformly to a limit B on sets at positive distance from F, so B is continuous on $K \setminus \overline{F}$ and analytic on K° .

Finally let $z \in F$. Then $z \in V_j$ for infinitely many j. For each such j we have $V_j \subseteq W_{\zeta_j}$ and for all $w \in W_{\zeta_j}$,

$$\left|rac{G_j(w)}{2n_jc_j+G_j(w)}
ight| \leq rac{n_jc_j}{2n_jc_j} = rac{1}{2} \; .$$

It follows that $B_r(z) \to 0$ and $\lim |B_r|$ is continuous at z. Thus B has the asserted properties, and f = 1 - B satisfies the requirements of the theorem.

LEMMA 3. Let X be a compact subset of K, W a neighborhood of X, and h a continuous function on K with support in X such that $||h|| \leq 1$. Let $\eta > 0$.

Then there exists $f \in H^{\infty}_{F \cup (K \setminus \overline{F})}$ such that $|f - h| < \eta$ on F, $||f|| \leq 3$, and $|f| < \eta$ on $K \setminus W$.

Proof. Choose $0 < \delta < d(X, K \setminus W)$ so small that $|h(x) - h(y)| < \eta/8$ whenever $x, y \in K, |x - y| < \delta$. We can easily find an integer N > 0, compact sets $X_1 \cdots X_r$ contained in X, and open sets $W_1 \cdots W_r$, with diameters $< \delta$, with $W_i \supseteq X_i, W_i \subseteq W$, such that

(a) if $x \in X$ and N_x is the number of integers i in $\{1, \dots, r\}$ for which $x \in X_i$, $|N_x - N| < \eta N/8$

(b) if $x \in C^n$ the number of integers *i* for which $x \in W_i \setminus X_i$ is less than ηN .

Let $F_i = F \cap X_i$. For $i = 1, 2 \cdots r$ we can find by Lemma 2 functions $f_i \in H^{\infty}_{F_i \cup (K \setminus \overline{F}_i)}$ with $f_i = 1$ on F_i , $||f_i|| \leq 2$ and $|f_i| < \eta/3r$ on $K \setminus W_i$.

Choose $x_i \in X_i$ for each i and put $f(z) = 1/N \sum_{i=1}^r f_i(z)h(x_i), z \in F \cup (K \setminus \overline{F})$. Clearly $f \in H^{\infty}_{F \cup (K \setminus \overline{F})}$ and $||f|| \leq 3$ by (a). If $z \in K \setminus W$ then $|f_i(z)| < \eta/r$ for each i so $|f(z)| < \eta$.

Finally let $z \in F$. Then

$$egin{aligned} f(z) &= rac{1}{N} \left(\sum\limits_{z \,\in\, X_i} + \sum\limits_{z \,\in\, W_i \setminus X_i} + \sum\limits_{z \,\in\, W_i}
ight) f_i(z) h(x_i) \ &= f_1(z) \,+\, f_2(z) \,+\, f_3(z), \,\, ext{say.} \end{aligned}$$

We have

$$egin{aligned} ert f_{\scriptscriptstyle 1}(z) \, - \, h(z) ert &\leq \left| rac{1}{N} \sum_{z \, \in \, X_i} f_i(z) (h(z) \, - \, h(x_i))
ight| \ &+ \left| 1 - rac{N_z}{N}
ight| < rac{\eta N_z}{8N} + \left| 1 - rac{N_z}{N}
ight| < \eta/3 \; , \end{aligned}$$

by (a), since $|z - x_i| < \delta$. Moreover, $|f_2(z)| < \sum_{i=1}^r \eta/3$, by (b) and $|f_3(z)| < \sum_{i=1}^r \eta/3r = \eta/3$, so that we have $|f(z) - h(z)| < \eta$ as required.

LEMMA 4. With F as in the theorem, if W is any open neighborhood of F and h a bounded continuous function on W with $||h|| \leq 1$, we can find $G \in H_{F \cup (K \setminus \overline{F})}$ with $|G - h| < \eta$ on F, $||G|| \leq 7$, and $|G| < \eta$ outside W.

Proof. Choose a sequence $\{W_n\}$ of relatively compact open subsets of W with $W = \bigcup_{n=1}^{\infty} W_n$, such that $\overline{W}_n \cap \overline{W}_n = \emptyset$ if |m - n| > 1. We can write $h = \sum_{n=1}^{\infty} h_n$ on W where $h_n \in C(K)$ has support in W_n and $||h_n|| \leq 1$. By Lemma 3 for each n we can find $f_n \in H^{\infty}_{F \cup (K \setminus \overline{F})}$ with $|f_n - h_n| < 2^{-n}\eta$ on F, $|f_n| < 2^{-n}\eta$ on $K \setminus W$, and $||f_n|| \leq 3$. Then $G = \sum_{n=1}^{\infty} f_n$ has the required properties.

Proof of Theorem 1. By Lemma 4 and using the fact that g can be approximated uniformly by functions continuous in a neighborhood of F, we can construct by induction on n a sequence $\{G_n\}_{n=0}^{\infty}$ in $H_{F\cup(K\setminus\overline{F})}^{\infty}$ such that, writing $f_n = G_0 + \cdots + G_n$ we have:

(1)
$$|G_{\scriptscriptstyle 0}-g|<\lambda/7$$
 on F ,

$$(1)_n \qquad |G_n + f_{n-1} - (1 + \lambda + \cdots + \lambda^n)g| < rac{\lambda^{n+1}}{7}$$

on F, n > 1, where $\lambda = 9/10$

$$(2)_{n} \qquad ||G_{n}|| \leq 7 ||f_{n-1} - (1 + \lambda + \cdots + \lambda^{n})g||_{F} < 8\lambda^{n}$$

 $(3)_n$ $||f_n|| \leq 1 + \lambda + \cdots + 9\lambda^n$.

(To get (3)_n observe that by $(1)_{n-1}$ we have $|f_{n-1}| < 1 + \lambda + \cdots + \lambda^{n-1} + \lambda^n/7$ on F, and hence on a neighborhood of F; if we make $|G_n| < \lambda^{n-1}/10$ outside this neighborhood then (3)_n follows from (2)_n and (3)_{n-1}).

$$(\ 4 \)_n \qquad \qquad | \ G_n | < 2^{-n} \ ext{ on } \ K ackslash V$$
 .

Then $(2)_n$ shows that $f_n \to G$ say uniformly on K, so $G \in H^{\infty}_{F \cup (K \setminus \overline{F})}$; by $(1)_n G = 10g$ on F and by $(3)_n ||G|| \leq 10$. Finally by $(4)_n |G| < \eta$ on $K \setminus V$. Then f = (1/10)G is the required function.

REMARK. The metric condition on F in Theorem 1 is clearly satisfied if F has zero one-dimensional Hausdorff measure; however it is also satisfied by sets which are thicker in the direction of the complex tangent space, e.g. any smooth arc in ∂K whose tangent at each point lies in the complex tangent space.

If F is compact then of course it is a peak interpolation set, so Theorem 1 extends the Rudin-Carleson theorem. The extension to nonclosed sets in the case of the disc has been obtained independently by Detraz [1], and subsequently generalized to other domains in the plane by A. Stray (private communication).

If we assume that F has zero one-dimensional Hausdorff measure then we can make do with a weaker pseudoconvexity hypothesis at the points of F. We say that ∂K is point pseudoconvex at ζ if there exists a neighborhood N of ζ and a real C^2 strictly plurisubharmonic function ρ in N such that $\rho(\zeta) = 0$ and $\rho(z) \leq 0$ in $N \cap K$.

THEOREM 2. Let K be holomorphically convex, and let F be a subset of ∂K with zero one-dimensional Hausdorff outer measure such that ∂K is point pseudoconvex at each point of F. Let V be a neighborhood of F in K, let $\eta > 0$, and let g be a bounded continuous function on F with $||g|| \leq 1$.

Then we can find $f \in H^{\infty}_{F \cup (K \setminus \overline{F})}$ with f | F = g, $|| f || \leq 1$ and $| f | < \eta$ on $K \setminus V$.

Proof. We show that the conclusion of Lemma 2 holds; the rest of the proof is just as before. As in the proof of Lemma 2 for each $\zeta \in F$ we can find positive constants m_{ζ} and M_{ζ} , a neighborhood W_{ζ} of ζ , and $G_{\zeta} \in H(K)$ such that

(a) $m_{\zeta}|\zeta-z|^2 \leq \operatorname{Re} G_{\zeta}(z), \qquad z \in K$

(b) $|G_{\zeta}(z)| \leq M_{\zeta} |\zeta - z|, \qquad z \in K.$

Then whenever $\zeta \in U \subset W_{\zeta}$ and $z \in U$ we have $|G_{\zeta}(z)| \leq M_{\zeta} \dim (U)$. We define F_n as before and cover F_n by balls $\Delta_i^{(n)}$ such that $\sum_i \dim (\Delta_i^n) < \varepsilon n^{-2}2^{-n-2}$. The rest of the proof goes just as before, with c_j replaced by diam (Δ_j) . COROLLARY. Let F be a compact subset of ∂K with zero 1-dimensional Hausdorff measure and assume ∂K is point pseudoconvex at each point of F. Then F is a peak interpolation set for A(K).

Finally we remark that the functions obtained in Theorem 1 and 2 are actually pointwise limits on K° of bounded sequences in H(K); this follows from the construction. If F is compact the peak-interpolating functions constructed are in $\overline{H}(K)$; in this case the proof simplifies somewhat since it is only necessary to take finite products in Lemma 2 and the theorem follows from Lemma 2 by general theorems on peak interpolation sets.

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